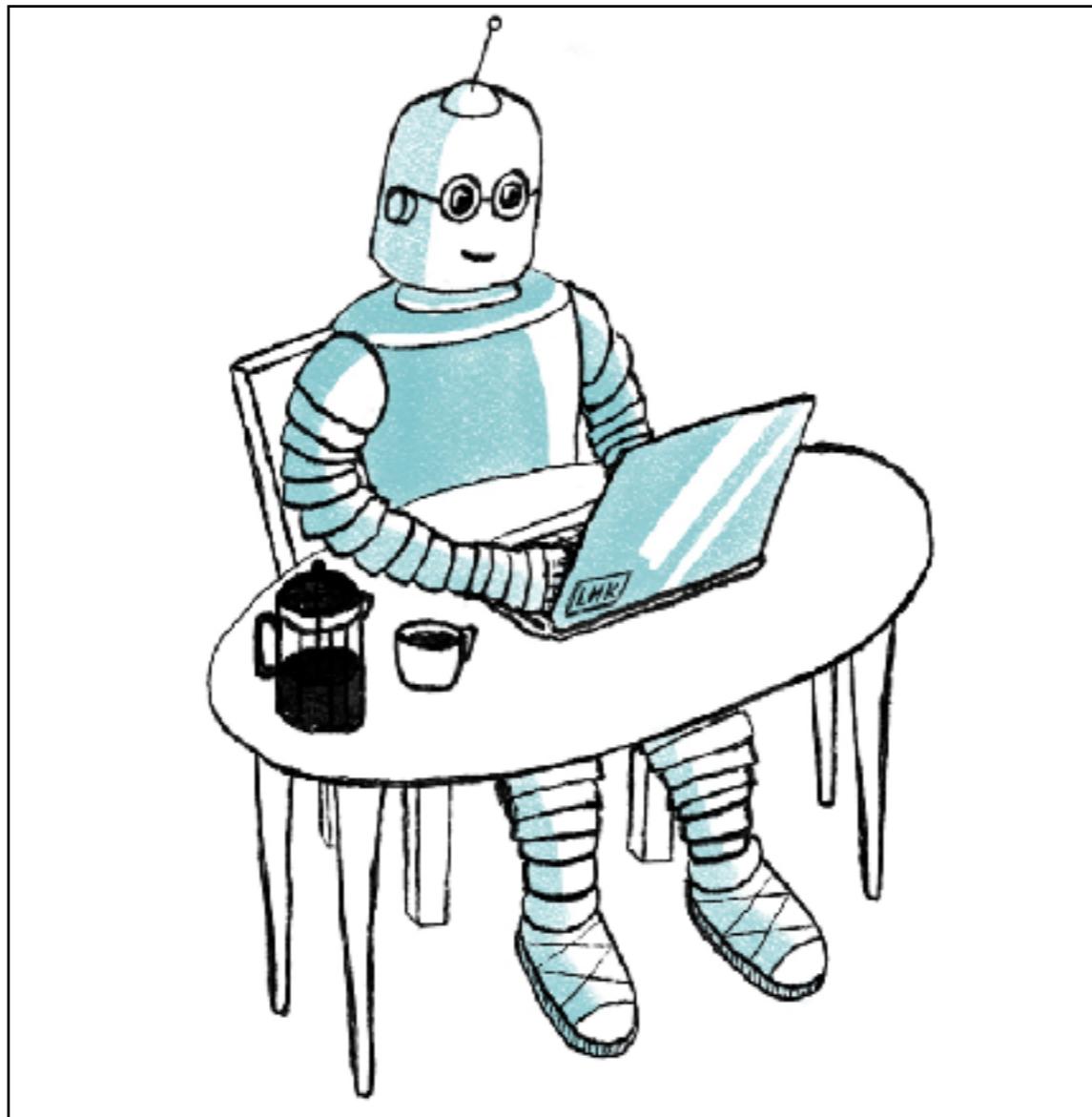


# Logical scientific discovery



Andrew Cropper

# **My long-term goal**

**Accelerate scientific discovery**

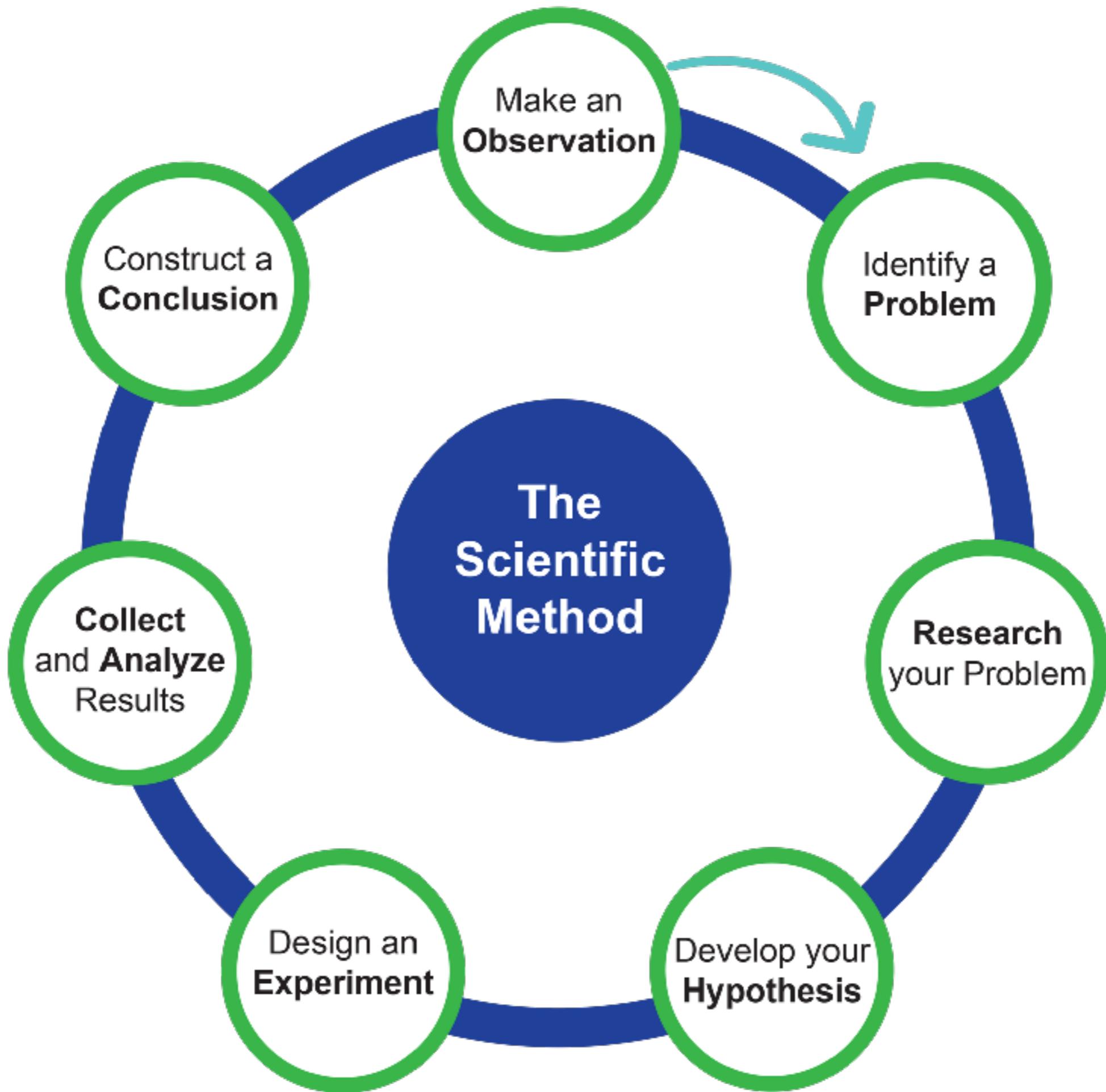
# Why?

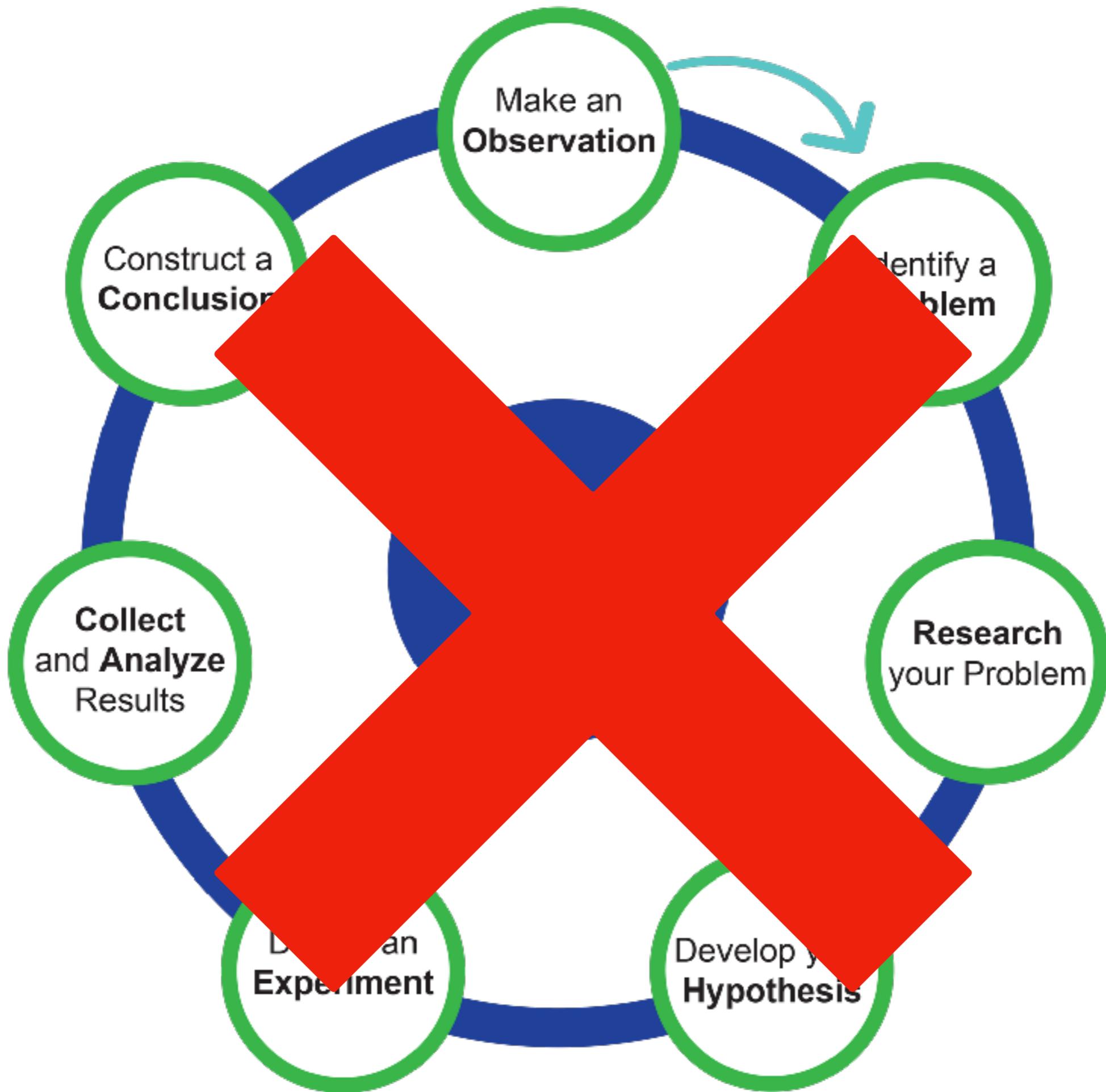
Science is important

# Antibiotics



What exactly do I want to do?



