An Analysis of the Department of Education Quality Survey and Its Efficacy

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# Abstract

Abstract coming soon!

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#### Introduction

The NYC School Survey seeks to collect data to provide an overview of New York City (NYC) Schools. Beginning in 2005, the survey looks to collect demographic and achievement data for New York City Public Schools, and provide a standardized rating of various elements of school quality.

The survey has changed over the years. This change has come from recommendations of public policy analysts in order to more accurately define the quality of schools *New York City Schools (2018)*. The 2020-21 academic year report provides a robust dataset defined at the school level with academic and socioeconomic data provided.

Research Question: This study aims to determine whether the school ratings within the NYC School Quality Survey accurately reflect educational outcomes, or if other variables related to certain schools can be used as a better proxy.

In our case, we are interested in predicting the 4-year college persistence rate for an NYC high school. This measure is defined as the percent of students who graduate from a high school, and eventually go on to graduate from a 4-year college. Being able to identify the main indicators of a school's ability to successfully prepare students for college can benefit the NYC Department of Education, and New York City Schools along a couple of dimensions:

- 1. More directed instruction to enable useful skill transfer in preparatory courses
- 2. Better use of resourcing available to public schools to increase the percentage of college-ready students

For point 2 above, it's well correlated that students who attend 4-year institutions increase their career potential earnings significantly.

#### Literature Review

One of the main predictors of academic performance is the socioeconomic background of a student. Students from low-income families are nearly four times more likely to drop out of high school than students from wealthy families *Education Statistics* (2008).

Attempts to use more sophisticated modeling techniques and different sources datasets come from several prior studies. Bernacki, Chavez, and Uesbeck (2020) based their modeling off trying to predict based on student digital behavior, rather than social factors. The model in this study reached an accuracy of 75%, and was able to flag early interventions. While this modeling technique attempts to predict the same variable (educational achievement, albeit a different metric where we are predicting college attainment), the base dataset used to train the model and input variables are different.

Similarly, Musso, Cascallar, Bostani, and Crawford (2020) attempted to train an artificial neural network (ANN) to identify variable relationships to educational performance data. They modeled educational performance of Vietnamese students in grade 5. They included individual characteristics as well as information related to daily routines in their training data. This method uses a more sophisticated model, and resulted in accuracy in prediction of 95-100 higher than other modeling techniques. However, the training data came in that case from a different country (Vietnam, rather than the United States). Comparing modeling results from this (and other US-centric studies) may not be prudent.

Yağcı (2022) predicted final grade exams for Turkish students as well via machine learning models. Their input variables were prior exam grades. These can be a good "vacuum" comparison to compare one set of academci performance to another. However, there is a concern that good exam grades (even in one subject) do not correspond to a higher rate of career success later in life Afarian and Kleiner (2003). Additionally, a parent study also found a correlation of up to 0.3 between academic grades and later job performance

Roth, BeVier, Switzer III, and Schippmann (1996).

Measuring the input variables that impact educational outcomes is a difficult task.

With so many confounding variables, it can be difficult to determine direct causal relationships that have an outsized impact

## **Data Sourcing**

The dataset used in this study is published from the NYC School Quality Report for the Academic Year 2020 - 2021. It consists of data from 487 New York City public schools, and 391 variables (in the form of columns). This dataset is defined at the school level, indexed by a school's district borough number (DBN).

In addition to the school quality ratings provided from survey responses in the data, there is average and raw academic performance data included. In addition to these academic indicators, there are socioeconomic variables included as well, such as the percentage of students at a given school in temporary housing services.

#### Methodology

Our primary interest is finding proxy variables within our dataset that can better serve as predictors of 4-year college persistence rates as a given NYC high school than the survey ratings collected by the school quality review. As a result, we'll need to first construct a "base" model that predicts a school's college persistence rate.

We can use two variables as a proxy for the school's survey rating in predicting college persistence:

- Percent of Students in Tempoarary Housing (temp housing pct)
- Economic Need Index (eni\_hs\_pct\_912) this is a measure of the percent of students facing economic hardship at a school (noauthor\_student\_2021?). This measures the economic hardship faced by students measured along a few criteria:

- The student is eligible for public assistance from the NYC Human Resources
   Administration (HRA)
- The student lived in temporary housing in the past four years
- The student is in high school, has a home language other than English, and entered the NYC DOE for the first time within the last four years.

