

1: *"Given values"*

2: Width = 20 [m] *"Room width"*

3: Height = 2.5 [m] *"Room height"*

4: T_1 = converttemp(C,K,25) *"Initial room temperature"*

5: P_1 = 100 [kPa] *"Initial room pressure"*

6: P_in = 110 [kPa] *"Supply pressure"*

7: T_in = converttemp(C,K,15) *"Supply temperature"*

8: V_dot = 2.78 [m^3/s] *"Supply volumetric flow rate"*

9: P_atm = 100 [kPa] *"Hallway pressure"*

10: K = 0.0157 [kg/(s*Pa^0.65)] * convert(kg/(s*Pa^0.65),kg/(s*kPa^0.65)) *"Orifice constant"*

11: Q_dot = 3.5 [kW] *"Energy in"*

12: h_conv = 15 [W/(m^2*K)] * convert(W/(m^2*K), kW/(m^2*K)) *"Heat transfer coefficient"*

13: t_start = 0 [min] * convert(min,s) *"Start time"*

14: t_stop = 1 [min] * convert(min,s) *"Stop time"*

15:

16: *"Derived values"*

17: V_room = Width * Width * Height *"Volume of the room"*

18: A_walls = (2 * Width * Width) + (4 * Width * Height) *"Surface area of walls/floors/ceiling"*

19: rho_supply = density(Air,T=T_in,P=P_in) *"Supply air density"*

20: m_dot_in = V_dot * rho_supply *"Supply mass flow rate"*

21: s_in=entropy(Air,T=T_in,P=P_in) *"Supply air entropy"*

22: h_in=enthalpy(Air,T=T_in) *"Supply air enthalpy"*

23: h_1=enthalpy(Air,T=T_1) *"Initial enthalpy of room"*

24: MW_air=molarmass(Air) *"Molar mass of air"*

25: rho_1=density(Air,T=T_1,P=P_1) *"Density of air at t=0"*

26: m_1 = rho_1 * V_room *"Mass of air at t=0"*

27: n_1 = m_1/MW_air *"Number of moles of air at t=0"*

28: R_air = (P_1*V_room)/(n_1*T_1) *"Specific gas constant of air"*

29: u_1 = intenergy(Air,T=T_1) *"Internal energy of gas in room initially"*

30:

31: *"Equations for Part A"*

32: m_dot_2 = K * DELTA_P_2^0.65 *"Given equation for orifice"*

33: DELTA_P_2 = P_2 - P_atm *"Differential pressure at given time"*

34: DELTA_T_2 = T_2 - T_1 *"Temperature difference between the room and the surrounding rooms"*

35: W_2 = h_conv * A_walls * DELTA_T_2 *"Energy lost through the walls"*

36: h_2=enthalpy(Air,T=T_2) *"Enthalpy of air leaving room"*

37: u_2=intenergy(Air,T=T_2) *"Internal energy of the room"*

38: Q_dot - W_2 - (m_dot_2 * h_2) + (m_dot_in * h_in) = dEdt *"Energy balance equation"*

39: P_2 * V_room = (m_2 / MW_air) * R_air * T_2 *"Ideal gas law"*

40: m_dot_net = m_dot_in - m_dot_2 *"Net mass flow rate into room"*

41: m_2 = m_1 + integral(m_dot_net, time) *"Mass balance of the air in the room"*

42: m_2*u_2 - m_1*u_1 = integral(dEdt, time) *"Net change in internal energy of the room"*

43:

44: *"Equations for Part B"*

45: m_dot_3 = m_dot_in *"Conservation of mass at equilibrium"*

46: DELTA_P_3 = P_3 - P_atm *"Differential pressure at equilibrium"*

47: m_dot_3 = K * DELTA_P_3^0.65 *"Given equation for orifice"*

48: DELTA_T_3 = T_3 - T_1 *"Temperature difference between the room and the surrounding rooms"*

49: W_3 = h_conv * A_walls * DELTA_T_3 *"Energy lost through the walls"*

50: h_3=enthalpy(Air,T=T_3) *"Enthalpy of air leaving room"*

51: Q_dot - W_3 = (m_dot_3 * h_3) - (m_dot_in * h_in) *"Energy balance equation"*

Given values

$$\text{Width} = 20 \text{ [m] } \textit{Room width}$$

$$\text{Height} = 2.5 \text{ [m] } \textit{Room height}$$

$$T_1 = \text{ConvertTemp} [\text{C}, \text{K}, 25] \textit{ Initial room temperature}$$

$$P_1 = 100 \text{ [kPa] } \textit{Initial room pressure}$$

$$P_{\text{in}} = 110 \text{ [kPa] } \textit{Supply pressure}$$

$$T_{\text{in}} = \text{ConvertTemp} [\text{C}, \text{K}, 15] \textit{ Supply temperature}$$

$$\dot{V} = 2.78 \text{ [m}^3\text{/s] } \textit{Supply volumetric flow rate}$$

$$P_{\text{atm}} = 100 \text{ [kPa] } \textit{Hallway pressure}$$

$$K = 0.0157 \text{ [kg/(s*Pa}^{0.65})] } \cdot \left| 89.13 \cdot \frac{\text{kg/(s*kPa}^{0.65})}{\text{kg/(s*Pa}^{0.65})} \right| \textit{ Orifice constant}$$

