# **Describing Motion: Kinematics in One Dimension**

# Displacement

"the change in x," or "change in position"

$$\Delta x = x_2 - x_1$$

The change

in any quantity means the final value of that quantity, minus the initial value.

# Average Speed

is defined as the total distance travelled along its path divided by the time it takes to travel this distance.

average speed =  $\frac{\text{total distance travelled}}{\text{time elapsed}}$ 

# Average Velocity

is defined in terms of displacement, rather than total distance travelled.

average velocity = 
$$\frac{\text{displacement}}{\text{time elapsed}} = \frac{\text{final position} - \text{initial position}}{\text{time elapsed}}$$

is defined as the displacement divided by the elapsed time

$$\bar{v} = \frac{x_2 - x_1}{t_2 - t_1} = \frac{\Delta x}{\Delta t}$$

### **Instantaneous Velocity**

Instantaneous velocity at any moment is defined as the average velocity over

is defined as the average velocity over an infinitesimally short time interval. 
$$v = \lim_{\Delta t \to 0} \frac{\Delta x}{\Delta t}$$

# **Average Acceleration**

is defined

as the change in velocity divided by the time taken to make this change.

average acceleration 
$$=$$
  $\frac{\text{change of velocity}}{\text{time elapsed}}$ 

$$\bar{a} = \frac{v_2 - v_1}{t_2 - t_1} = \frac{\Delta v}{\Delta t}$$

#### **Instantaneous Acceleration**

Instantaneous acceleration,

a, can be defined in analogy to instantaneous velocity as the average acceleration over an infinitesimally short time interval at a given instant.

$$a = \lim_{\Delta t \to 0} \frac{\Delta v}{\Delta t}$$

#### **Deceleration**

is whenever the magnitude of the velocity is decreasing. is when velocity and acceleration point in opposite directions.

#### **Motion at Constant Acceleration**

We now examine motion in a straight line when the magnitude of the acceleration is constant. In this case, the instantaneous and average accelerations are equal.

We use the definitions of average velocity and acceleration to derive a set of valuable equations that relate x, v, a, and t when a is constant, allowing us to determine any one of these variables if we know the others. We can then solve many interesting Problems.

First we choose the initial time in any discussion to be zero, and we call it  $t_0$ . That is,  $t_1 = t_0 = 0$ . (This is effectively starting a stopwatch at  $t_0$ .) We can then let  $t_2 = t$  be the elapsed time.

The initial position  $x_1$  and the initial velocity  $v_1$  of an object will now be represented by  $x_0$  and  $v_0$ , since they represent x and v at t=0. At time t the position and velocity will be called x and v (rather than  $x_2$  and  $v_2$ ). The average velocity during the time interval  $t-t_0$  will be

$$\bar{v} = \frac{\Delta x}{\Delta t} = \frac{x - x_0}{t - t_0} = \frac{x - x_0}{t}$$
since we chose  $t_0 = 0$ 

$$a = \frac{v - v_0}{t}$$

The velocity of an object after any elapsed time t  $v=v_0+at$  Calculating the Position x of an object after a time t  $\bar{v}=\frac{x-x_0}{t}$  becomes  $x=x_0+\bar{v}t$  Because the velocity increases at a uniform rate  $\bar{v}$  will be midway between the initial and final velocities  $\bar{v}=\frac{v_0+v}{2}$  Combining the last three equations these become  $x=x_0+\bar{v}t$   $x=x_0+(\frac{v_0+v}{2})t$ 

$$x = x_0 + (\frac{v_0 + (v_0 + at)}{2})t$$

$$x = x_0 + v_0 t + \frac{1}{2}at^2$$
Three of the four most useful equations for motion at constant acceleration

 $v = v_0 + at$ 

Average velocity  $\bar{v} = \frac{v_0 + v}{2}$ Position x of an object after a time t

$$x = x_0 + v_0 t + \frac{1}{2} a t^2$$

Situations where time *t* is not known  $v = v + (v_0 + v_1)t$ 

$$x = x_0 + \left(\frac{v_0 + v}{2}\right)t$$
solve for  $t = v_0 + at$ 

Substituting this into the previous equation we get

The velocity of an object after any elapsed time t

$$x = x_0 + (\frac{v_0 + v}{2})(\frac{v - v_0}{a}) = x_0 + \frac{v^2 - v_0^2}{2a}$$
solve for  $v^2$ 

$$v^2 = v_0^2 + 2a(x - x_0)$$
Kinematic equations for constant acceleration

[
$$a$$
=constant]  
 $v$ = $v_0$ + $at$   
 $x$ = $x_0$ + $v_0t$ + $\frac{1}{2}at^2$   
 $v^2$ = $v_0^2$ + $2a(x-x_0)$   
 $\bar{v}$ = $\frac{v+v_0}{2}$ 

# Solving Problems

- Read and reread the whole problem carefully before trying to solve it.
   Decide what object (or objects) you are going to study, and for what time
- interval. You can often choose the initial time to be t = 0.
- 3. Draw a diagram or picture of the situation, with coordinate axes wherever applicable. [You can place the origin of coordinates and the axes wherever you
- like to make your calculations easier. You also choose which direction is positive and which is negative. Usually we choose the x axis to the right as positive.]