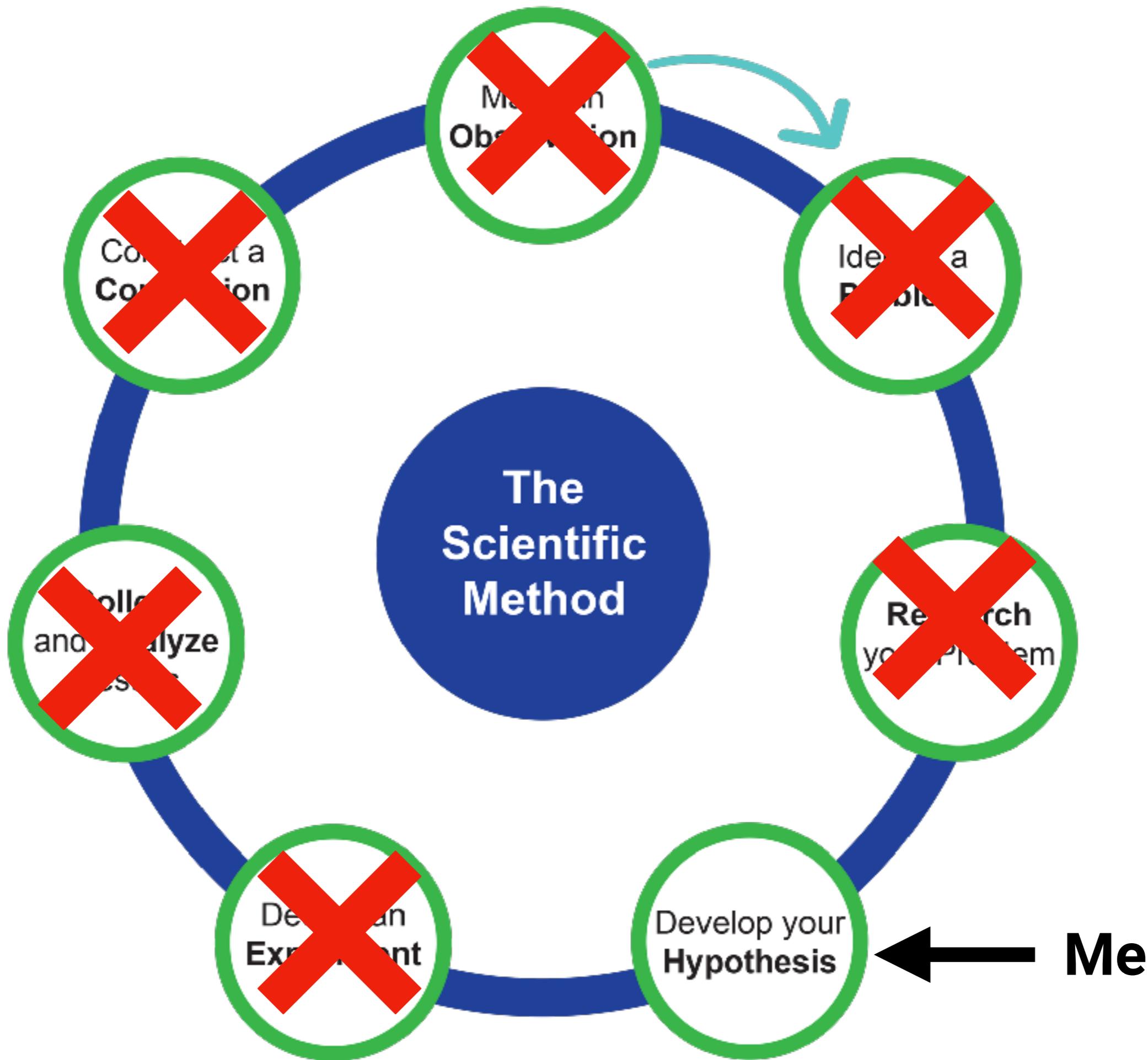


# Robot scientist



# Robot scientist





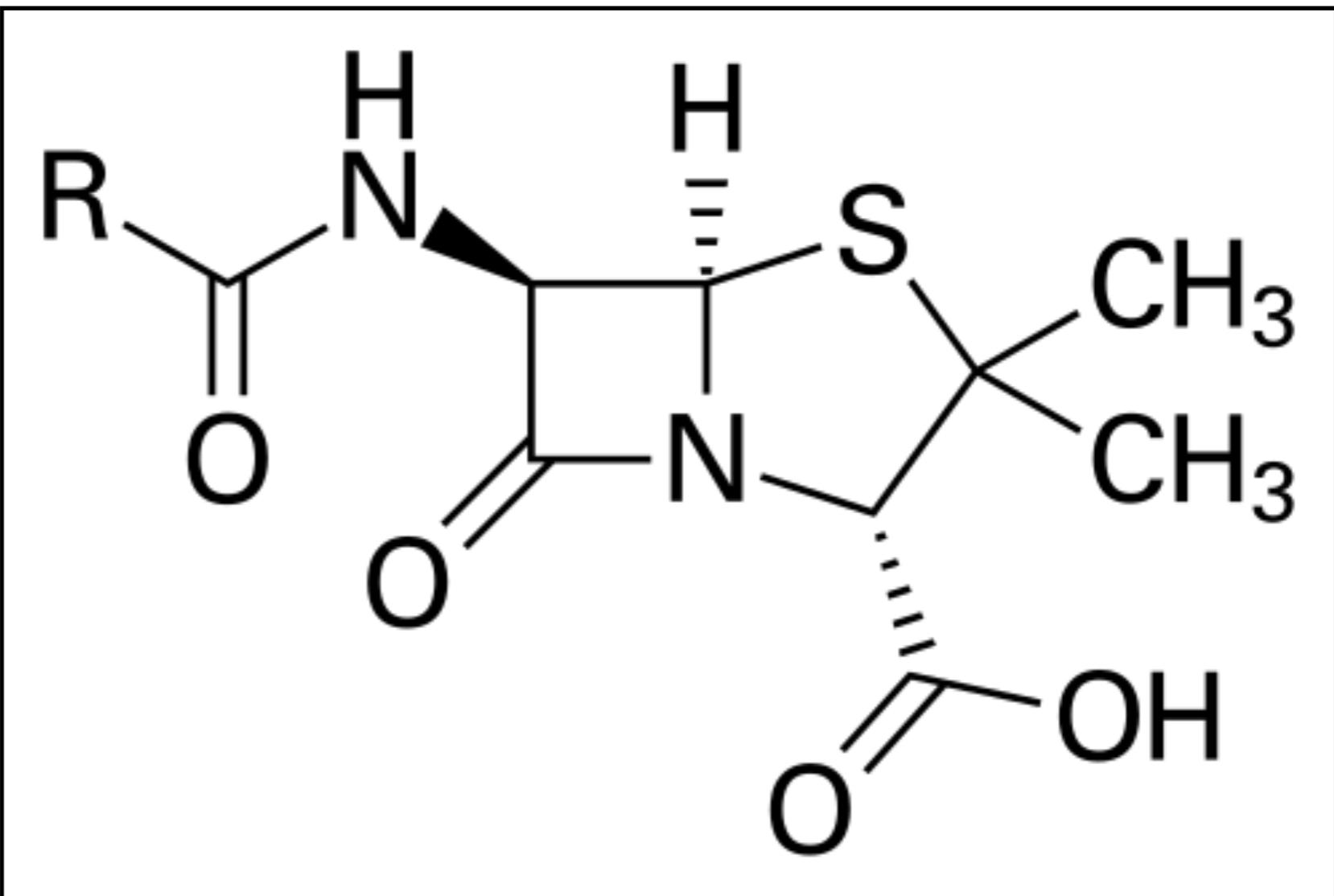
# **My research**

# My research

Prior  
knowledge

# My research

Prior  
knowledge



# My research

Observations

# My research



Observations

# My research

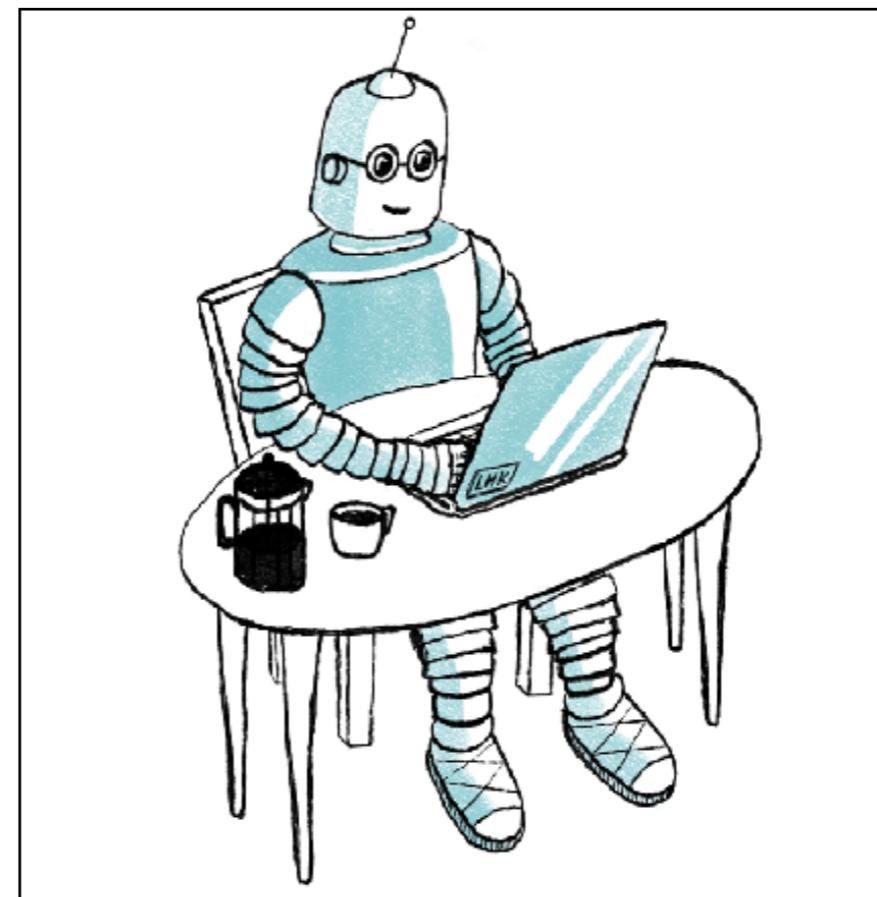
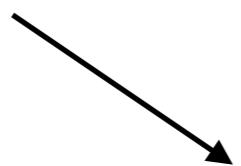
Prior  
knowledge

