

Chapter 5 Some Discrete Probability Distributions

Binomial: Two possible outcomes from each trial.

Binomial Distribution: $b(x; n, p) = \binom{n}{x} p^x q^{n-x}$ x: num of successes. n: num of indep. trials. p: prob. of success. q: prob. of failure. $\mu = np$, $\sigma^2 = npq$

Multinomial: $f(x_1, x_2, \dots, x_k; p_1, p_2, \dots, p_k, n) = \binom{n}{x_1, x_2, \dots, x_k} p_1^{x_1} p_2^{x_2} \dots p_k^{x_k}$. $n = \sum_{i=1}^k x_i$, and $\sum_{i=1}^k p_i = 1$

Hypergeometric: Choosing successful items.

Hypergeometric Distribution: $h(x; N, n, k) = \frac{\binom{k}{x} \binom{N-k}{n-x}}{\binom{N}{n}}$. $\max(0, n - (N - k)) \leq x \leq \min(n, k)$. x: num of successes. N: num of items. n: num of selection. k: num of total successes. $\mu = \frac{nk}{N}$, $\sigma^2 = \frac{N-n}{N-1} n \frac{k}{N} (1 - \frac{k}{N})$

Estimating Hypergeometric using Binomial: If n is small compared to N : $(n/N) \leq 0.05$.

Chapter 6 Some Continuous Probability Distributions

Uniform Distribution: Equal Probability throughout interval.

$f(x; A, B) = \frac{1}{B-A}$ if $A \leq x \leq B$, 0 otherwise. $\mu = \frac{A+B}{2}$, $\sigma^2 = \frac{(B-A)^2}{12}$.

Normal Distribution: Bell curve. $n(x; \mu, \sigma) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2\sigma^2}(x-\mu)^2}$. x: select time. μ : mean. σ : standard deviation.

Standard Normal: A normal distribution where mean is 0 and variance is 1. $Z = \frac{X-\mu}{\sigma}$

Estimating Binomial with Normal: For large n . $P(X \leq x) \approx P(Z \leq \frac{x+0.5-np}{\sqrt{npq}})$

Gamma Function: $\Gamma(n) = (n-1)!$. $\Gamma(1) = 1$. $\Gamma(1/2) = \sqrt{\pi}$.

Gamma Distribution: Wait time, reliability. $f(x; \alpha, \beta) =$

Multivariate: $f(x_1, x_2, \dots, x_k; a_1, a_2, \dots, a_k, N, n) = \frac{\binom{a_1}{x_1} \binom{a_2}{x_2} \dots \binom{a_k}{x_k}}{\binom{N}{n}}$. $n =$

$\sum_{i=1}^k x_i$, $N = \sum_{i=1}^k a_i$.

Negative Binomial Distribution: Prob. the k th success will happen by the x th trial. $b^*(x; k, p) = \binom{x-1}{k-1} p^k q^{x-k}$. x: trial number. k: success number. p: prob. success. q: prob. failure.

Geometric Distribution: Prob. the x th trial is the first success. $g(x; p) = pq^{x-1}$. x: trial number. p: prob. success. q: prob. failure. $\mu = \frac{1}{p}$. $\sigma^2 = \frac{1-p}{p^2}$.

Poisson Distribution: Prob. something happens x times in t time.

$p(x; \lambda t) = \frac{e^{-\lambda t} (\lambda t)^x}{x!}$. x: num of times. λ : average number of outcomes per time period. t: time interval.

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$\frac{1}{\beta^\alpha \Gamma(\alpha)} x^{\alpha-1} e^{-\frac{x}{\beta}}$, $x > 0$. or 0 otherwise. $\mu = \alpha\beta$, $\sigma^2 = \alpha\beta^2$.

Exponential Distribution: Special case of Gamma where $\alpha = 1$.

$f(x; \beta) = \frac{1}{\beta} e^{-\frac{x}{\beta}}$ where $x > 0$. 0 elsewhere. β : mean time between failures. α : number of events. $\mu = \beta$, $\sigma^2 = \beta^2$.

Chi-Squared Distribution: Special case of Gamma where $\alpha = v/2$ and $\beta = 2$. $f(x; v) = \frac{1}{2^{v/2} \Gamma(v/2)} x^{v/2-1} e^{-x/2}$, $x > 0$. 0 elsewhere. v: degrees of freedom. $\mu = v$, $\sigma^2 = 2v$.

Beta Function: $B(\alpha, \beta) = \frac{\Gamma(\alpha)\Gamma(\beta)}{\Gamma(\alpha+\beta)}$, $\alpha, \beta > 0$.

Beta Distribution: $f(x) = \frac{1}{B(\alpha, \beta)} x^{\alpha-1} (1-x)^{\beta-1}$, $0 < x < 1$. 0 elsewhere. $\mu = \frac{\alpha}{\alpha+\beta}$, $\sigma^2 = \frac{\alpha\beta}{(\alpha+\beta)^2(\alpha+\beta+1)}$.

Chapter 8 Fundamental Sampling Distributions and Data Descriptions Chapter 9 One- and Two-Sample Estimation Problems