  4. Write down what quantities are "known" or "given," and then what you
- want to know. Consider quantities both at the beginning and at the end of the chosen time interval. You may need to "translate" language into physical terms, such as "starts from rest" means v0 = 0.
- 5. Think about which principles of physics apply in this problem. Use common sense and your own experiences. Then plan an approach
- sense and your own experiences. Then plan an approach.

  6. Consider which equations (and/or definitions) relate the quantities involved.
- Before using them, be sure their range of validity includes your problem (for example, Eqs. 2–11 are valid only when the acceleration is constant). If you find an applicable equation that involves only known quantities and one desired unknown, solve the equation algebraically for the unknown. Sometimes several

sequential calculations, or a combination of equations, may be needed. It is often preferable to solve algebraically for the desired unknown before putting

- in numerical values. 7. Carry out the calculation if it is a numerical problem. Keep one or two extra digits during the calculations, but round off the final answer(s) to the correct
- number of significant figures (Section 1–4). 8. Think carefully about the result you obtain: Is it reasonable? Does it make
- sense according to your own intuition and experience? A good check is to do a rough estimate using only powers of 10, as discussed in Section 1–7. Often it is preferable to do a rough estimate at the start of a numerical problem because it can help you focus your attention on finding a path toward a solution.
- 9. A very important aspect of doing problems is keeping track of units. An equals sign implies the units on each side must be the same, just as the numbers must. If the units do not balance, a mistake has been made. This can serve as a check on your solution (but it only tells you if you're wrong, not if you're right). Always use a consistent set of units.

#### Freely Falling Objects

with upwards as positive solving for t

$$y = y_0 + v_0 t + \frac{1}{2} at$$

 $y=y_0+v_0t+\frac{1}{2}at^2$ We rewrite our y equation just above in standard form,

$$at^{2}+bt+c=0$$

$$0=(y_{0}-y)+v_{0}t+\frac{1}{2}at^{2}$$

$$\frac{1}{2}at^{2} + v_{0}t + (y_{0} - y) = 0$$

$$(\frac{1}{2}a)t^{2} + (v_{0})t + (y_{0} - y) = 0$$

Using the quadratic formula, we find as solutions

$$t = \frac{-b \pm \sqrt{b^2 - 4a}}{2a}$$

$$g = 9.80m/s^2$$

# Stuff about graphing

# Right angled triangles

$$\sin\theta = Opp/Hyp$$

$$\cos\theta = Adj/Hyp$$

$$\tan\theta = Opp/Adj$$

$$\csc\theta = Hyp/Opp = 1/\sin\theta$$

$$\sec\theta = Hyp/Adj = 1/\cos\theta$$

$$\cot\theta = Adj/Opp = 1/\tan\theta$$

# Resolving vectors $\mathbf{v}_r = r \cos \theta$

$$\mathbf{v}_y = r\sin\theta$$
  
 $r = |\mathbf{v}| = \sqrt{x^2 + y^2}$  (Magnitude)  
 $r = |\mathbf{v}| = \sqrt{x^2 + y^2 + z^2}$  (Magnitude for 3-space)  
 $\theta = \tan^{-1}(\frac{\mathbf{v}_y}{\mathbf{v}_x})$ 

$$\theta = \begin{array}{c|c} 180 - \theta & \theta \\ \hline 180 + \theta & 360 - \theta \end{array}$$

#### Kinematics in Two Dimensions; Vectors

# **Solving Projectile Motion Problems**

General Kinematic Equations for Constant Acceleration in Two Dimensions x component (horizontal) y component (vertical)

We can simplify Eqs to use for projectile motion because we can set  $a_x = 0$ ,  $a_y = -g$ 

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Kinematic Equations for Projectile Motion (y positive upward;  $a_x = 0$ ,  $a_y = -g = 9.80 m/s^2$ ) Horizontal Motion Vertical Motion  $(a_x = 0, v_x = \text{constant})$  $(a_v = -g = \text{constant})$  $v_r = v_{r0}$  $v_y = v_{y0} - gt$  $y = y_0 + v_{y0}t - \frac{1}{2}gt^2$  $x=x_0+v_{x0}t$ 

# **Projectile Motion Is Parabolic**

We now show that the path followed by any projectile is a parabola, if we can ignore air resistance and can assume that g is constant.