We create a 20% holdout set of data to be used later on in order to evaluate the efficacy of our model's predictive capability. The remaining 80% of the data is to be used for model training and exploratory data analysis (EDA).

For ease of single-node computation, we'll select the variables of interest from our dataset. Notably, these are the survey ratings for each school, as well as our preferred froxy variables. Additionally, we impute both our training and evaluation datasets. Given we are dealing with continuous numeric (and not categorical variables), we use the *Predictive Mean Matching* imputation method native to the R mice package

```
## iter imp variable
```

##

##

3

survey\_pp\_CT

survey\_pp\_RI

```
##
     1
            survey_pp_CT
                           survey_pp_RI
                                          survey_pp_ES
                                                         survey_pp_SE
                                                                        survey_pp_SF
                                                                                       survey
##
     1
         2
            survey_pp_CT
                           survey_pp_RI
                                          survey_pp_ES
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##
     1
         3
            survey pp CT
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                                                                                       survey
##
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            survey pp CT
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                                                                        survey pp SF
                                                                                       survey
                                                         survey_pp_SE
##
     1
         5
            survey pp CT
                           survey pp RI
                                          survey pp ES
                                                                        survey_pp_SF
                                                                                       survey
##
     2
            survey pp CT
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                                                                                       survey
         1
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         2
            survey_pp_CT
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                                                                                       survey
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            survey_pp_CT
                           survey_pp_RI
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                                                         survey_pp_SE
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     2
            survey pp CT
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##
                           survey pp RI
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                                                                        survey pp SF
                                                                                       survey
     2
            survey pp CT
##
                           survey_pp_RI
                                          survey_pp_ES
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                                                                        survey_pp_SF
                                                                                       survey
         5
```

survey\_pp\_ES

survey\_pp\_SE

survey\_pp\_SF

survey

```
##
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         2
            survey pp CT
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                                                                        survey_pp_SF
            survey_pp_CT
                           survey_pp_RI
                                                                                       survey
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            survey_pp_CT
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     3
            survey_pp_CT
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                                                                        survey_pp_SF
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            survey_pp_CT
##
     4
                           survey_pp_RI
                                          survey_pp_ES
                                                         survey_pp_SE
                                                                        survey_pp_SF
                                                                                       survey
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     4
            survey_pp_CT
                           survey_pp_RI
                                          survey_pp_ES
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                                                                        survey_pp_SF
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                                                                        survey_pp_SF
##
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            survey_pp_CT
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     4
            survey_pp_CT
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                                                                        survey_pp_SF
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##
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         5
                                                         survey_pp_SE
            survey_pp_CT
                           survey_pp_RI
                                          survey_pp_ES
                                                                        survey_pp_SF
                                                                                       survey
##
     5
            survey_pp_CT
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                                          survey_pp_ES
                                                         survey_pp_SE
                                                                        survey_pp_SF
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     5
##
            survey_pp_CT
                           survey_pp_RI
                                          survey_pp_ES
                                                         survey_pp_SE
                                                                        survey_pp_SF
                                                                                       survey
                                                         survey_pp_SE
##
     5
         3
            survey pp CT
                           survey pp RI
                                                                        survey pp SF
                                          survey_pp_ES
                                                                                       survey
##
     5
            survey_pp_CT
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                                                                        survey_pp_SF
                                                                                       survey
##
     5
            survey_pp_CT
                           survey_pp_RI
                                          survey_pp_ES
                                                         survey_pp_SE
                                                                        survey_pp_SF
                                                                                       survey
##
##
    iter imp variable
##
     1
            survey_pp_CT
                           survey_pp_RI
                                          survey_pp_SE
                                                         college_rate
                                          survey_pp_SE
##
     1
            survey_pp_CT
                           survey_pp_RI
                                                         college_rate
##
     1
            survey_pp_CT
                           survey_pp_RI
                                          survey_pp_SE
                                                         college_rate
##
     1
            survey_pp_CT
                           survey_pp_RI
                                          survey_pp_SE
                                                         college_rate
```

