

Midterm #2 Coverage Summary -

Coverage: Chapt. 10 (Navier-Stokes Eqs.)
Chapt. 11 (Exact Solutions)

N-S eqn: (no need to study 10.1)

- understand concept of stress tensor & index notation (τ_{ij})
- velocity gradient tensor $\frac{\partial u_i}{\partial x_j}$ can be written as sum

of two parts $\frac{\partial u_i}{\partial x_j} = e_{ij} + \frac{1}{2} \zeta_k \epsilon_{kij}$

$e_{ij} = \frac{1}{2} \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right)$ strain rate tensor

$\zeta_k = \left(\frac{\partial u_i}{\partial x_j} - \frac{\partial u_j}{\partial x_i} \right)$ vorticity

- stress-strain rate model

$\frac{\partial \tau_{ji}}{\partial x_j}$ is the net viscous force/volume.

model: $\tau_{ji} = 2\mu e_{ji}$ stress tensor is proportional to strain rate tensor

If τ_{ji} (as used in the text) is to

include all of the forces (Press., viscous, & volume compression)

$$\tau_{ji} = \underbrace{-\frac{2}{3}\mu\theta\delta_{ji}}_{\text{vol. comp.}} - \underbrace{p\delta_{ji}}_{\text{press}} + \underbrace{2\mu e_{ji}}_{\text{viscous}}$$

Resulting N-S eqn.

- know the physics of each term
- how to simplify is incompressible, $\mu = \text{constant}$.

N-S expressed using vorticity: changes to convective accel. and viscous terms.

Exact Soln: (simplified form)

- what are nonlinear terms
- how to apply boundary & initial conditions
- see example flows to see how integrated to get velocity.
- Stokes 1st problem
 - interpretation of similarity soln.
 - evaluation of wall stress.
 - evaluation of viscous layer, $\delta(t)$
 - evaluation of vorticity, circulation.