Introduction to Programming Homework 6

Due Friday Nov 4

You will turn in your homework via e-mail (andrew.yarmola@uni.lu). For this homework, you will work in a text editor of your choosing. See instructions from the previous homework on how to write modules.

Exercise 1 (Generators)

Make a module called generators.py. You will implement the following three generators.

• **a.** (Binary Decimal Expansion) Given a ratio m/n of positive integers with $m \le n$, we can consider the binary expansion

$$\frac{m}{n} = \sum_{i=1}^{\infty} \frac{a_i}{2^i}.$$

Write a generator function binary_decimal(m,n) which yields the sequence a_i in order. For example,

```
import generators as gen
  one_third = gen.binary_decimal(1,3)
  for _ in range(5) :
     print(next(one_third))

should print

0
     1
     0
     1
     0
     1
     0
```

Be sure to raise an error on bad input.

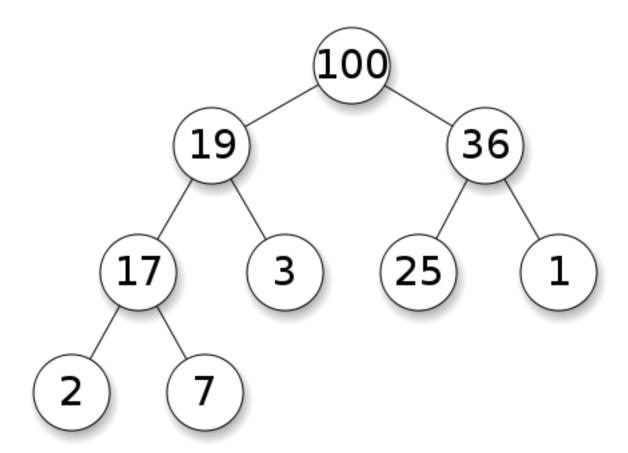
- **b.** (Biased coin from a fair one) A common problem in computer science is to take one pseudorandom number generator and use it to construct another. We can model a fair coin flip by using random.randint(0, 1) form the random module. This returns a 0 or a 1 with equal probability. **Using this fair coin**, write a function biased_coin(m,n) that returns 1 with probability exactly m/n.
 - Hint : Make use of part a.

- c. (Shuffle generator) Write a generator shuffle_gen(start, stop) that returns random numbers between start and stop without repetition. Make sure this works for very large integers.
 - Hint: See the modern version of the Fisher-Yates shuffle at
 <u>https://en.wikipedia.org/wiki/Fisher-Yates_shuffle#Modern_method</u> but instead of swapping numbers into a list you should use a better data structure.

Exercise 2 (Heap)

Create a module called heap.py.

A binary heap is a binary tree with the property that for every node x one has x.data >= x.left.data and x.data >= x.right.data. For example, this image represents a heap



In this exercise, we will create a Heap class that will manage a tree with the heap property. **Instead** of using the Node class from the previous homework, the Heap will **store all data in a list in level-order** (i.e. we read off each level of the tree from left to right). For example, the data in the tree above will stored as the list

You can see that the node at index i of data_list has the left child at index 2*i+1 and the right child at index 2*i+2. Similarly, you can use the index in the list to find a node's parent.

You will notice that with this structure, the maximum of the data in the tree is always the first element of the list. Our goal will be to write methods that allow us to insert new data into the heap and to remove the largest value from the heap all while preserving the heap property.

- **a.** Create a class called Heap. Inside, you will store a private self._data_list attribute. The init method should simply have type __init__(self) where you initialize the data list. In part **b**, we will be inserting elements to the end of self._data_list and then using the following methods to force the heap property using the following methods:
 - def bubble down(self, i):
 - start with the node at index i
 - if the data at index i is larger than that of its children, stop.
 - if not, switch the data at index i with either child that has greater value.
 - continue doing this process to the child until you stop.
 - def bubble up(self, i):
 - start with the node at index i
 - if the data at index i is smaller than that of its parent, stop.
 - if not, switch the data at index i with that of its parent.
 - continue doing this process to the parent until you stop.

Do not use recursion for the above methods!

- **b.** We will now us the _bubble_down and _bubble_up methods to insert elements into the heap and delete the largest value. Implement the following methods:
 - def insert(self, value):
 - add value at the end of self._data_list
 - run self._bubble_up to move the newly inserted element into a position that doesn't violate the heap property.
 - def pop max(self):
 - record the first value of self. data list
 - replace the first value of self. data list with the last value
 - use self._bubble_down to push this replaced value down until it doesn't violate the heap property.
 - return the recorded first value as the maximum in the heap.

Observe that you can now sort a list of data by inserting elements one by one into a heap and then using pop max() to read off the sorted list from largest to smallest.

• c. Create a global function called sort_all_lines(path_to_file) which will read a file at path_to_file. Each line of path_to_file will be a comma separated list of integers. Use the heap class you built above to sort each line from greatest to smallest. Write you data to a file named as follows: if path_to_file = 'dir1/dir2/filename.extension save your file to 'dir1/dir2/filename_sorted.extension'. For example, if file 'test_data.csv' contains

```
4,6,1,47,241,352,7,0,-140,352
35,2601,362,1350305,-9352,38351
```

you code should write a file called test_data_sorted.csv as

```
352, 352, 241, 47, 7, 6, 4, 1, 0, -140
1350305, 38351, 2601, 362, 35, -9352
```