 $v_{y}^{2} = v_{y0}^{2} - 2g(y - y_{0})$ 

for simplicity we set  $x_0 = y_0 = 0$  $x = v_{x0}t$ 

$$y = v_{y0}t - \frac{1}{2}gt^2$$

From the first

equation, we have  $t = \frac{x}{y}$ , and we substitute this into the second one to obtain

$$y = v_{y0}(\frac{x}{v_{x0}}) - \frac{1}{2}g(\frac{x}{v_{x0}})^{2}$$
$$y = (\frac{v_{y0}}{v_{x0}})x - \frac{1}{2}g(\frac{x^{2}}{v_{x0}^{2}})$$

$$y = \left(\frac{v_{y0}}{v_{x0}}\right)x - \frac{1}{2}g\left(\frac{x^2}{v_{x0}^2}\right)$$
$$y = \left(\frac{v_{y0}}{v_{x0}}\right)x - \left(\frac{g}{2v_{x0}^2}\right)x^2$$

$$y = (\frac{1}{v_{x0}})x - (\frac{1}{2v_{x0}^2})x^2$$

We see that

y as a function of x has the form  $y=Ax-Bx^2$ , where A and B are constants for any specific projectile motion. This is the standard equation for a parabola.

# Relative Velocity

We now consider how observations made in different frames of reference are related to each other.

For example, consider two trains approaching one another, each with a speed of 80 kmh with respect to the Earth. Observers on the Earth beside the train

tracks will measure 80 kmh for the speed of each of the trains. Observers on either one of the trains (a different frame of reference) will measure a speed of 160 kmh for the train approaching them.

Similarly, when one car traveling 90 kmh passes a second car traveling in the

same direction at 75 kmh, the first car has a speed relative to the second car

Use a diagram and a careful labeling process. Each velocity is labeled by two subscripts: the first refers to the object, the second to the reference frame in

which it has this velocity.  $\vec{v}_{OR}$  Example, suppose a boat heads directly across a river let

 $\vec{v}_{BW}$  be the velocity of the Boat with respect to the Water.  $\vec{v}_{BS}$  be the velocity of the Boat with respect to the Shore,  $\vec{v}_{WS}$  be the velocity of the Water with respect to the Shore

of 90 kmh - 75 kmh = 15 kmh.

 $\vec{v}_{BS} = \vec{v}_{BW} + \vec{v}_{WS}$ By writing the subscripts using this convention, we see that the inner subscripts (the two W's) on the right-hand side of Eq. 3-7 are the same; also, the outer subscripts on the right of Eq. 3-7 (the B and the S) are the same as the two

(first subscript for the object, second for the reference frame), you can write down the correct equation relating velocities in different reference frames. Equation 3-7 is valid in general and can be extended to three or more velocities. example,

subscripts for the sum vector on the left, vBS. By following this convention

 $\vec{v}_{FB}$  is the velocity of the fisherman relative to the boat his velocity relative to the shore is  $\vec{v}_{FS} = \vec{v}_{FB} + \vec{v}_{BW} + \vec{v}_{WS}$ The equations involving relative velocity will be correct when there is no vector subtraction adjacent inner subscripts are identical

and when the outermost ones correspond exactly to the two on the velocity on the left of the equation. It is often useful to remember that for any two objects or reference frames,

•

A and B, the velocity of A relative to B has the same magnitude, but opposite direction, as the velocity of B relative to A:  $\vec{v}_{AB} = -\vec{v}_{BA}$ 

# Work and Energy

# Kinetic Energy, and the Work-Energy Principle

 $F_{net} = ma$ , we determine the work done:

To obtain a quantitative definition for kinetic energy, let us consider a simple rigid object of mass m (treated as a particle) that is moving in a straight line with an initial speed  $v_1$ . To accelerate it uniformly to a speed  $v_2$  a constant net force

 $F_{net}$  is exerted on it parallel to its motion over a displacement d, Fig. 6–7. Then the net work done on the object is  $W_{net} = F_{net}d$ . We apply Newton's second law,  $F_{net} = ma$  and use Eq. 2–11c  $(v_2^2 = v_1^2 + 2ad)$  which we rewrite as  $a = \frac{v_2^2 - v_1^2}{2d}$ where  $v_1$  is the initial speed and  $v_2$  is the final speed. Substituting this into

$$W_{net} = F_{net}d = mad = m(\frac{v_2^2 - v_1^2}{2d})d = m(\frac{v_2^2 - v_1^2}{2})$$
or
$$W_{net} = \frac{1}{2}mv_2^2 - \frac{1}{2}mv_1^2$$

 $W_{net} = KE_2 - KE_1$ 

We define the quantity to be the translational kinetic energy (KE) of the object:  

$$KE = \frac{1}{2}mv^2$$

work-energy principle

$$W_{net} = \Delta KE = \frac{1}{2}mv_2^2 - \frac{1}{2}mv_1^2$$
It can be stated in words:

The net work done on an object is equal to the change in the object's kinetic energy.