## 1 5 survey\_pp\_CT survey\_pp\_RI survey\_pp\_SE college\_rate ## 2 survey pp CT survey\_pp\_RI survey\_pp\_SE 1 college\_rate 2 ## 2 survey\_pp\_CT survey\_pp\_RI survey\_pp\_SE college\_rate ## 2 3 survey\_pp\_CT survey\_pp\_RI survey\_pp\_SE college\_rate 2 college\_rate ## survey\_pp\_CT survey\_pp\_RI survey\_pp\_SE 2 survey\_pp\_CT survey\_pp\_SE ## 5 survey\_pp\_RI college\_rate ## 3 survey\_pp\_CT survey\_pp\_RI survey\_pp\_SE college\_rate

```
##
    3
        2
           survey pp CT
                         survey pp RI survey pp SE college rate
##
    3
        3
           survey pp CT
                         survey_pp_RI
                                       survey_pp_SE college_rate
##
    3
           survey_pp_CT
                         survey_pp_RI
                                       survey_pp_SE college_rate
           survey pp CT survey pp RI
                                       survey pp SE college rate
##
    3
        5
##
    4
           survey_pp_CT
                        survey_pp_RI
                                       survey_pp_SE college_rate
           survey_pp_CT
                         survey_pp_RI
                                       survey_pp_SE college_rate
##
    4
           survey_pp_CT
                         survey_pp_RI
                                       survey_pp_SE college_rate
##
    4
##
    4
           survey_pp_CT
                         survey_pp_RI
                                       survey_pp_SE college_rate
##
    4
        5
           survey_pp_CT
                         survey_pp_RI
                                       survey_pp_SE college_rate
##
    5
           survey_pp_CT survey_pp_RI
                                       survey_pp_SE college_rate
##
    5
        2
           survey_pp_CT
                         survey_pp_RI
                                       survey_pp_SE college_rate
           survey pp CT survey pp RI
                                       survey pp SE college rate
##
    5
        3
        4
           survey_pp_CT survey_pp_RI
                                       survey_pp_SE college_rate
##
    5
           survey_pp_CT survey_pp_RI
##
    5
                                       survey_pp_SE college_rate
```

To check underlying modeling assumptions, we plot distributions and relationships of different variables. First, we plot the distribution of college persistence rates among NYC high schools to check for normality.

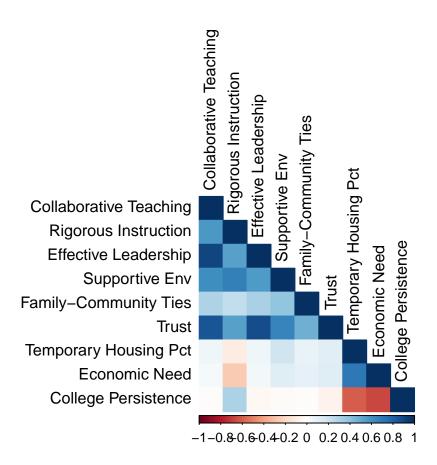


Average 4-Year Colege Persistence Rates: NYC High Schools 2020-2021

The average NYC high school sees ~50% of students go on to have 4-year college persistence.

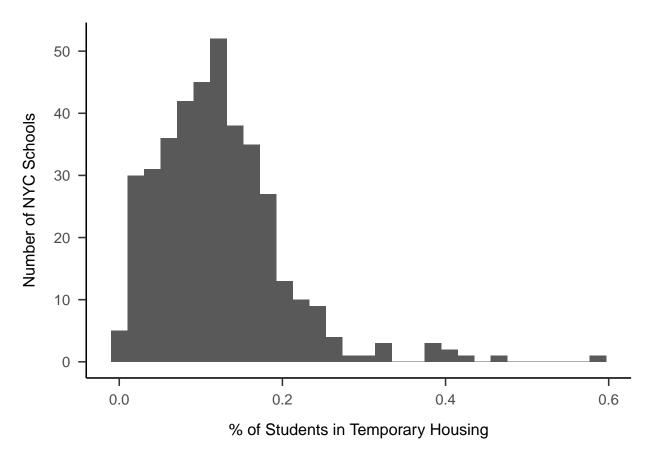
We see a relatively normal distribution of college persistence rates. In the case of NYC high schools, the peak is at around 50%. This is inline with national averages released by US Census Bureau (2023)

The below plot shows the raw correlation between each variable in our pared down dataset (*Collaborative Teaching*, *Trust*, etc) and the response variable of interest: 4-Year College Persistence Rate.



