CS 375 Homework 1 Anchu A. Lee

I have done this assignment completely on my own. I have not copied it, nor have I given my solution to anyone else. I understand that if I am involved in plagiarism or cheating I will have to sign an official form that I have cheated and that this form will be stored in my official university record. I also understand that I will receive a grade of 0 for the involved assignment for my first offense and that I will receive a grade of F for the course for any additional offense.

1. Use the Master theorem to solve the following recurrences.
   (a) $T(n) = 3T(n/4) + n$
   (b) $T(n) = 2T(n/4) + \sqrt{n}lg(n)$
   (c) $T(n) = 5T(n/2) + n^2$
2. Solve the recurrence
$$T(n) = \begin{cases} \Theta(1) & \text{for } n \leq 1 \\ T(n/4) + T(3n/4) + n & \text{otherwise} \end{cases}$$
   using the recursion tree method. Draw the recursion tree and show the aggregate instruction counts for the following levels (0th, 1st, and last levels), and derive the growth class for T(n) with justifications.
3. Use the substitution method to prove that $T(n) = T(n-1) + n \in O(n^2)$