Thus, the work-energy principle is valid only if W is the net work done on the object—that is, the work done by all forces acting on the object.

# Potential Energy Defined in General

In general, the change in potential energy associated with a particular force is equal to the negative of the work done by that force when the object is moved from one point to a second point (as in Eq. 6–7b for gravity). Alternatively, we can define the change in potential energy as the work required of an external

force to move the object without acceleration between the two points FS = -kx. where k is a constant, called the spring stiffness constant (or simply spring

constant), and is a measure of the stiffness of the particular spring. spring either stretched or compressed an amount x from its natural (unstretched) length spring equation and also as Hooke's law, and is accurate for springs as long as x is not too great.

# elastic potential energy Phys1006 formula sheet

DATA	
Avogadro's number	$N_A = 6.02 \times 10^{23} \text{mol}^{-1}$
Planck's constant	$h=6.626\times10^{-34}$ Js
Stephan-Boltzmann's constant	$\sigma = 5.67 \times 10^{-8} \text{Wm}^{-2} \text{K}^{-4}$
Boltzmann's constant	$k_B = 1.38 \times 10^{-23} JK^{-1}$
Gravitational constant	$G = 6.67 \times 10^{-11} \text{N} \cdot \text{m}^2 \cdot \text{kg}^{-2}$
Radius of the Earth	$R_{\rm E} = 6.38 \times 10^6 \text{m}$
Mass of the Earth	$M_{\rm E} = 5.98 \times 10^{24} \rm kg$
Gas constant	R=8.314J/mol.K
Permittivity of free space	$\varepsilon_{\rm o} = 8.85 \times 10^{-12} \text{C}^2/\text{N} \cdot \text{m}^2$
Permeability of free space	$\mu$ o= $4\pi \times 10^{-7}$ T.m/A
Coulomb constant	$k=9.0\times10^{9} \text{Nm}^{2}/\text{C}^{2}$

freezing point of water	$=0^{\circ}C = 32^{\circ}F$
boiling point of water	$=100^{\circ}C=212^{\circ}F$
specific heat of water	$c_{\text{water}} = 4186 \text{Jkg}^{-1} \text{C}^{\circ -1}$
specific heat of ice	$c_{ice} = 2100 Jkg^{-1} C^{\circ -1}$
specific heat of iron	$c_{iron} = 450 Jkg^{-1} C^{\circ -1}$
specific heat of copper	$c_{cu} = 390 \text{Jkg}^{-1} \text{C}^{\circ -1}$
specific heat of aluminum	$c_{Al} = 900 \text{Jkg}^{-1} \text{C}^{\circ -1}$
latent heat of vaporization of water	$=2.26\times10^{6}$ Jkg <sup>-1</sup>
latent heat of fusion of ice	$=3.33\times10^{5}$ Jkg <sup>-1</sup>
coefficient of volume expansion of petrol	$=950\times10^{-6}\text{C}^{\circ-1}$
coefficient of linear expansion of steel/iron	$=12\times10^{-6}\text{C}^{\circ-1}$
coefficient of linear expansion of brass	$=19\times10^{-6}\text{C}^{\circ-1}$
charge on an electron	$=1.6\times10^{-19}$ C
leV lev	$=1.6\times10^{-19}$ J
FORMULA SHEET	
MODULE 1: FUNDAMENTALS	

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acceleration due to gravity index of refraction of air (STP)

speed of light (in vacuum)

speed of sound (at  $0^{\circ}$ C)

Pi

Volume

density of water

atmospheric pressure volume of air at STP

coefficient of thermal conductivity for brick

coefficient of thermal conductivity for glass

density of air

zero Kelvin

 $g = 9.80 \text{ms}^{-2}$ 

n = 1.0003 $c = 3 \times 10^8 \text{ms}^{-1}$ 

 $v = 331 \text{ms}^{-1}$ 

 $\rho = 1000 \text{kgm}^{-3}$ 

 $=1.29 \text{kgm}^{-3}$ 

 $=0.84 \text{Jm}^{-1} \text{s}^{-1} \text{K}^{-1}$ 

 $=0.84 \text{Jm}^{-1} \text{s}^{-1} \text{K}^{-1}$ 

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 $1atm = 1.013 \times 10^5 Pa$ 

 $=-273^{\circ}C$  $=0^{\circ}C = 32^{\circ}F$  $=100^{\circ}C = 212^{\circ}F$ 

=22.41.

