

Let $z \in \mathbb{C}$ For any positive integer k , $|z^k| = |z|^k$ Proof by induction.

$$k^1 = |k|^1.$$

$$z^{k+1} = z^k \cdot z$$

$$\text{By 4 of modulus properties } |z^k \cdot z| = |z^k| \cdot |z| = |z|^{k+1}$$