Observations

# My research

Prior  
knowledge

Observations

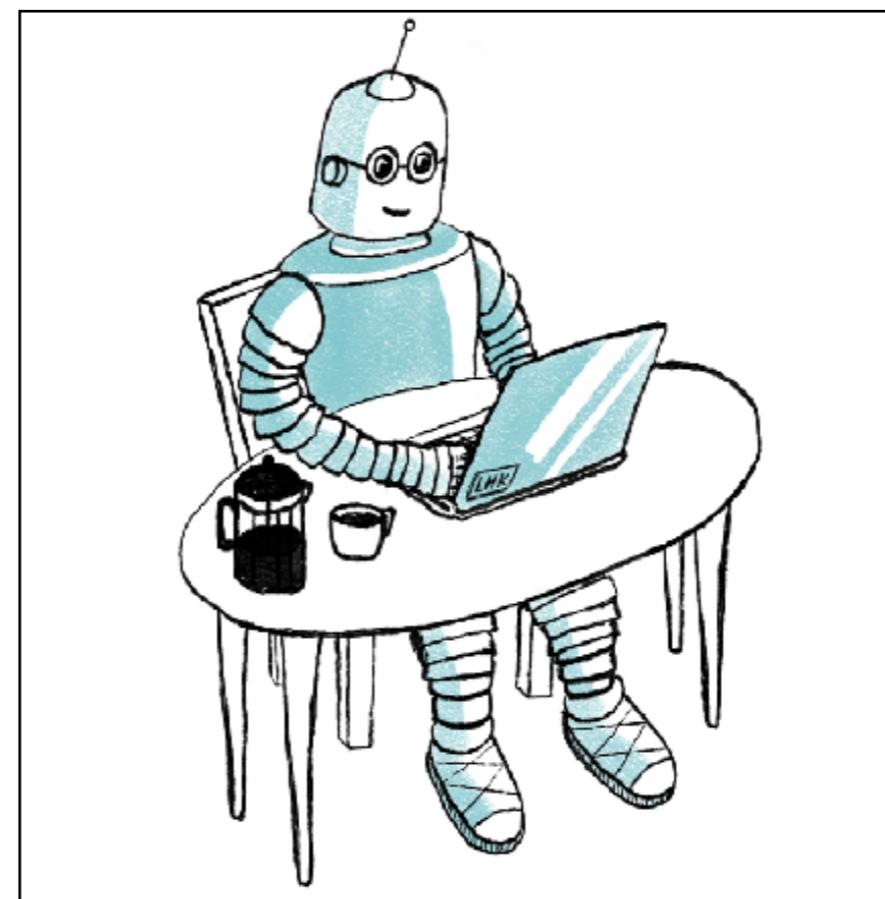


# My research

Prior  
knowledge

Observations

Hypothesis

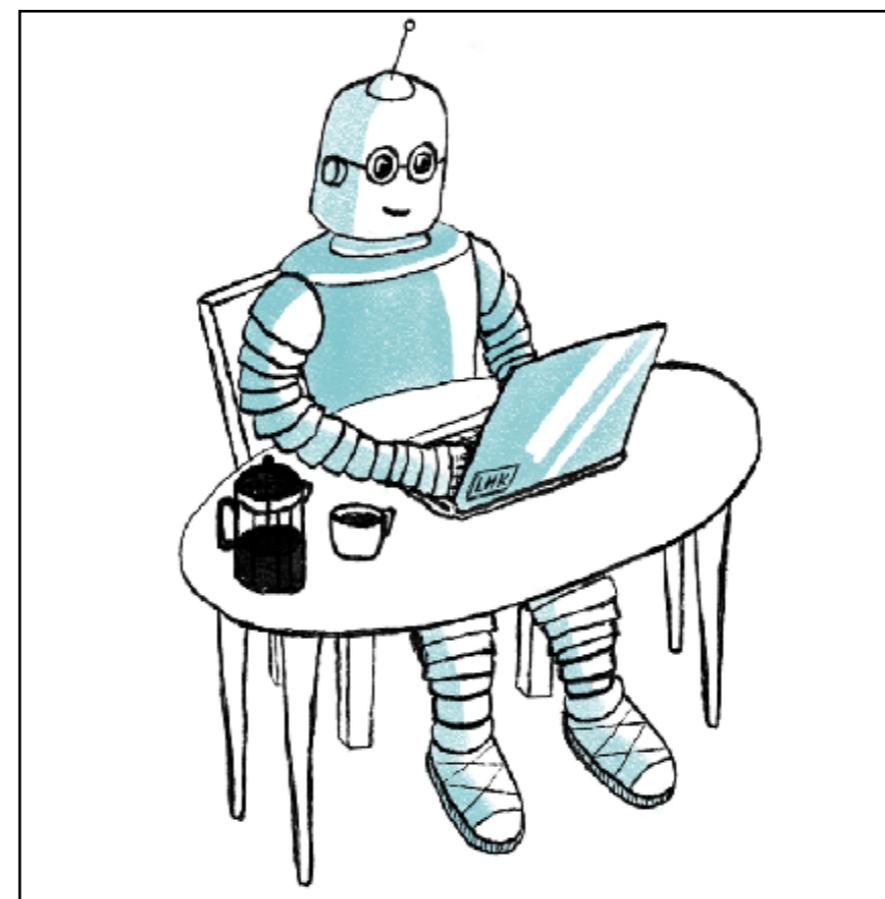


# My research

Prior  
knowledge

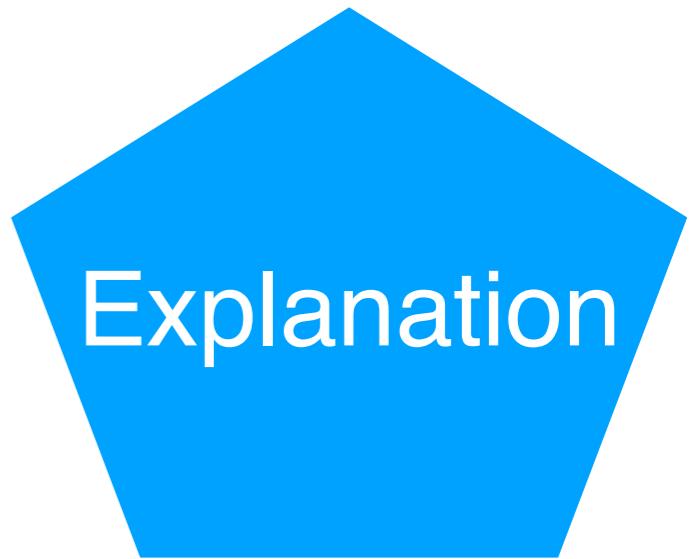
Observations

Explanation



# My research

A drug works if it has both a hydroxyl group and an amine group and the oxygen atom of the hydroxyl group is connected to the nitrogen atom of the amine group



Explanation

What do we need?

