

Math 327 Homework 3
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Question 4.2

x	0	1	2	3
$f(x)$	$\frac{27}{64}$	$\frac{27}{64}$	$\frac{9}{64}$	$\frac{1}{64}$

$$E(X) = \sum_{x=0}^3 x \cdot f(x) = 0 \cdot \frac{27}{64} + 1 \cdot \frac{27}{64} + 2 \cdot \frac{9}{64} + 3 \cdot \frac{1}{64} = \frac{3}{4}$$

Question 4.4

$$P(H) = \frac{3}{4}, P(T) = \frac{1}{4}$$

x	0	1	2
$f(x)$	$\frac{9}{16}$	$\frac{6}{16}$	$\frac{1}{16}$

$$E(X) = 0 \cdot \frac{9}{16} + 1 \cdot \frac{6}{16} + 2 \cdot \frac{1}{16} = \frac{1}{2}$$

Question 4.10

$$\mu_X = 1 \cdot 0.17 + 2 \cdot 0.50 + 3 \cdot 0.33 = 2.16$$

$$\mu_Y = 1 \cdot 0.23 + 2 \cdot 0.50 + 3 \cdot 0.27 = 2.04$$

Question 4.14

$$E(X) = \int_0^1 \frac{x \cdot 2(x+2)}{5} dx = \frac{8}{15}$$

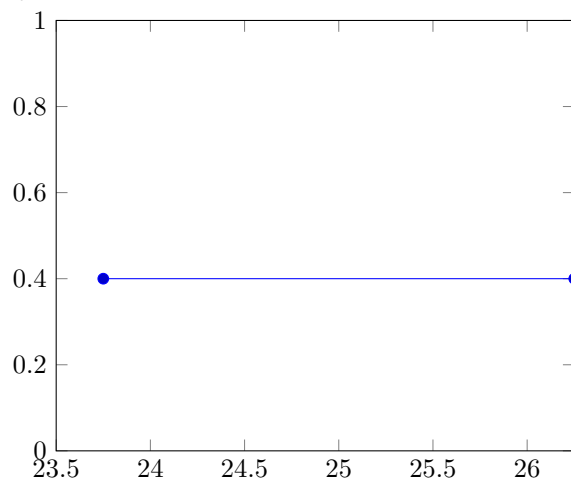
Question 4.18

$$E(X^2) = \sum_{x=0}^3 x^2 \cdot f(x) = 0 \cdot \frac{27}{64} + 1 \cdot \frac{27}{64} + 4 \cdot \frac{9}{64} + 9 \cdot \frac{1}{64} = \frac{9}{8}$$

Question 4.20

$$E(e^{2X/3}) = \int_0^\infty e^{2x/3} \cdot e^{-x} dx = 3$$

Question 4.28



$$E(X) = \int_{23.75}^{26.25} \frac{2}{5} x dx = 25$$

Not suprised, this is the expected value as it is exactly in the middle of the interval.

Question 4.34

$$\mu_X = (-2)(0.3) + (3)(0.2) + (5)(0.5) = 2.5$$

$$\sigma_X^2 = \sum x^2 f(x) - \mu_X^2$$

$$\sum x^2 f(x) = (4)(0.3) + (9)(0.2) + (25)(0.5) = 15.5$$

$$\sigma_X^2 = 15.5 - 2.5^2 = 9.25$$

$$\sigma = 3.04138...$$

Question 4.38

$$\begin{aligned}\mu_X &= \frac{8}{15} \\ \sigma_X^2 &= \int_0^1 x^2 \frac{2(x+2)}{5} dx - \mu_X^2 \\ \int_0^1 x^2 \frac{2(x+2)}{5} dx &= \frac{11}{30} \\ \sigma_X^2 &= \frac{11}{30} - \left(\frac{8}{15}\right)^2 = \frac{37}{450}\end{aligned}$$

Question 4.40

$$\begin{aligned}g(X) &= 3X^2 + 4 \\ \mu_{g(X)} &= \int_0^1 (3x^2 + 4) \frac{2(x+2)}{5} dx = 5.1 \\ \sigma_{g(X)}^2 &= \int_0^1 (3x^2 + 4)^2 \frac{2(x+2)}{5} dx - \mu_{g(X)}^2 \\ \int_0^1 (3x^2 + 4) \frac{2(x+2)}{5} dx &= \frac{671}{25} \\ \sigma_{g(X)}^2 &= \frac{671}{25} - (5.1)^2 = 0.83\end{aligned}$$

Question 4.46

$$\begin{aligned}k &= \left(\frac{3}{392}\right)10^{-4}, g(x) = k(20x^2 + \frac{98000}{3}) \\ u_X &= \int_{30}^{50} x \cdot \left(\frac{3}{392}\right)10^{-4}(20x^2 + \frac{98000}{3})dx = 40.81632... \\ u_Y &= \int_{30}^{50} y \cdot \left(\frac{3}{392}\right)10^{-4}(20y^2 + \frac{98000}{3})dy = 40.81632... \\ E(XY) &= \int_{30}^{50} \int_{30}^{50} kxy(x^2 + y^2)dydx = k \int_{30}^{50} 800x^3 + 1360000xdx \\ E(XY) &= k \int_{30}^{50} 800x^3 + 1360000xdx = 1665.30612... \\ \sigma_{XY} &= E(XY) - u_X u_Y = -0.6642...\end{aligned}$$

Question 4.58

$$\begin{aligned}E(Y) &= 60E(X^2) + 39E(X) \\ E(X) &= \int_0^1 x^2 + \int_1^2 x(2-x) = 1 \\ E(X^2) &= \int_0^1 x^3 + \int_1^2 x^2(2-x) = \frac{7}{6} \\ E(Y) &= (60)\left(\frac{7}{6}\right) + (39)(1) = 109 \text{ kwh}\end{aligned}$$

Question 4.60**Question 4.62****Question 4.64****Question 4.76****Question 4.92****Question 4.98**