 $\pi = 3.1416$  $11itre = 1000cm^{3}$ 

$$\cos\theta = \frac{\text{adjacent}}{\text{hypotenuse}}$$

$$\tan\theta = \frac{\text{opposite}}{\text{adjacent}}$$
Area of a circle =  $\pi r^2$ 
Circumference of a circle =  $2\pi r$ 
Surface area of a sphere =  $4\pi r^2$ 
Volume of a sphere =  $\frac{4}{3}\pi r^3$ 
Volume of a cylinder =  $\pi r^2 h$ 
Density  $(\rho) = \frac{\text{mass}(m)}{\text{volume}(V)}$ 

$$v_{\text{average}} = \frac{v_i + v_f}{2}$$
 $(x_f - x_i) = \text{displacement/distance}$ 

$$v_f = v_i + at$$

$$v_f^2 = v_i^2 + 2a(x_f - x_i)$$

$$(x_f - x_i) = v_i t + \frac{1}{2}at^2$$

$$R = \frac{v_i^2 \sin 2\theta}{g}, t = \frac{v \sin \theta}{g}$$

$$F = ma$$

$$F = ma$$

$$F_{\text{friction}} = \mu N \quad W = mg \quad N = mg \cos\theta$$

$$\mu_S = \tan\theta_c \quad F_x = F \cos\theta, \quad F_y = F \sin\theta, F = \sqrt{(F_x)^2 + (F_y)^2}, \tan\theta = \frac{F_y}{F_x}$$
Work Done =  $F = \frac{1}{2}mv^2$ 
Potential Energy =  $F = \frac{1}{2}mv^2$ 

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 $\sin\theta = \frac{\text{opposite}}{\text{hypotenuse}}$ 

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 $P = \frac{\text{Work}}{\text{time}} = \frac{W}{t} = Fv$ Normal force in an elevator N=mg±ma

# **Propagation of Uncertainties**

For Additions or Subtractions of measured values C = A + B AC = AA + AB

For Multiplications and Divisions of measured values

$$x = \frac{k^a t^b}{m^c n^d} \quad \frac{\Delta x}{x} = a \frac{\Delta k}{k} + b \frac{\Delta t}{t} + c \frac{\Delta m}{m} + d \frac{\Delta n}{n}$$

# MODULE 2:

Data

 $=1.6\times10^{-19}$ C Charge on electron  $=9.11\times10^{-31}$ kg Mass of electron

Charge on proton

 $=1.6\times10^{-19}$ C  $=1.67\times10^{-27}$ kg Mass of proton

 $k=9.0\times10^{9}N.m^{2}/C^{2}$ Coulomb constant  $=1.6\times10^{-19}$  I 1eV

 $\varepsilon O = 8.85 \times 10^{-12} C^2 / N.m^2$ Permittivity of free space  $\mu_0 = 4\pi \times 10^{-7} \text{T.m/A}$ Permeability of free space  $\rho = 100 \times 10^{-8} \Omega.m$ 

Resistivity of nichrome,  $\rho = 1.68 \times 10^{-8} \Omega.m$ Resistivity of copper,  $c = 3 \times 10^8 \text{ms}^{-1}$ speed of light (in vacuum)

Formula Sheet  $F = \frac{kq_1q_2}{r^2}$   $E_{\text{isolated charge}} = \frac{F}{q} = \frac{kq_1}{r^2}$   $V = \text{Ed}(\text{ uniform } \mathbf{E})$ 

V = IR  $R = \frac{\rho L}{\Lambda} \quad I = Q/t$ 

V=IR 
$$R = \frac{\rho L}{A}$$
  $I = Q/t$ 

V=IR  $V = qV$   $P = VI = C = \frac{\varepsilon_0 A}{d} = \frac{k\varepsilon_0 A}{d}$   $Q = CV$   $U = \frac{1}{2}CV$ 
 $R_{\text{series}} = \sum_{i} R_i = R + R_2 + R_3$   $\frac{1}{R_{\text{parallel}}} = \sum_{i} \frac{1}{R_i} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$ 
 $P = VI = I^2 R = \frac{V^2}{R}$   $R_T = R_0(1 + \alpha \Delta T)$ 
 $P_{\text{max}} = I_0 V_0$   $P_{\text{average}} = I_{\text{rms}} V_{\text{rms}} = I_0 V_0 / 2$ 
 $F = qv \text{Bsin}\theta$   $F = IIB \sin \theta$ 
 $F = qv \text{Bsin}\theta$   $F = IIB \sin \theta$ 
 $F = qv \text{Bsin}\theta$   $F = IIB \sin \theta$ 
 $F = \frac{\mu_0 I}{2\pi r}$   $\frac{V_S}{V_P} = \frac{N_S}{N_P} = \frac{I_P}{I_S}$ 

MODULE 3: WAVES and SOUND Also see Fundamental Principles formulae

 $F = kx$  [spring]

 $PE = 1/2kx^2$  [spring]

 $E = 1/2mv^2$ 

Total  $E = KE + PE$ 
 $E = 1/2mv^2$ 

Total  $E = KE + PE$ 
 $E = 1/2mv^2$ 

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 $E = 1/2mv^2$ 

Total  $E = KE + PE$ 

Speed of wave in a solid, 
$$v = \sqrt{\frac{E}{\rho}}$$

Speed of wave in a liquid/gas,  $v = \sqrt{\frac{B}{\rho}}$ 

Harmonics: strings/open pipes,  $f_n = n\left(\frac{v}{2L}\right)$  Closed pipes,  $f_n = n\left(\frac{v}{4L}\right)$ 