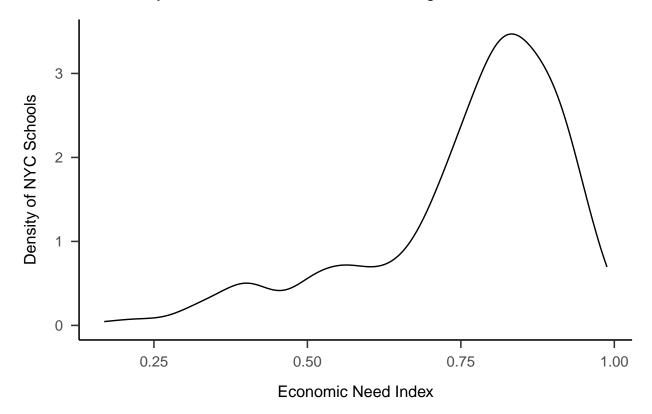
From our correlation plot above, we can see strong negative relationships between our proxy variables of interest (*Temporary Housing Rate* and *Economic Need Index*) and our target variable: *College Persistence Rate*. This gives signal that constructing models based on these variables could give good insight into the factors that most influence college persistence.

Now we can plot the distributions of our proxy variables of interest. First we can plot the temp housing rate:



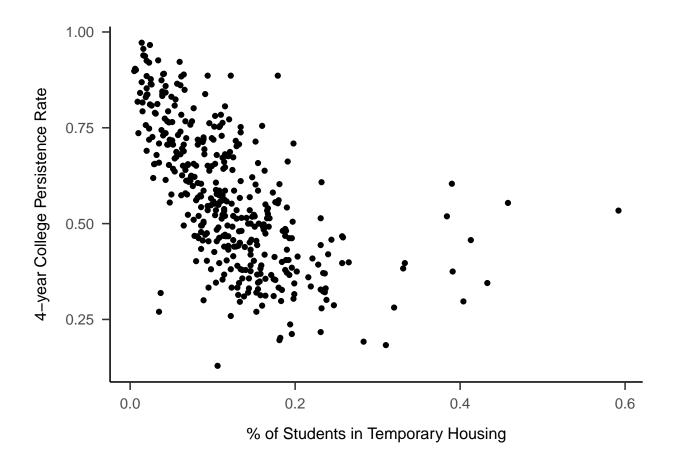
We see this distribution of the percentage of students in temporary housing per school to be skewed left. This will be an important piece of information as we model these relationships later. We also show the distribution of schools' economic need indices (also between 0 and 1). This index is closer to 1 the more economic hardship a student at a school faces (temporary housing use or food assistance, for instance).

Density of Economic Need Index: NYC High Schools 2020–2021

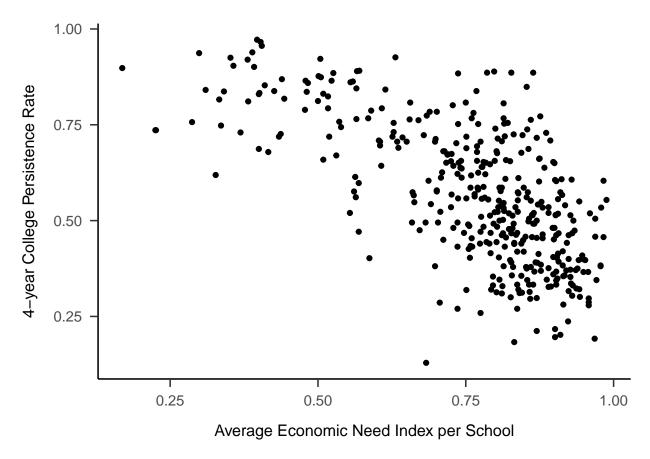


We also see a skewed distribution for our economic need index. This is a candidate for transformation before feeding into our proxy variable model.