# Efficiency

**MasterControl**

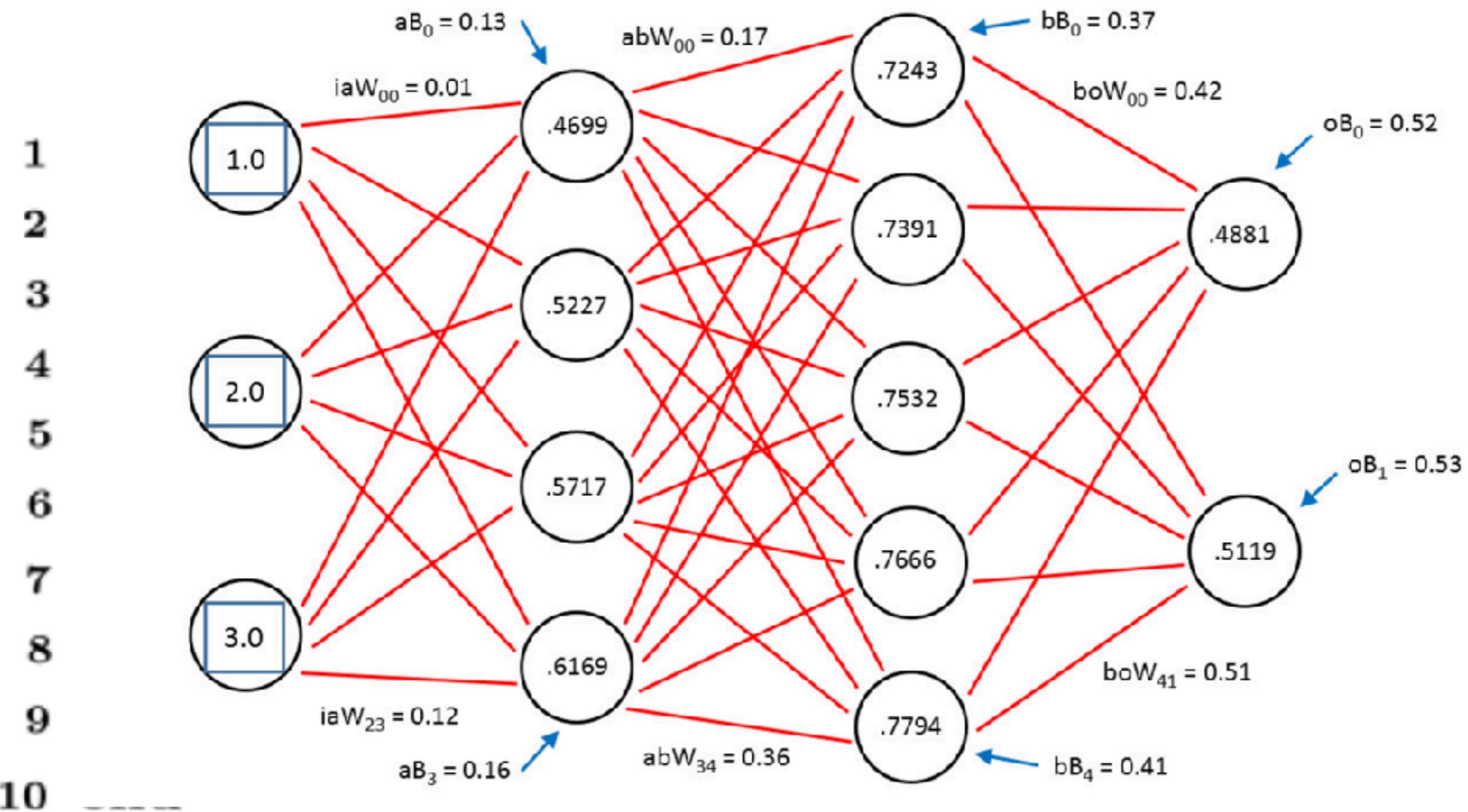


# Explainability

To publish a discovery, we must **explain** it

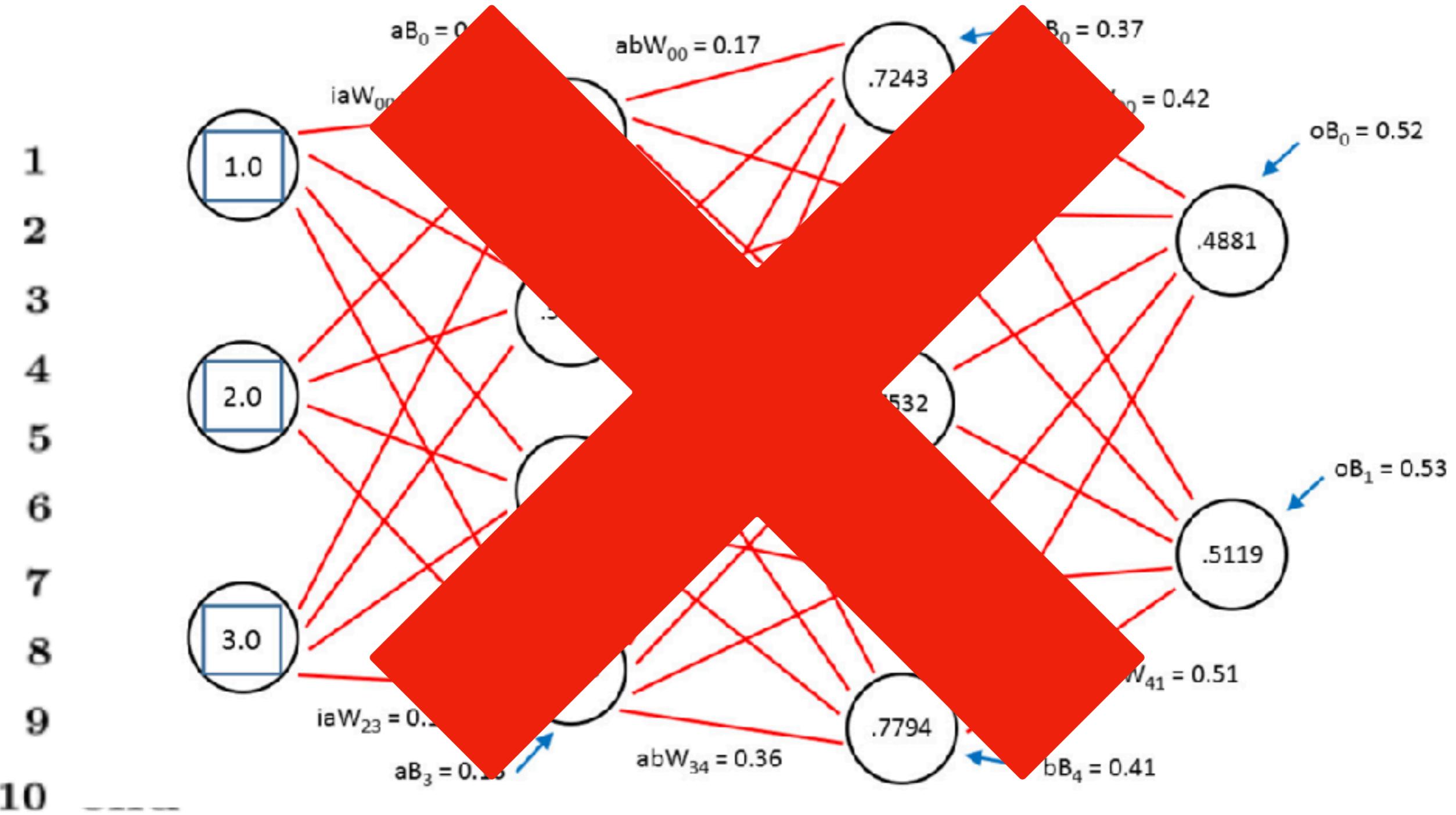
# Explainability

## Algorithm 1: How to write algorithms



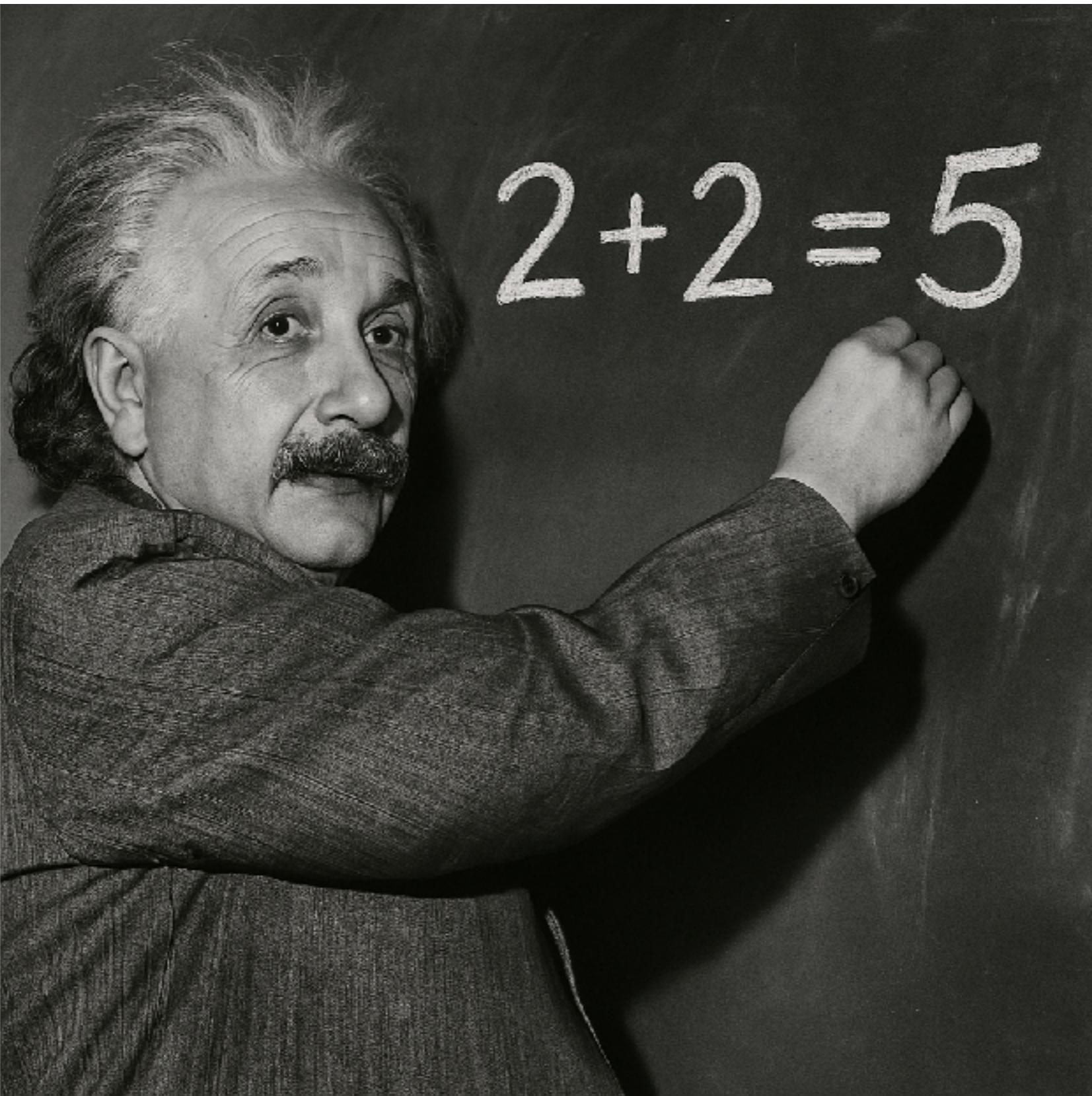
# Explainability

## Algorithm 1: How to write algorithms

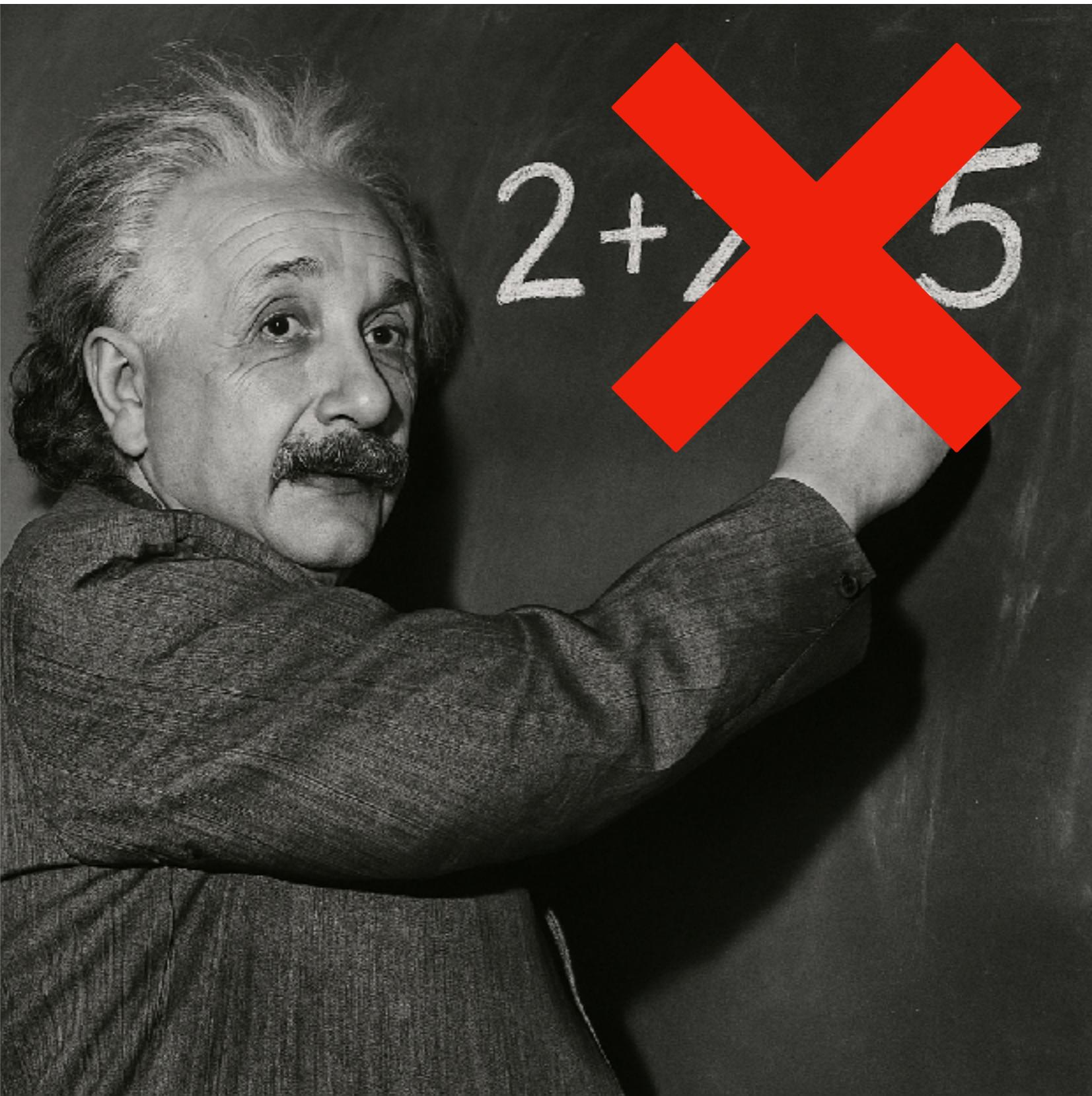


# **Trustworthy**

# Trustworthy



# Trustworthy



A problem

# FCAT

Key objectives: data efficiency, trust & ethics, understandability

To create Real AI, we have set up three grand scientific objectives: data efficiency, trust & ethics, and understandability.

Present-day AI solutions work well only in a very small subset of simple domains. In order to expand the deployment of AI further, we need new AI tools that overcome the key shortcomings of current AI systems.



## DATA EFFICIENCY

Current AI solutions can be very successful in domains where tasks are relatively simple and well-defined and an abundance of high-quality, properly annotated data are available. Existing AI methods do not, however, easily extend to domains where such data are not available or are difficult or expensive to acquire. Real AIs will be able to work with real-world scarce data – ill-defined, hard to acquire or unavailable.

## TRUST & ETHICS

We will create AIs that are secure, give trustworthy results, preserve privacy, are fair, and whose use is ethically sustainable. We will develop the required privacy-preserving and secure methods to address challenges related to susceptibility to manipulation, information stealing and unethical approaches. We will provide new resilient deep learning approaches for the currently popular and successful deep neural networks.



## UNDERSTANDABILITY

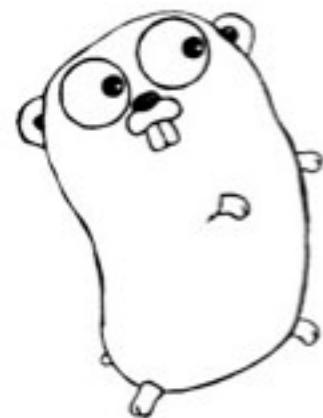
AI does not yet understand users. We need to open the "black box" of many AI methods: to understand how methods such as neural networks operate and what are the uncertainties inherent to their outputs. Modeling the user and the interaction will help the AI understand the user and vice versa. The outcome is AIs that are able to augment human capabilities in a multitude of tasks.

How?

