

Example of Determining Uncertainty

ME 552

A displacement transducer has the relationship, $y=Bv$. Determine the uncertainty in y for $V=5.00$ V, if $B=12$ mm/V and $u_B=\pm 0.15$ mm/V and $u_V=\pm 0.05$ V at 95% confidence.

Example for Determining Uncertainty

Displacement

transducer with curve $y = Bv$, determine the uncertainty in y for $v = 5.00V$,
if $B = 12 \text{ mm/V}$ with $u_B = \pm 0.15 \text{ mm/V}$ and $u_v = \pm 0.05V$ at
95% confidence

Known

$$\begin{aligned} y &= Bv & u_v &= \pm 0.05V \\ v &= 5.00V & u_B &= \pm 0.15 \text{ mm/V} \\ B &= 12 \text{ mm/V} \end{aligned}$$

Find

u_y

Solution:

I. Propagation of Error

$$y = Bv \quad \frac{\partial y}{\partial v} = B, \quad \frac{\partial y}{\partial B} = v$$

$$u_y = \left[\left[\left(\frac{\partial y}{\partial v} \right) u_v \right]^2 + \left[\left(\frac{\partial y}{\partial B} \right) u_B \right]^2 \right]^{1/2} = u_y = \left[(B \cdot u_v)^2 + (v \cdot u_B)^2 \right]^{1/2}$$

$$u_y = \left[(12 \cdot 0.05)^2 + (5 \cdot 0.15)^2 \right]^{1/2} = 0.96 \text{ mm}$$

$$y = (12 \text{ mm/V})(5.00V) = 60 \text{ mm} \quad \boxed{60 \pm 0.96 \text{ mm}}$$

II. Sequential Perturbation

$$y_0 = Bv$$

$$y_0 = 60 \text{ mm}$$

$$y_1^+ = (B + u_B)v \quad y_1^- = (B - u_B)v$$

$$y_2^+ = B(v + u_v) \quad y_2^- = B(v - u_v)$$

$$\delta y_1 = \frac{|y_1^+ - y_0| + |y_1^- - y_0|}{2}, \quad \delta y_2 = \frac{|y_2^+ - y_0| + |y_2^- - y_0|}{2}$$

$$u_y = \pm \left[(\delta y_1)^2 + (\delta y_2)^2 \right]^{1/2} = \pm 0.96 \text{ mm}$$

$$\boxed{60 \pm 0.96 \text{ mm}}$$