First, we should check an assumption of linearity between our predictor and response variables. In this case this a scatter plot of the percentage of students in temporary housing



We see a general linear relationship for schools with lower rates of students in temp housing. However, this linear relationship does **not** visually hold for schools with higher rates of temp housing use.



Again, we see a non-linear relationship between our predictor (*Economic Need Index*) and Outcome Variable (*College Persistence Rate*)

Modeling. For evaluation purposes, we create a linear model based on the survey ratings present per school in our data. We fit this multiple least-squares model to

```
##
## Call:
## lm(formula = base_formula, data = train)
##
## Residuals:
                                      3Q
##
        Min
                   1Q
                        Median
                                              Max
## -0.54578 -0.11206
                       0.00304
                                0.11205
                                         0.41671
##
## Coefficients:
```

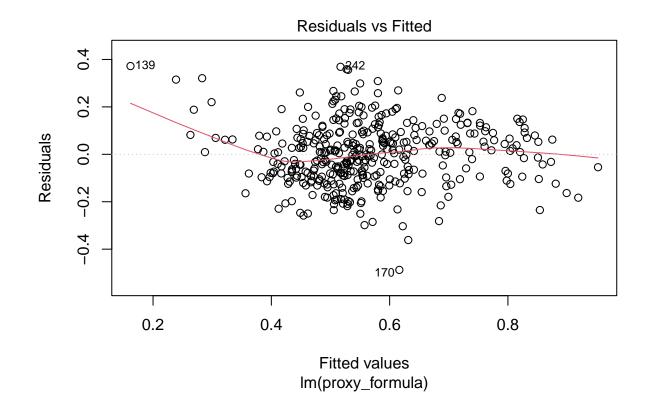
```
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                0.49700
                           0.20023
                                     2.482
                                             0.0135 *
## survey pp CT 0.04036
                           0.27214
                                     0.148
                                             0.8822
## survey pp RI 2.10716
                                            < 2e-16 ***
                           0.19902 10.587
## survey_pp_SE -1.41047
                           0.26337 -5.356 1.47e-07 ***
## survey_pp_ES -0.22948
                           0.28878 -0.795
                                             0.4273
## survey_pp_SF 0.26272
                           0.21171
                                     1.241
                                             0.2154
## survey_pp_TR -0.48790
                           0.42585
                                   -1.146
                                             0.2526
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1592 on 383 degrees of freedom
## Multiple R-squared: 0.2348, Adjusted R-squared: 0.2228
## F-statistic: 19.58 on 6 and 383 DF, p-value: < 2.2e-16
```

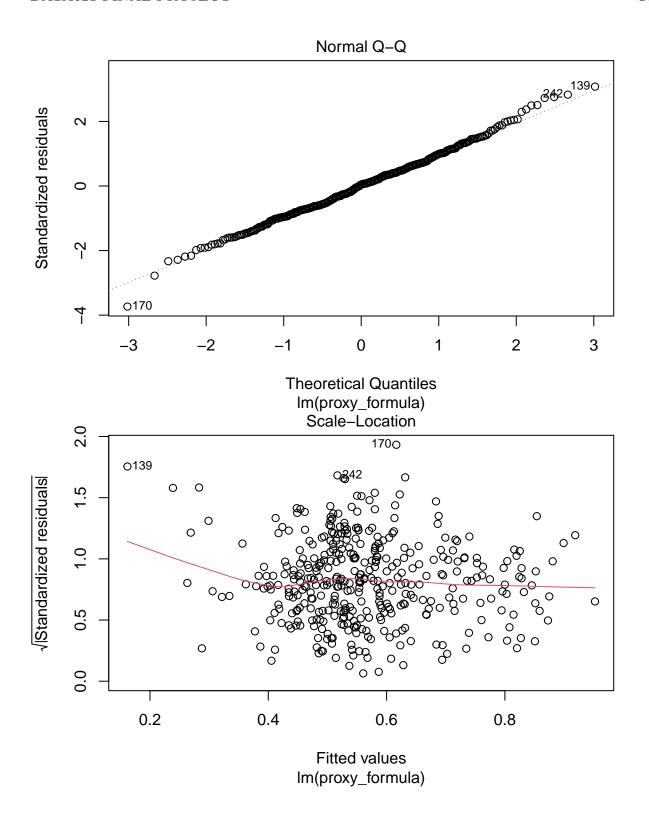
We find our base model for the school survey ratings produces an adjusted R-squared of  $R_{adi}^2 = 0.22$ . This is lower than the predictive model produces in *Roth et al.* (1996).