# Inductive logic programming

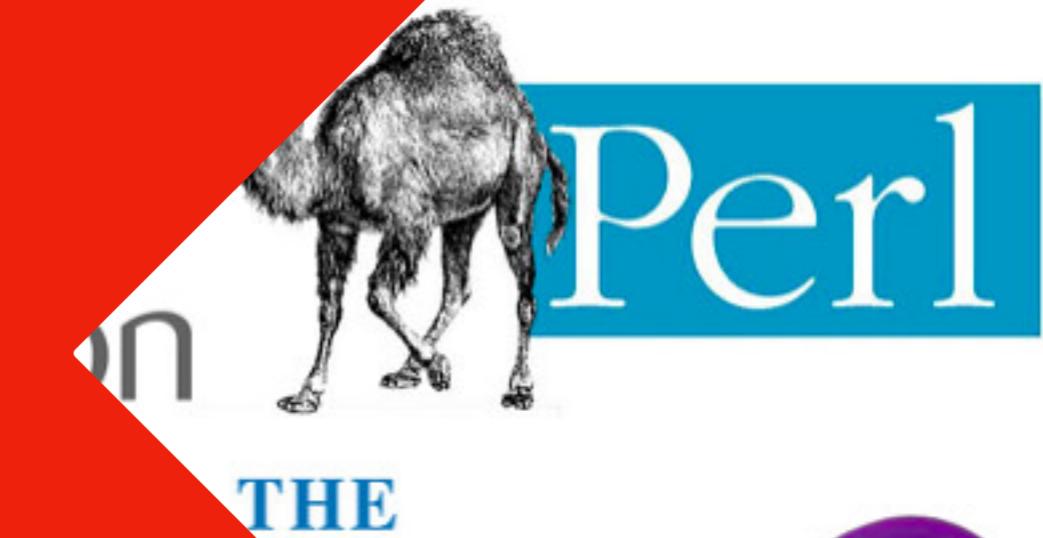


C++



JavaScript

C#



PROGRAMMING  
LANGUAGE

# Logical machine learning

# **Inductive logic programming**

# Inductive logic programming

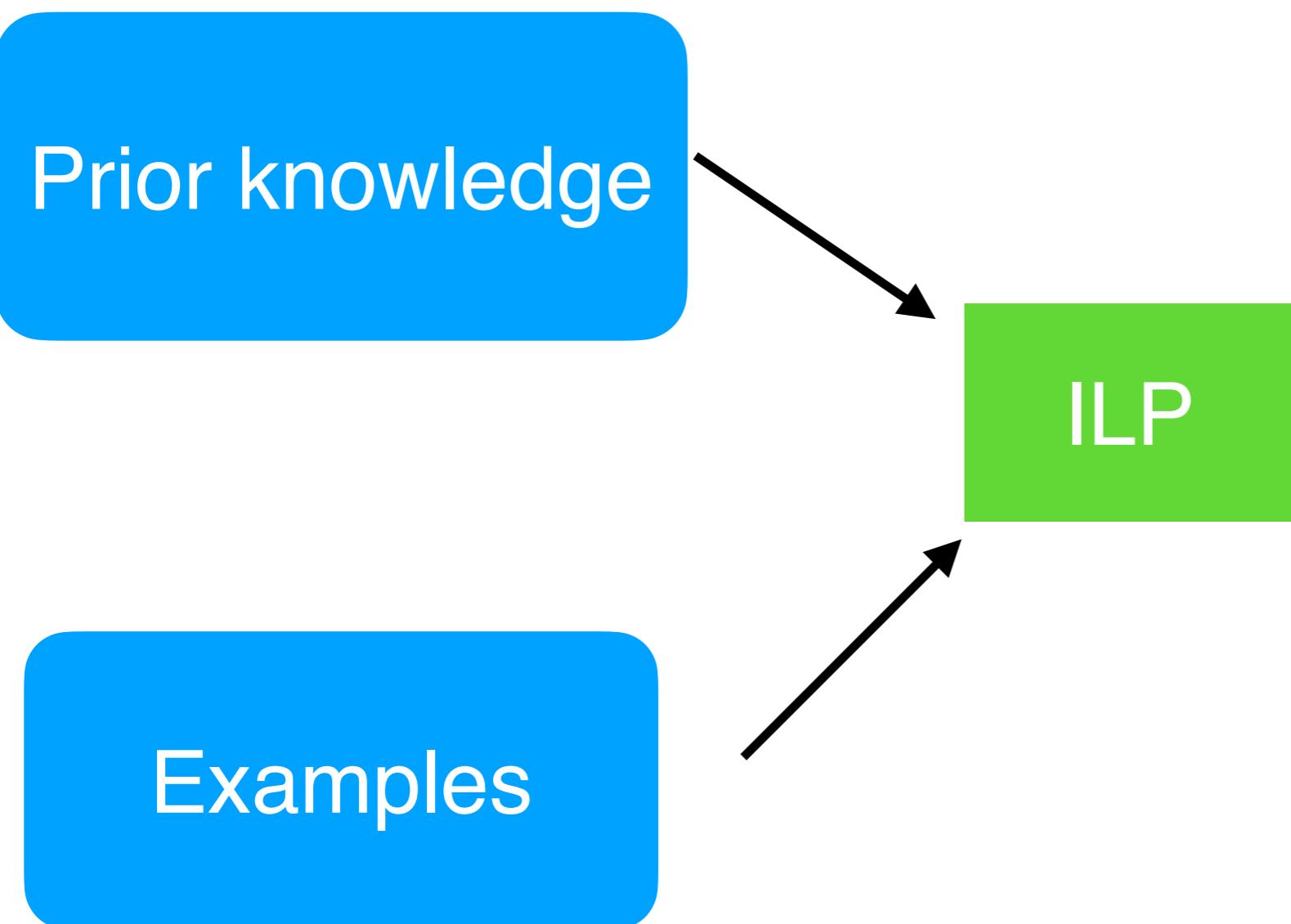
Prior knowledge

# Inductive logic programming

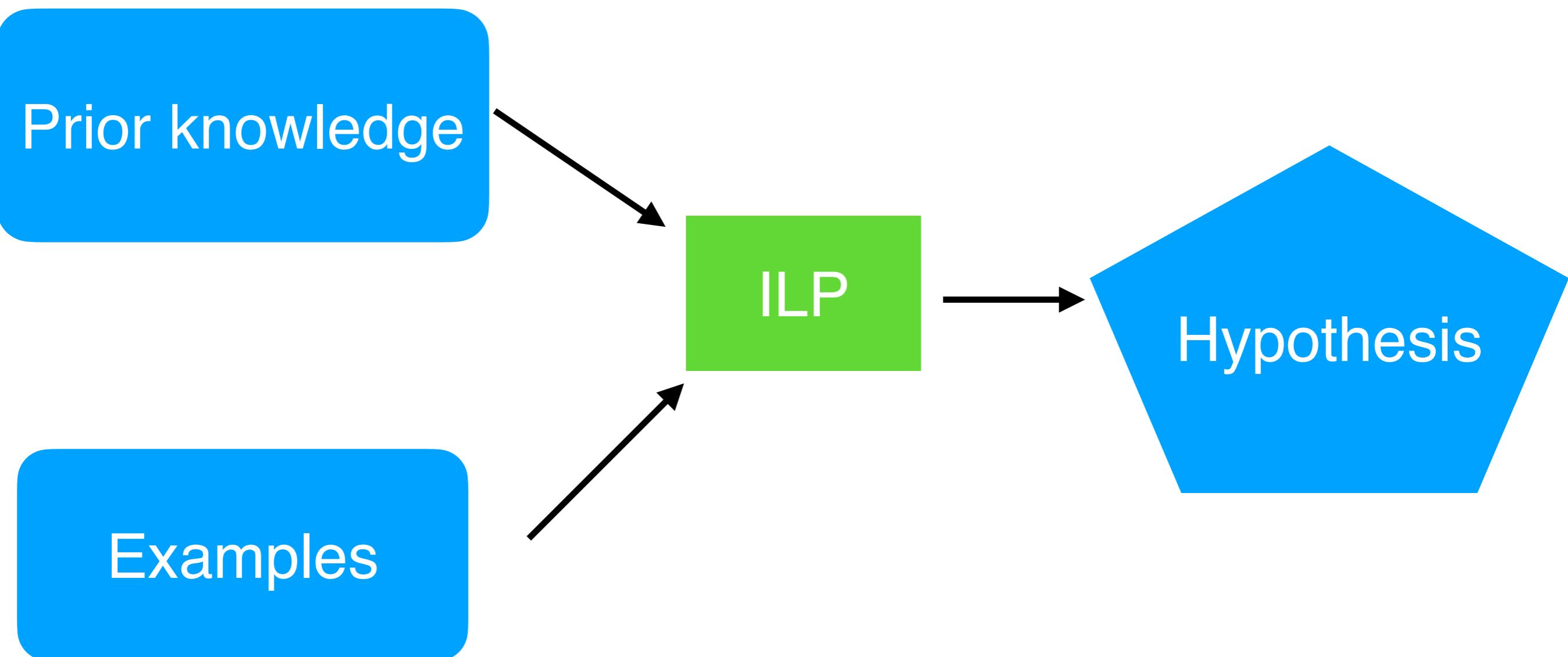
Prior knowledge

Examples

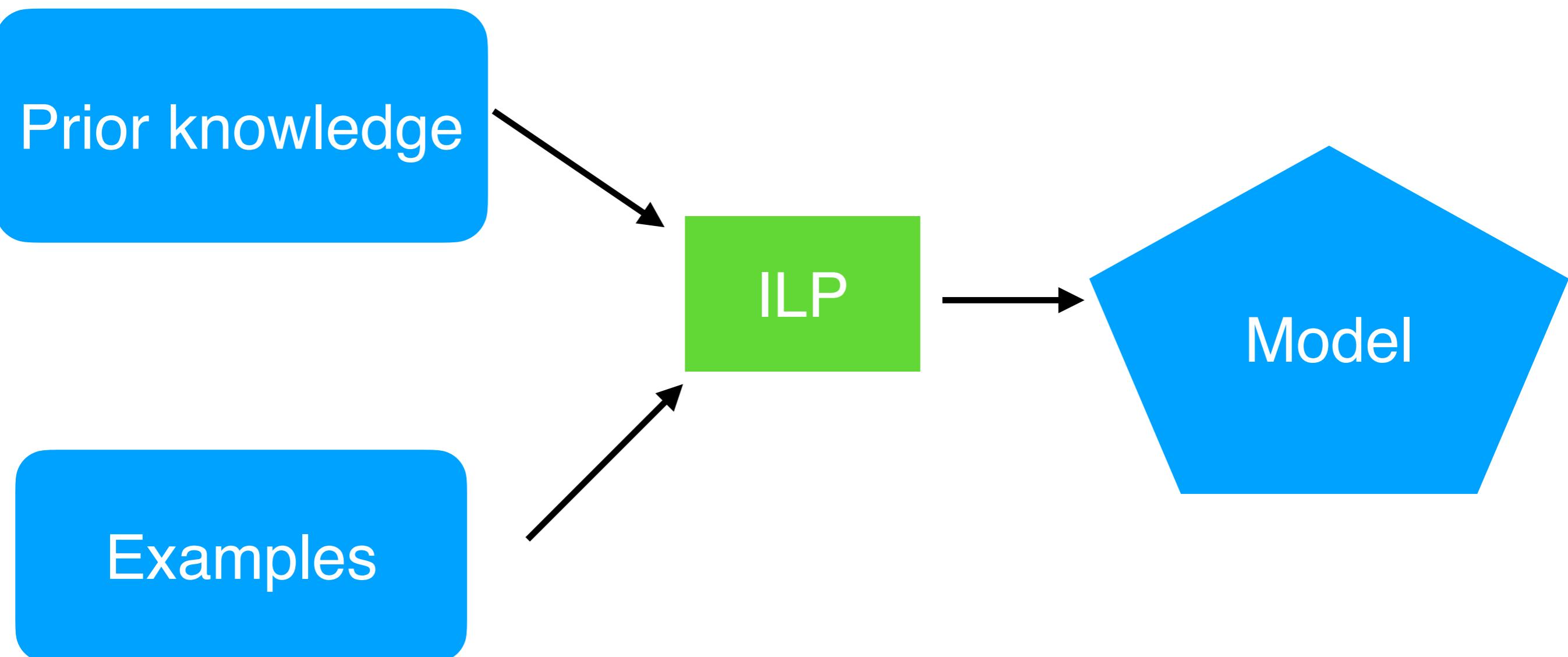
# Inductive logic programming



# Inductive logic programming

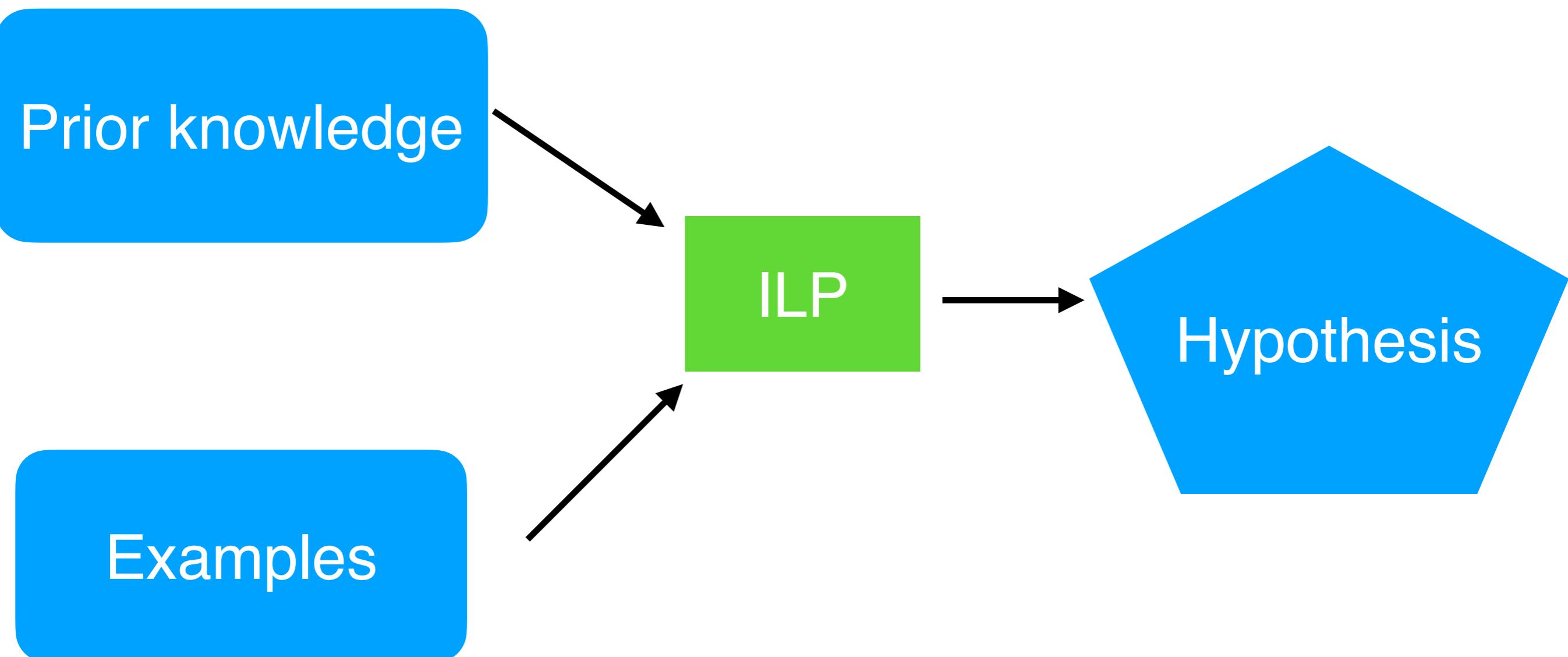


# Inductive logic programming



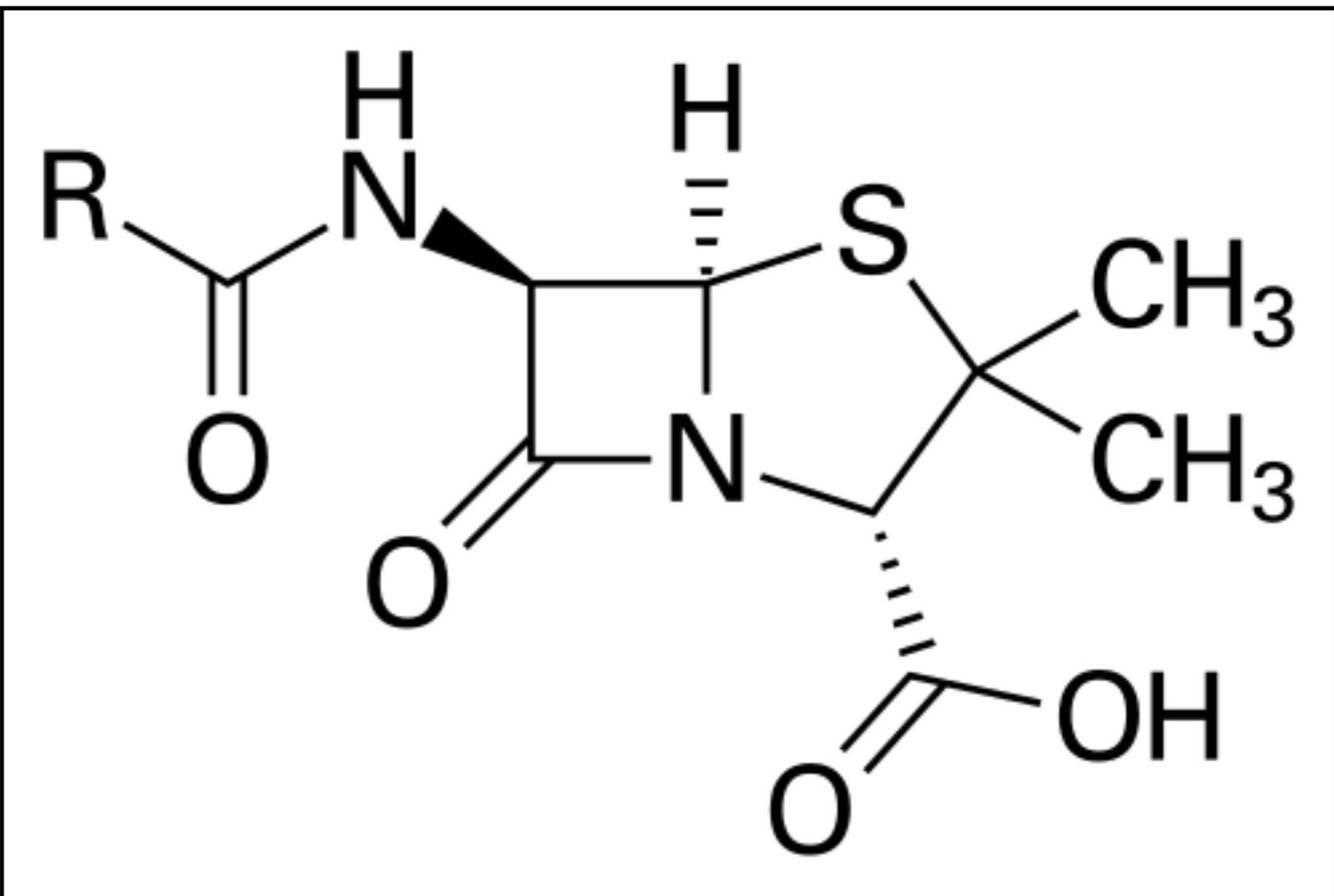
**Supervised machine learning**

# Inductive logic programming



**Uses logic to represent data**

Prior  
knowledge



## Prior knowledge

```
atom(7, o).  
atom(8, o).  
atom(9, h).  
atom(10, h).  
atom(11, h).  
atom(12, h).  
  
...  
bond(1, 2, single).  
bond(2, 3, single).  
bond(3, 4, single).  
bond(4, 5, single).  
  
...
```



## Observations

# Hypothesis

```
∀Mol((has_hydroxyl(Mol)