Law of reflection,  $\theta_i = \theta_r$ 

Law of refraction,  $v_1 \sin \theta_1 = v_2 \sin \theta_2$ 

Intensity level  $\beta(dB) = 10\log\left(\frac{I}{I_0}\right)$ 

where  $I_0 = 1.0 \times 10^{-12} W/m^2$ 
 $\beta_2 - \beta_1 = \Delta \beta = \log\left(\frac{I_2}{I_1}\right)$  I = Power  $/4\pi r^2$ 

MODULE 4: THERMAL PHYSICS

 $T(^oC) = \frac{5}{9}[T(F) - 32]$ 
 $\Delta L = \alpha L_o \Delta T$  linear thermal expansion ]

 $\Delta V = \beta V_o \Delta T$  [volume thermal expansion ]

 $Q = mc\Delta T$ [Specific heat]

 $Q = mL$ [Latent heat]

Rate of heat flow by conduction  $\frac{\Delta Q}{\Delta t} = kA\frac{\Delta T}{L}$ 

Thermal insulation  $R = \frac{L}{k}$ 

Net flow rate of heat radiation  $P = \sigma Ae(T_{body}^4 - T_{environment}^4)$ 

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 $\mathbf{v} = \sqrt{\frac{\mathbf{k}}{m}(A^2 - x^2)}$   $a_{\text{max}} = \boldsymbol{\omega}^2 A$ 

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Speed of wave in a string/wire,  $V = \sqrt{\frac{F_T}{m/L}}$ 

Brewster's Law 
$$\tan \theta_p = n_2/n_1$$
  
Malus' Law: : : : : Lawlus' Law:: : : :  $I = (1/2)I_0 \cos^2 \theta$   
MODULE 6: NUCLEAR RADIATION

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 $\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2}$   $PV = nRT \quad \text{(Ideal gas law)}$ 

 $PV = Nk_BT$   $\left(k_B = \frac{R}{N_A}\right)$ 

(Average KE of a molecule)

MODULE 5: OPTICS

 $\overline{\text{KE}} = \frac{3}{2} k_B T$ 

 $P = \frac{1}{f(m)}$ 

 $N = nN_A$  (N = number of molcules in a gas smaple)

Index of refraction n = c/v Snell's Law,  $n_1 \sin \theta_1 = n_2 \sin \theta_2$ 

Mirror/Lens formula  $(1/f) = (1/d_0) + (1/d_i)$ Magnification  $M = -(d_i/d_0) = (-h_i/h_0)$ 

Lens makers' formula  $(1/f) = (n-1)(1/R_1+1/R_2)$ 

Magnifying glass  $M_{\text{infinity}} = N/f$   $M_N = 1 + N/f$ 

Rayleigh criterion for resolution  $\theta_{\text{min}} = 1.22 \lambda / D$ Resolving power of a microscope  $S = f(1.22 \lambda / D)$ 

Microscope  $M = M_O M_e = (N \times L) / f_O f_e$ 

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 $v_{rms} = \sqrt{\frac{3k_BT}{m}} (rms \text{ speed of moecule})$  where m is the mass of a molecule

Binding Energy =  $(Zm_p + Nm_n - M_A) \times 931.5 \text{MeV}/u$ Absorbed dose: 1Gy = 1J/kg dose = dose rate x time Equivalent dose = absorbed dose x w R Effective dose = Equivalent dose x wr  $kg^- \cdot m^- \cdot s^{-2} \cdot A^-$ Named units derived from SI base units

 $N = N_0 \exp(-\lambda t)$  (number of atoms)  $A = \lambda N$  (activity)

charge on an electron

mass of hydrogen atom

 $P = \sigma A e T^{4} \quad \lambda_{MAX} T = 2.89 \times 10^{-3} \text{mK}$   $h f = W_{0} + K E_{MAX} \quad K E_{MAX} = e V_{\text{STOPPING}}$   $E_{n} = \frac{-13.6}{n^{2}} e V \quad E = 13.6 \left(\frac{1}{n_{x}^{2}} - \frac{1}{n_{z}^{2}}\right) e V$ 