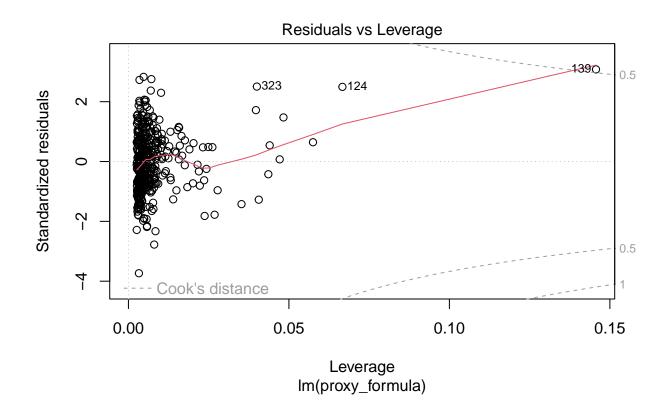
We then create a basic multiple least squares linear model between our two socioeconomic proxy variables: Temporary Housing PErcentage of a School and Average Economic Need Index.

```
##
## Call:
## lm(formula = proxy_formula, data = train)
##
## Residuals:
## Min   1Q   Median   3Q   Max
## -0.48742 -0.09012   0.00566   0.08315   0.37216
```

```
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
                               0.03621 28.873 < 2e-16 ***
## (Intercept)
                    1.04561
## temp_housing_pct -0.61032
                               0.12311 -4.958 1.07e-06 ***
## economic_need
                   -0.53367
                               0.05893 -9.056 < 2e-16 ***
## ---
                  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 0.1307 on 387 degrees of freedom
## Multiple R-squared: 0.4786, Adjusted R-squared: 0.4759
## F-statistic: 177.6 on 2 and 387 DF, p-value: < 2.2e-16
```







Given the

```
##
## Call:
## lm(formula = proxy_formula, data = train, weights = weights)
##
## Weighted Residuals:
##
      Min
                1Q
                   Median
                                3Q
                                       Max
## -4.8222 -0.8301 0.0452 0.7834
                                    3.5360
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                     1.02985
                                0.03260
                                        31.595 < 2e-16 ***
## temp_housing_pct -0.74319
                                0.13149 -5.652 3.08e-08 ***
## economic_need
                    -0.49180
                                0.05594 -8.791
                                                < 2e-16 ***
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.256 on 387 degrees of freedom
## Multiple R-squared: 0.5104, Adjusted R-squared: 0.5078
## F-statistic: 201.7 on 2 and 387 DF, p-value: < 2.2e-16</pre>
```

## **Experimentation and Results**

#### Model Evaluation.

```
## [1] 0.1653904
```

## [1] 0.1366313

## [1] 0.1372144

We can also use the Akaike and Bayesian Information Criterion for evaluating the complexity of our models. We're using fewer variables in our proxy and WLS models, so we'd expect better results (minimized values) for each of those criteria

```
## AIC for base model (rating results): -317.495489747942

## AIC for proxy variable model: -475.126800916888

## AIC for WLS model: -480.729858621265

## BIC for base model (rating results): -285.766315834952

## BIC for proxy variable model: -459.262213960393
```