      ∧ has_amine(Mol)
      ∧ ∃A1,A2(bond(A1,A2,Mol)
                  ∧ atom(Mol,A1,oxygen)
                  ∧ atom(Mol,A2,nitrogen)))
      → active(Mol))
```

# Hypothesis

A drug works if it has both a hydroxyl group  
and an amine group and the oxygen atom of  
there is a bond between the hydroxyl group  
and the nitrogen atom of the amine group

# Why ILP?

- Interpretable ✓
- Efficient ✓
- Trustworthy ✓

What have I done?

Design ILP algorithms and package them into open-source tools

# Contributions

scalability

data efficiency

handling noisy numerical data

How does old ILP work?

# Old ILP

Pick a hypothesis and tweak it to fit the data

# My contribution

Automate Karl Popper's  
logic of scientific discovery



Science progresses by eliminating false theories

# **My contribution**

Popper ILP system

**What is the impact?**

**Learn hypotheses 100x bigger than  
traditional approaches**

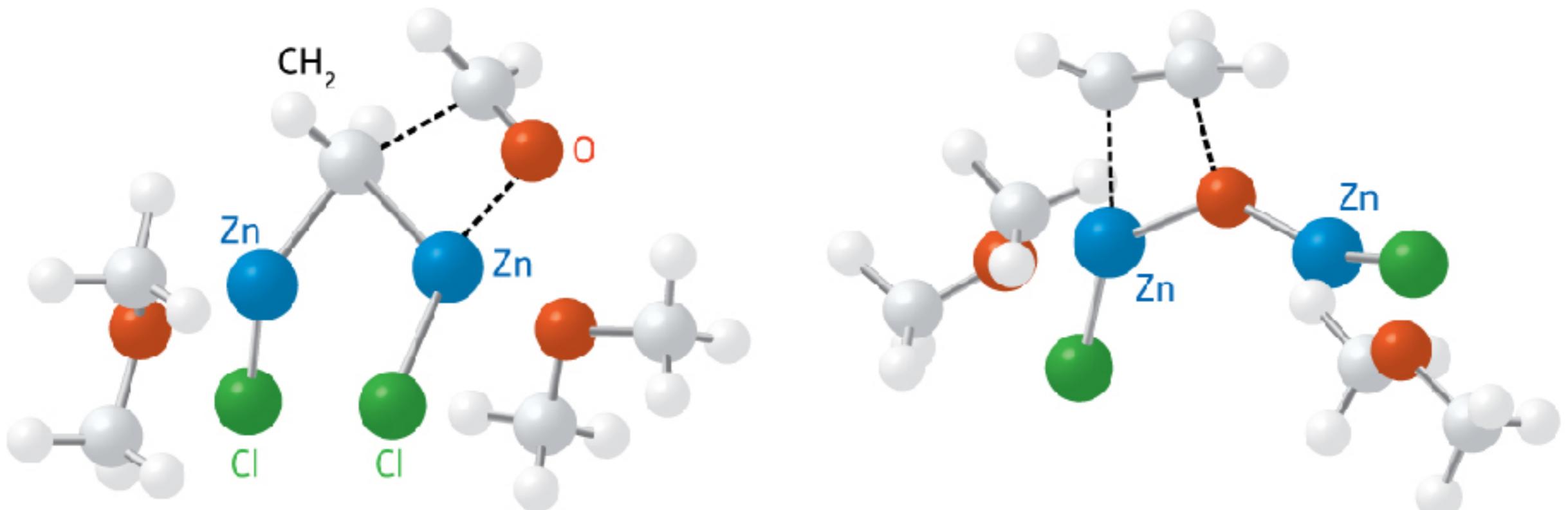
Learn from less data by learning  
**recursive** hypotheses