$$\dot{Q} = 3.5 \text{ [kW] } \textit{Energy in}$$

$$h_{\text{conv}} = 15 \text{ [W/(m}^2\text{*K)] } \cdot \left| 0.001 \cdot \frac{\text{kW/(m}^2\text{*K)}}{\text{W/(m}^2\text{*K)}} \right| \textit{ Heat transfer coefficient}$$

$$t_{\text{start}} = 0 \text{ [min] } \cdot \left| 60 \cdot \frac{\text{s}}{\text{min}} \right| \textit{ Start time}$$

$$t_{\text{stop}} = 1 \text{ [min] } \cdot \left| 60 \cdot \frac{\text{s}}{\text{min}} \right| \textit{ Stop time}$$

Derived values

$$V_{\text{room}} = \text{Width} \cdot \text{Width} \cdot \text{Height} \textit{ Volume of the room}$$

$$A_{\text{walls}} = 2 \cdot \text{Width} \cdot \text{Width} + 4 \cdot \text{Width} \cdot \text{Height} \textit{ Surface area of walls/floors/ceiling}$$

$$\rho_{\text{supply}} = \rho [\text{Air}, T = T_{\text{in}}, P = P_{\text{in}}] \textit{ Supply air density}$$

$$\dot{m}_{\text{in}} = \dot{V} \cdot \rho_{\text{supply}} \textit{ Supply mass flow rate}$$

$$s_{\text{in}} = s [\text{Air}, T = T_{\text{in}}, P = P_{\text{in}}] \textit{ Supply air entropy}$$

$$h_{\text{in}} = h [\text{Air}, T = T_{\text{in}}] \textit{ Supply air enthalpy}$$

$$h_1 = h [\text{Air}, T = T_1] \textit{ Initial enthalpy of room}$$

$$MW_{\text{air}} = \text{MolarMass} [\text{Air}] \textit{ Molar mass of air}$$

$$\rho_1 = \rho [\text{Air}, T = T_1, P = P_1] \textit{ Density of air at t=0}$$

$$m_1 = \rho_1 \cdot V_{\text{room}} \textit{ Mass of air at t=0}$$

$$n_1 = \frac{m_1}{MW_{\text{air}}} \textit{ Number of moles of air at t=0}$$

$$R_{\text{air}} = \frac{P_1 \cdot V_{\text{room}}}{n_1 \cdot T_1} \quad \text{Specific gas constant of air}$$

$$u_1 = u [\text{Air}, T = T_1] \quad \text{Internal energy of gas in room initially}$$

Equations for Part A

$$\dot{m}_2 = K \cdot \Delta P_{2,2}^{0.65} \quad \text{Given equation for orifice}$$

$$\Delta P_{2,2} = P_2 - P_{\text{atm}} \quad \text{Differential pressure at given time}$$

$$\Delta T_{2,2} = T_2 - T_1$$

Temperature difference between the room and the surrounding rooms

$$W_2 = h_{\text{conv}} \cdot A_{\text{walls}} \cdot \Delta T_{2,2} \quad \text{Energy lost through the walls}$$

$$h_2 = h [\text{Air}, T = T_2] \quad \text{Enthalpy of air leaving room}$$

$$u_2 = u [\text{Air}, T = T_2] \quad \text{Internal energy of the room}$$

$$\dot{Q} - W_2 - \dot{m}_2 \cdot h_2 + \dot{m}_{\text{in}} \cdot h_{\text{in}} = dEdt \quad \text{Energy balance equation}$$

$$P_2 \cdot V_{\text{room}} = \frac{m_2}{MW_{\text{air}}} \cdot R_{\text{air}} \cdot T_2 \quad \text{Ideal gas law}$$

$$\dot{m}_{\text{net}} = \dot{m}_{\text{in}} - \dot{m}_2 \quad \text{Net mass flow rate into room}$$

$$m_2 = m_1 + \int [\dot{m}_{\text{net}}] d \text{ time} \quad \text{Mass balance of the air in the room}$$

$$m_2 \cdot u_2 - m_1 \cdot u_1 = \int [dEdt] d \text{ time} \quad \text{Net change in internal energy of the room}$$

Equations for Part B

$$\dot{m}_3 = \dot{m}_{\text{in}} \quad \text{Conservation of mass at equilibrium}$$

$$\Delta P_{3,3} = P_3 - P_{\text{atm}} \quad \text{Differential pressure at equilibrium}$$

$$\dot{m}_3 = K \cdot \Delta P_{3,3}^{0.65} \quad \text{Given equation for orifice}$$

$$\Delta T_{3,3} = T_3 - T_1$$

Temperature difference between the room and the surrounding rooms

$$W_3 = h_{\text{conv}} \cdot A_{\text{walls}} \cdot \Delta T_{3,3} \quad \text{Energy lost through the walls}$$

$$h_3 = h [\text{Air}, T = T_3] \quad \text{Enthalpy of air leaving room}$$

$$\dot{Q} - W_3 = \dot{m}_3 \cdot h_3 - \dot{m}_{\text{in}} \cdot h_{\text{in}} \quad \text{Energy balance equation}$$