## BIC for WLS model: -464.86527166477

# Conclusion

# TODO

- Merge/Join in ACT/SAT information by DBN
- Model Selection

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## **Appendices**

Below is the code used to generate this report. It's also available on GitHub here

```
knitr::opts chunk$set(echo = FALSE, warning = FALSE, message = FALSE)
library(tidyverse)
library(gridExtra)
library(glue)
library(mice)
library(corrplot)
library(caret)
library(modelr)
library("papaja")
r_refs("r-references.bib")
# Read in our dataset from GitHub
# https://www.opendatanetwork.com/dataset/data.cityofnewyork.us/bm9v-cvch
df <- read.csv("https://data.cityofnewyork.us/api/views/26je-vkp6/rows.csv?date=20231108</pre>
label_cols <- c("dbn", "school_name", "school_type")</pre>
# Convert needed columns to numeric typing
df <- cbind(df[, label_cols], as.data.frame(lapply(df[,!names(df) %in% label_cols], as.
df$college rate <- df$val persist3 4yr all</pre>
df$economic need <- df$eni hs pct 912
set.seed(42)
# Adding a 20% holdout of our input data for model evaluation later
train <- subset(df[sample(1:nrow(df)), ]) %>% sample_frac(0.8)
test <- dplyr::anti_join(df, train, by = 'dbn')</pre>
cols <- c("survey_pp_CT", "survey_pp_RI",</pre>
          "survey_pp_ES", "survey_pp_SE",
```

```
"survey pp SF", "survey pp TR",
          "temp housing pct", "economic need",
          "college rate")
train_data <- train[, cols]</pre>
imp <- mice(train_data, method="pmm", seed=42)</pre>
train <- complete(imp)</pre>
test data <- test[, cols]</pre>
imp <- mice(test data, method="pmm", seed=42)</pre>
test <- complete(imp)</pre>
# Plot target variable distribution
ggplot(train, aes(x=college rate)) +
    geom_density() +
    labs(x="4-Year College Persistence Rate", y="Density of NYC High Schools", title="Av
theme_set(theme_apa())
# Renaming training dataframe for correlation plot
train renamed <- train %>%
  rename("Collaborative Teaching"=survey pp CT,
         "Rigorous Instruction"=survey_pp_RI,
         "Supportive Env"=survey_pp_SE,
         "Effective Leadership"=survey_pp_ES,
         "Family-Community Ties"=survey_pp_SF,
         "Trust"=survey_pp_TR,
         "Temporary Housing Pct"=temp housing pct,
         "Economic Need"=economic need,
         "College Persistence"=college rate)
```

```
# Create correlation plot between vars of interest
corMatrix <- cor(train renamed)</pre>
corrplot(corMatrix, method="color", type="lower", tl.col="black")
# Plot temp housing rates
ggplot(train, aes(x=temp_housing_pct)) +
 geom_histogram() +
 labs(x="% of Students in Temporary Housing", y="Number of NYC Schools")
# Plot economic need index
ggplot(train, aes(x=economic need)) +
 geom_density() +
 labs(x="Economic Need Index", y="Density of NYC Schools",
       title="Density of Economic Need Index: NYC High Schools 2020-2021")
# Plot temp housing percentage vs college persistence rate
ggplot(train, aes(x=temp_housing_pct, y=college_rate)) +
 geom_point() +
 labs(x="% of Students in Temporary Housing",
       y="4-year College Persistence Rate")
# Plot ENI vs college persistence rate
ggplot(train, aes(x=economic need, y=college rate)) +
 geom_point() +
 labs(x="Average Economic Need Index per School",
       y="4-year College Persistence Rate")
base_formula <- college_rate ~ survey_pp_CT + survey_pp_RI + survey_pp_SE + survey_pp_ES
rating_model <- lm(base_formula,
                   train)
summary(rating_model)
```

```
# Create OLS linear model based on our proxy variables: no transforms
proxy_formula <- college_rate ~ temp_housing_pct + economic_need</pre>
proxy_model <- lm(proxy_formula, train)</pre>
summary(proxy_model)
plot(proxy_model)
# Calculating weights for WLS
weights <- 1 / lm(abs(proxy model$residuals) ~ proxy model$fitted.values)$fitted.values
#perform weighted least squares regression
wls model <- lm(proxy formula, data = train, weights=weights)</pre>
summary(wls_model)
# Compute RMSE for each model on our testing data
# TODO: Put in table with AIC and BIC results
rmse(rating model, test)
modelr::rmse(proxy model, test)
modelr::rmse(wls model, test)
# Print AIC for each model type
print(glue("AIC for base model (rating results): {AIC(rating model)}"))
print(glue("AIC for proxy variable model: {AIC(proxy_model)}"))
print(glue("AIC for WLS model: {AIC(wls_model)}"))
# BIC results
print(glue("BIC for base model (rating results): {BIC(rating model)}"))
print(glue("BIC for proxy variable model: {BIC(proxy model)}"))
print(glue("BIC for WLS model: {BIC(wls_model)}"))
```