Handle noisy data by learning **MDL**  
hypotheses

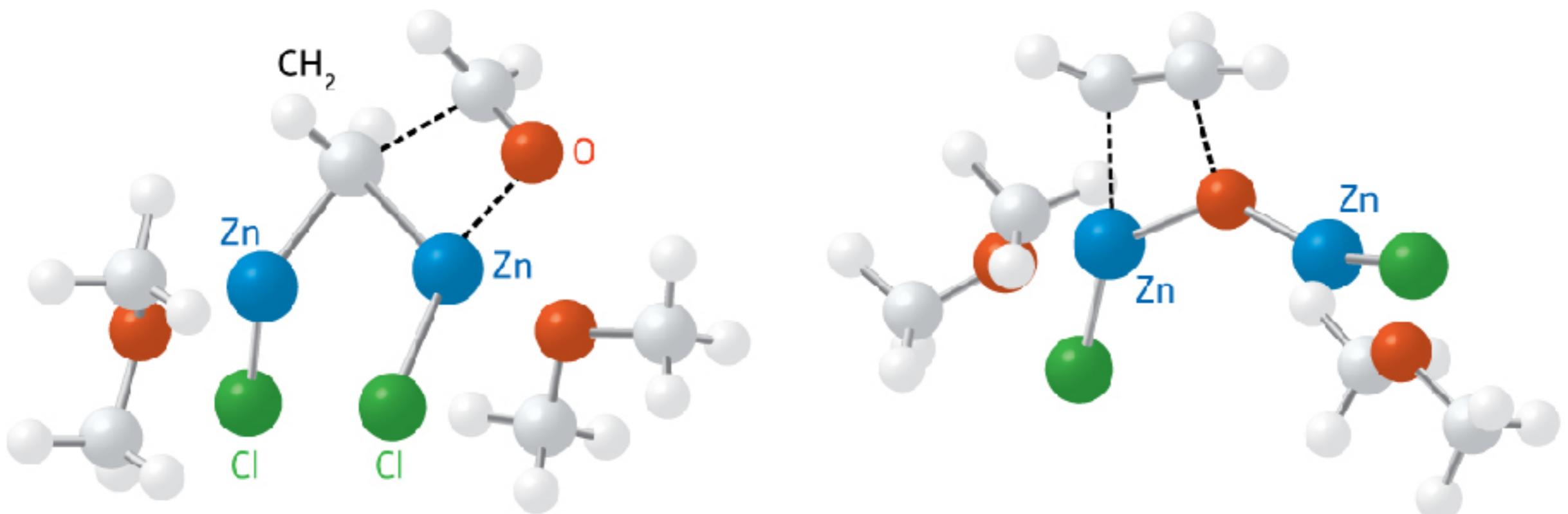
**But what is the actual impact?**

People use it

# Explainable drug design

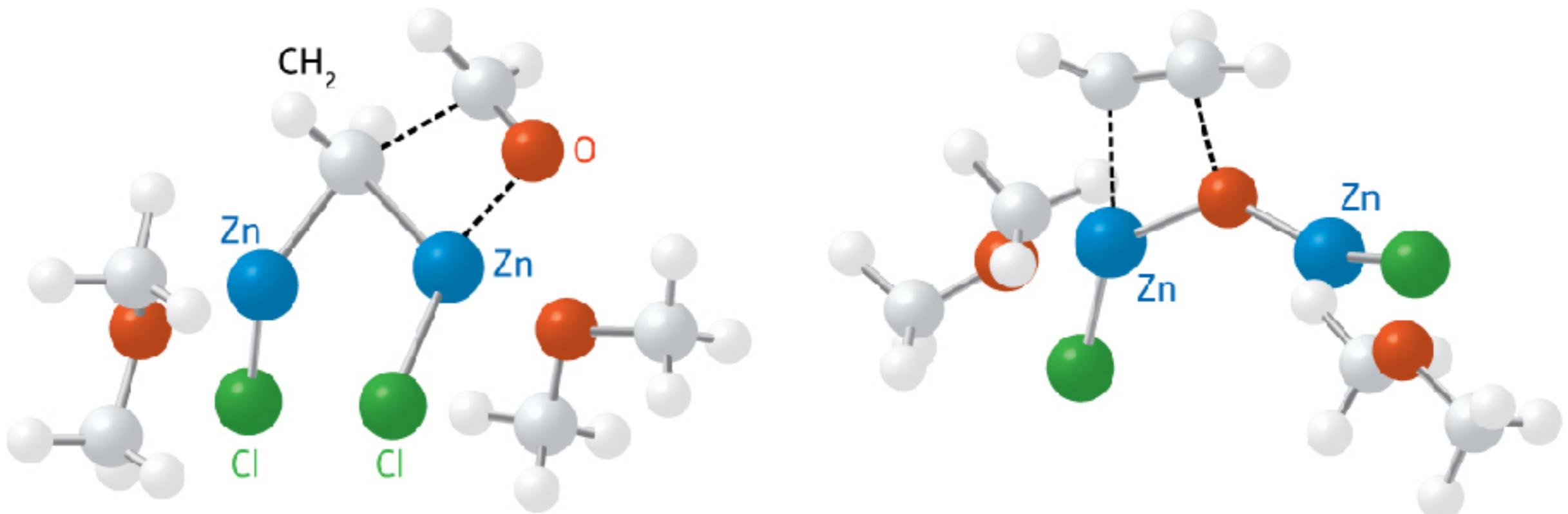


# Explainable drug design



```
active(A) ← zinc(A,C), zinc(A,B), bond(B,C,du),  
dist(A,B,C,D), leq(D,1.23).
```

# Explainable drug design



active if there are two zinc atoms  
and there is a 'du' bond type between them  
and the distance between them is  $\leq 1.23$

# Games



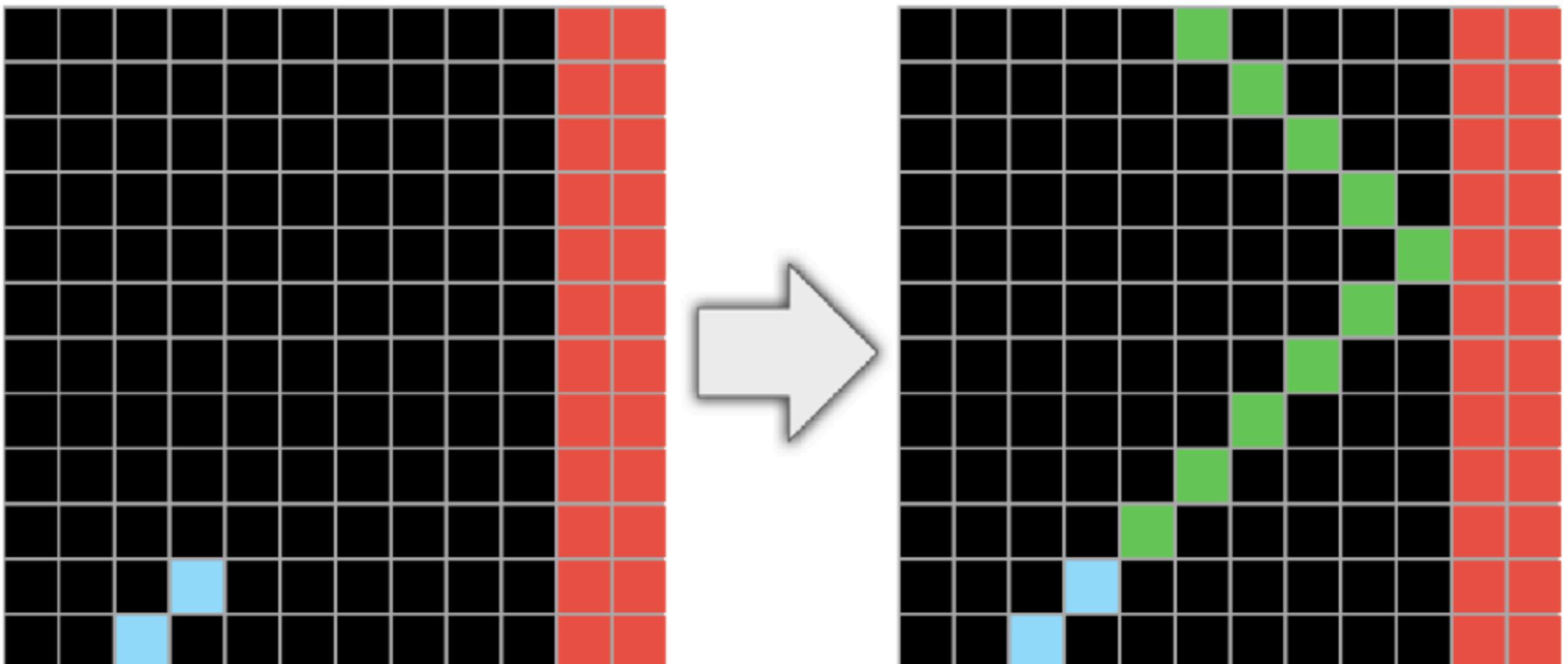
Stevens et al, 2023

# Puzzles



Lakkaraju et al, 2022

# Visual reasoning



# Human learning / program synthesis

[3, 1, 9, 0, 7]	→ [1, 9, 0]
[2, 1, 3, 4, 6, 9]	→ [1, 3]
[4, 1, 2, 3, 5, 0, 7, 6, 9, 8]	→ [1, 2, 3, 5]
[1, 5, 4, 2, 8, 3, 0, 6]	→ [5]
[5, 2, 1, 0, 4, 3, 7, 6]	→ [2, 1, 0, 4, 3]

What is missing?

# Now: undergraduate



Given much guidance learn **complex** hypotheses



# Five-years: professor



Given **little** guidance learn **publishable** hypotheses



# **How?**

**Better search**

**Complex prior knowledge**

**Scientist-aligned methods**

# Neural-symbolic

Can we learn which hypothesis to try next?

# How?

Better search

**Complex prior knowledge**

Scientist-aligned methods

# Uncertainty



Scale



Elbow Ruler



Calipers



Roll Meter



Micrometer



Beaker Glass



Stopwatch



Thermometer      Ruler



Angle Ruler

# **Uncertainty**

Can we combine Bayes and Popper?

# How?

Better search

Complex prior knowledge

**Scientist-aligned methods**

**There are significant discrepancies between  
what AI researchers do and what scientists need**

The ability to **understand a hypothesis** is equally, if not more, important than how well it performs

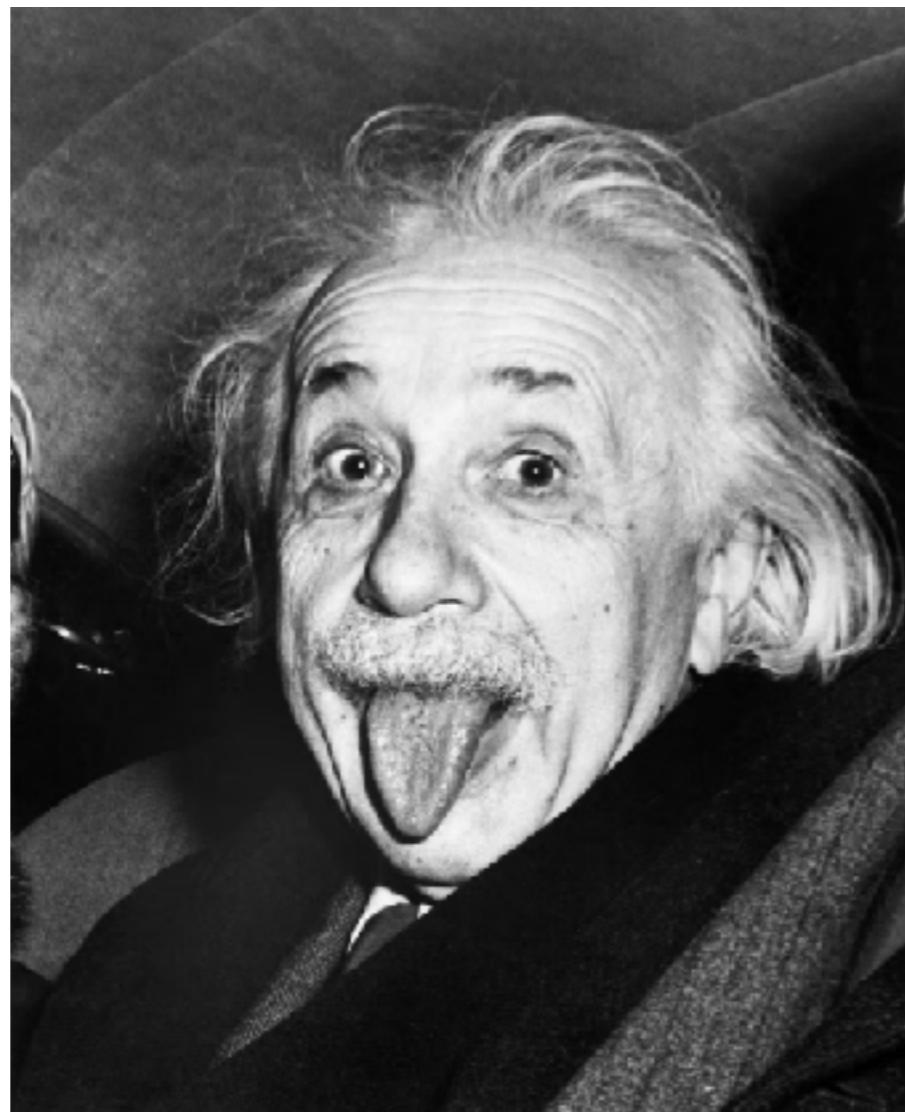
# Explainability

How do we trade-off accuracy vs explainability?