 $A = A_0 \exp(-\lambda t) \quad T_{1/2} = \frac{\ln(2)}{2}$ 

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mass of neutron

mass of <sup>4</sup>He atom

atomic mass unit

mass of electron

mass of proton  $f\lambda = c$  E = hf

1eV

 $=1.6\times10^{-19}$ C

 $=1.6 \times 10^{-19}$  I

=1.008665u

=1.007825u

=4.002602u

 $=9.11\times10^{-31}$ kg

 $=1.67 \times 10^{-27} \text{kg}$ 

 $1u = 1.66 \times 10^{-27} \text{kg}, = 931.5 \text{MeV/c}^2$ 

hertz	Hz	frequency	1/s	$s^{-1}$
radian		angle	m/m	1
steradian	sr	solid angle	m2/m2	1
newton	N	force, weight	kgm/s2	kg·m·s <sup>-2</sup>
pascal	Pa	pressure, stress	N/m2	$kg \cdot m^{-1} \cdot s^{-2}$
joule	J	energy, work, heat	mN, CV, Ws	$kg \cdot m^2 \cdot s^{-2}$
watt	W	power, radiant flux	J/s, VA	$kg \cdot m^2 \cdot s^{-3}$
coulomb		electric charge or quantity of electricity	sA, FV	s·A
volt		voltage, electrical potential difference, electromotive force	W/A, J/C	$kg \cdot m^2 \cdot s^{-3} \cdot A^{-1}$
farad		electrical capaci- tance		$kg^{-1} \cdot m^{-2} \cdot s^4 \cdot A^2$
ohm		electrical resis- tance, impedance, reactance	1/S, V/A	$kg \cdot m^2 \cdot s^{-3} \cdot A^{-2}$
siemens	S	electrical conduc- tance	1/, A/V	$kg^{-1} \cdot m^{-2} \cdot s^3 \cdot A^2$
weber	Wb	magnetic flux	J/A, Tm2,Vs	$kg \cdot m^2 \cdot s^{-2} \cdot A^{-1}$
tesla		magnetic induction, magnetic flux density		$kg \cdot s^{-2} \cdot A^{-1}$
henry		electrical inductance	Vs/A, s, Wb/A	$kg \cdot m^2 \cdot s^{-2} \cdot A^{-2}$
degree Celsius		temperature relative to 273.15 K	K	K
lumen	lm	luminous flux	cdsr	cd
lux	1x	illuminance	lm/m2	cd⋅m <sup>-2</sup>
becquerel		radioactivity (decays	1/s	$s^{-1}$
		per unit time)		
gray		absorbed dose (of		$m^2 \cdot s^{-2}$
PHYS1006°Fc	und	ionizing radiation) ations of Physics equivalent dose (of	Page 18	
sievert	Sv	equivalent dose (of	J/kg	$\mathrm{m}^2\cdot\mathrm{s}^{-2}$

# Kinematic SI derived units

metre per second	m/s	speed, velocity	$m \cdot s^{-1}$
metre per second squared	m/s2	acceleration	$m \cdot s^{-2}$
metre per second cubed	m/s3	jerk, jolt	$m \cdot s^{-3}$
metre per second to the fourth	m/s4	snap, jounce	$m \cdot s^{-4}$
radian per second	rad/s	angular velocity	$s^{-1}$
radian per second squared	rad/s2	angular acceleration	$s^{-2}$
hertz per second	Hz/s	frequency drift	$s^{-2}$
cubic metre per second	m3/s	volumetric flow	$m^3 \cdot s^{-1}$

# Mechanical SI derived units

square metre	m2	area	m2
cubic metre	m3	volume	m3
newton second	Ns	momentum, impulse	mkgs1
newton metre second	Nms	angular momentum	m2kgs1
newton metre	Nm = J/rad	torque, moment of force	m2kgs2
newton per second	N/s	yank	mkgs3
reciprocal metre	m1	wavenumber, optical power	m1
		curvature, spatial frequency	
kilogram per square metre	kg/m2	area density	m2kg
kilogram per cubic metre	kg/m3	density, mass density	m3kg
cubic metre per kilogram	m3/kg	specific volume	m3kg1
joule second	Js	action	m2kgs1
joule per kilogram	J/kg	specific energy	m2s2
joule per cubic metre	J/m3	energy density	m1kgs2
newton per metre	N/m = J/m2	surface tension, stiffness	kgs2
watt per square metre	W/m2	heat flux density, irradiance	
square metre per second	m2/s	kinematic viscosity, ther	
		mal diffusivity, diffusion	L
		coefficient	
		dynamic viscosity	m1kgs1
kilogram per metre	kg/m	linear mass density	m1kg
kilogram per second	kg/s	mass flow rate	kgs1
watt per steradian square	W/(srm2)	radiance	kgs3
metre			
watt per steradian cubic	W/(srm3)	spectral radiance	m1kgs3
metre	VVV/		1 2
watt per metre	W/m	spectral power	mkgs3
gray per second	Gy/s	absorbed dose rate	m2s3
metre per cubic metre	m/m3	fuel efficiency	m2
watt per cubic metre	W/m3	spectral irradiance, power	mlkgs3
	T// 2	density	1 2
joule per square metre	J/(m2s)	energy flux density	kgs3
second	D 1	21.21	1 1 6
reciprocal pascal PHYS1006 Foundations of Joule per square metre	Pal	compressibility	mkg1s2
Joule per square metrens of	J7fff2	radialle exposure	kgs2
kilogram squara matra	kam2	moment of inartic	malka

### Molar SI derived units

mole per cubic metre	mol/m3	molarity, amount of	m3mol
		substance concentration	
cubic metre per mole	m3/mol	molar volume	m3mol1
joule per kelvin mole	J/(Kmol)	molar heat capacity	m2kgs2K1mol1
		molar entropy	
joule per mole	J/mol	molar energy	m2kgs2mol1
siemens square metre per	Sm2/mol	molar conductivity	kg1s3A2mol1
mole			
mole per kilogram	mol/kg	molality	kg1mol
kilogram per mole	kg/mol	molar mass	kgmol1
cubic metre per mole	m3/(mols)	catalytic efficiency	m3s1mol1
second			

# Electromagnetic SI derived units

ampere per square metre	A/m <sup>2</sup>	electric current density	m2A		
siemens per metre	S/m	electrical conductivity	m3kg1s3A2		
farad per metre	F/m	permittivity	m3kg1s4A2		
henry per metre	H/m	magnetic permeability	mkgs2A2		
volt per metre	V/m		mkgs3A1		
ampere per metre	A/m	magnetization, magnetic	m1A		
		field strength			
coulomb per kilogram	C/kg	exposure (X and gamma	kg1sA		
		rays)			
ohm metre	m		m3kgs3A2		
coulomb per metre	C/m		m1sA		
joule per tesla	J/T	magnetic dipole moment	m2A		
square metre per volt secondm2/(Vs)electron mobility kg1s2A					
reciprocal henry	H1	magnetic reluctance	m2kg1s2A2		
weber per metre	Wb/m	magnetic vector potential	mkgs2A1		
weber metre	Wbm	magnetic moment	m3kgs2A1		
tesla metre	Tm		mkgs2A1		
ampere radian	Arad	magnetomotive force	A		
metre per henry	m/H	magnetic susceptibility	m1kg1s2A2		
Photometric SI derived units					
lumen second		luminous energy	scd		
lux second		luminous exposure	m2scd		
candela per square metre		luminance	m2cd		
lumen per watt	lm/W	luminous efficacy	m2kg1s3cd		

C/m2 electric displacement field m2sA polarization density

m3sA

C/m3 electric charge density

coulomb per square metre

coulomb per cubic metre

### Thermodynamic SI derived units

joule per kelvin	J/K	heat capacity, entropy	m2kgs2K1
joule per kilogram kelvin		specific heat capacity,	m2s2K1
		specific entropy	
watt per metre kelvin	W/(mK)	thermal conductivity	mkgs3K1
kelvin per watt	K/W	thermal resistance	m2kg1s3K
reciprocal kelvin	K1	thermal expansion coefficient	K1
kelvin per metre	K/m	temperature gradient	m1K

# **Newton's Laws of Motion**

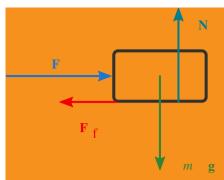
#### First law

An object at rest remains at rest unless a net force acts on it.

An object moving with constant velocity continues to move with same speed

and in the same direction unless a net force acts on it.

What is a Free-body diagram? Or Force diagram A diagram that shows all the forces acting On the object only and not by the object. To draw FBD -Represent the object of interest as a dot on the origin of a co-ordinate system. Isolate the object and draw all the forces acting on the object. Find the resultant force acting on the object and apply Newton's law. https://www.phyley.com/freebody-diagram



force is in newtons

$$\Sigma F = N - W = 0$$
  
$$\Sigma F = N - ma = N - mg = 0$$

sum of all forces = normal force - weight = 0

#### Second Law

When a net force acts on an object, it experiences acceleration.

$$\Sigma F = ma \Rightarrow a = \frac{\Sigma F}{m}$$

A 50 kg crate is being pulled with a constant force of 200N on a frictionless surface. Find its acceleration.

$$\Sigma F_x = ma_x \quad \Sigma F_y = ma_y$$
$$200 = 50a \quad N - (50 \times 9.8) = 0$$

$$200 = 50a \quad N - (50 \times 9.8) = 0$$

 $a = 4m/s^2$  N = 490N

Exercise. What force is needed to stop a 1000 kg car in 6 s if it is traveling at 90 km/h? (Assume constant acceleration)

$$v=90 \times 10^3 m_{\overline{60 \times 60 = 25 \text{m/s}}}$$

#### Third Law

Whenever one body exerts a force on a second body, the second body exerts an equal and opposite force on the first body.

These are called Action-Reaction forces.

Note: Action and Reaction Forces act on different objects.

#### Latex tools

https://www.tablesgenerator.com/latex\_tables http://w2.syronex.com/jmr/latex-symbols-converter