# Multidisciplinary collaborations



# 10-year goal: genius



Give **little** guidance make **Nobel-prize** worthy discoveries



2025



2031



2035

# Questions?

Inductive logic programming at 30: a new introduction. Cropper and Dumančić. JAIR 2022

<https://github.com/logic-and-learning-lab/Popper>

# Me

- Computer Engineering
- **Data Science**
- **Human-Technology Interaction**
- Mathematics
- Network and Information Security
- **Signal Processing**
- **Software Engineering**

# **Teaching**

**1.DATA.ML.310 Artificial Intelligence**

**2.DATA.ML.100 Introduction to Machine  
Learning**

**3.FIL.FIA.002. Logic**

# Popper

# Popper

0. Start with a hypothesis space

# Popper

0. Start with a hypothesis space
1. Select a hypothesis

# Popper

0. Start with a hypothesis space
1. Select a hypothesis
2. Empirically try to refute it

# Popper

0. Start with a hypothesis space
1. Select a hypothesis
2. Empirically try to refute it
3. If the hypothesis is falsified, determine **why**

# Popper

0. Start with a hypothesis space
1. Select a hypothesis
2. Empirically try to refute it
3. If the hypothesis is falsified, determine **why**
4. Use the **explanation** to prune the hypothesis space

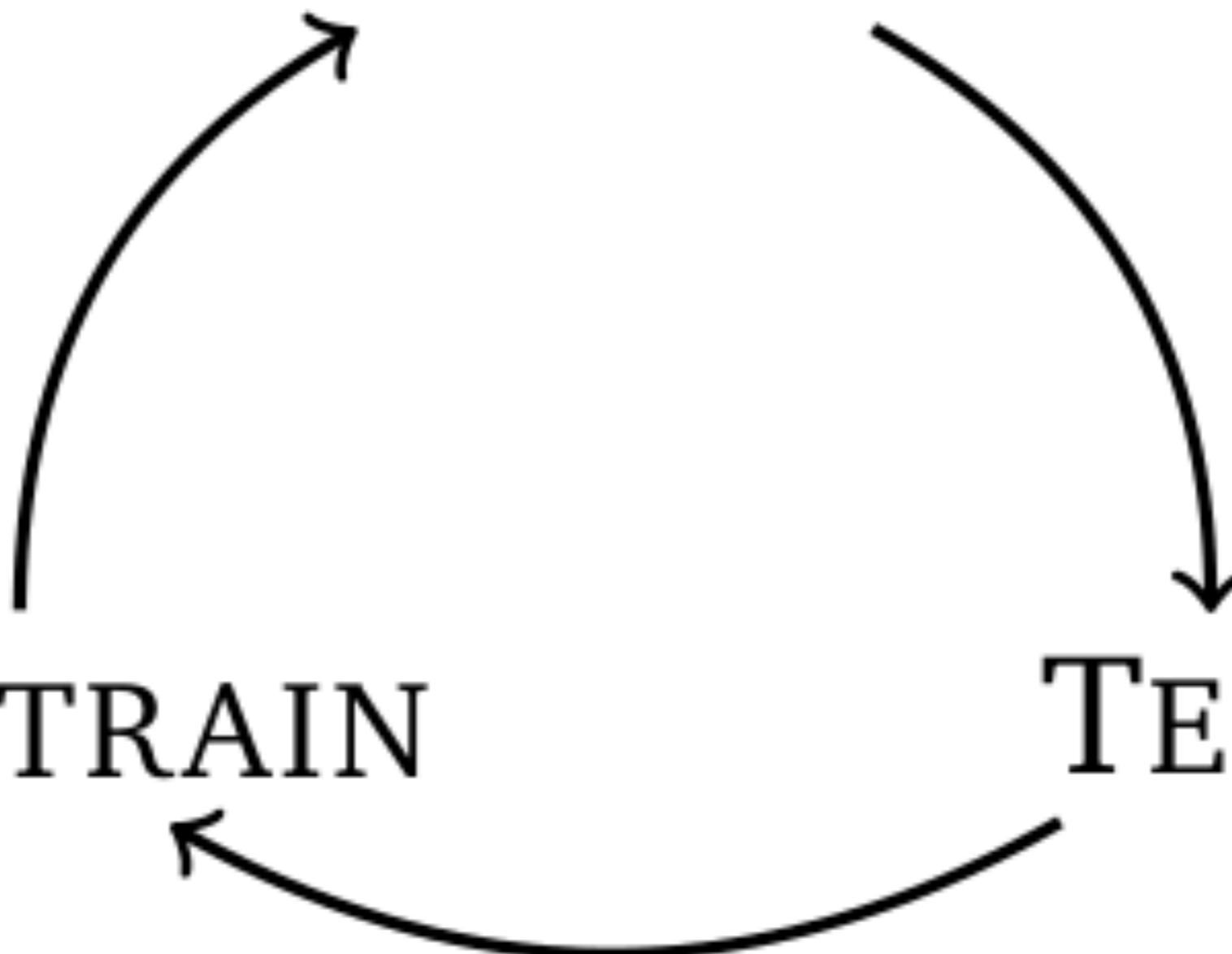
# Popper

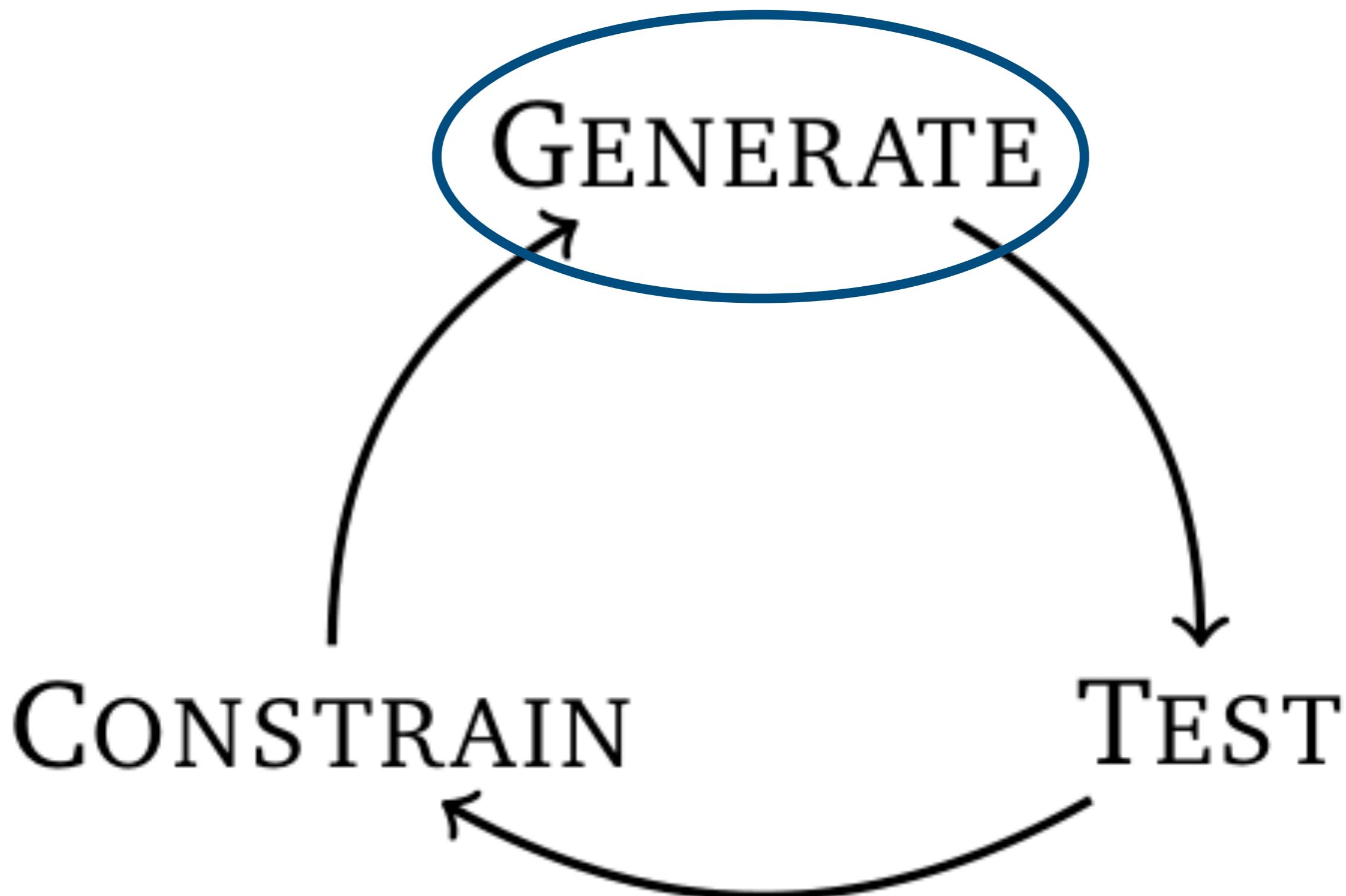
0. Start with a hypothesis space
1. Select a hypothesis
2. Empirically try to refute it
3. If the hypothesis is falsified, determine **why**
4. Use the **explanation** to prune the hypothesis space
5. Go to 1

GENERATE

CONSTRAIN

TEST





# Generate

We construct a logical formula where  
every truth assignment is a hypothesis

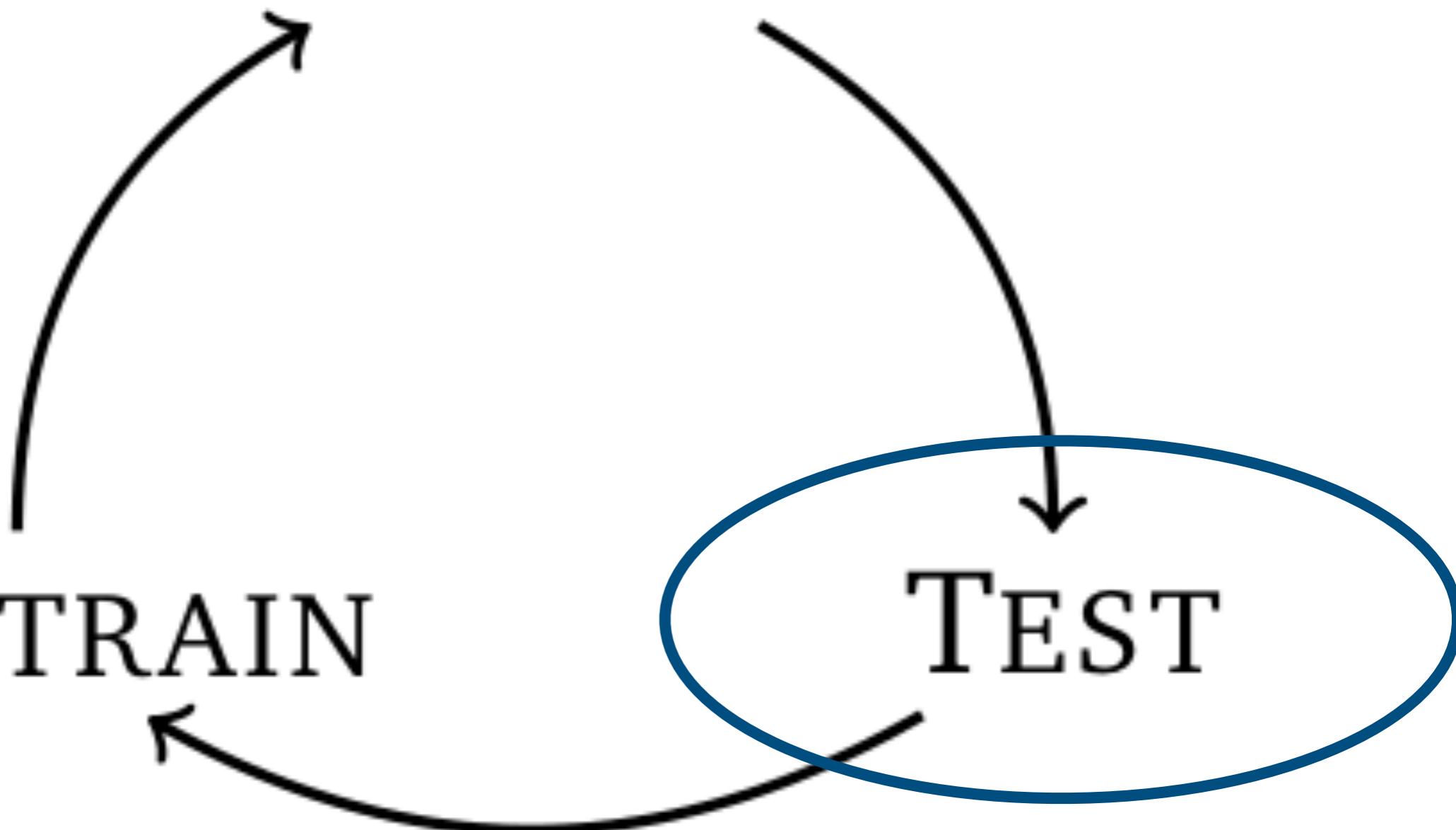
# Satisfiability problem

We ask a SAT solver to find a model/hypothesis

GENERATE

CONSTRAIN

TEST



GENERATE

CONSTRAIN

TEST



# Constrain

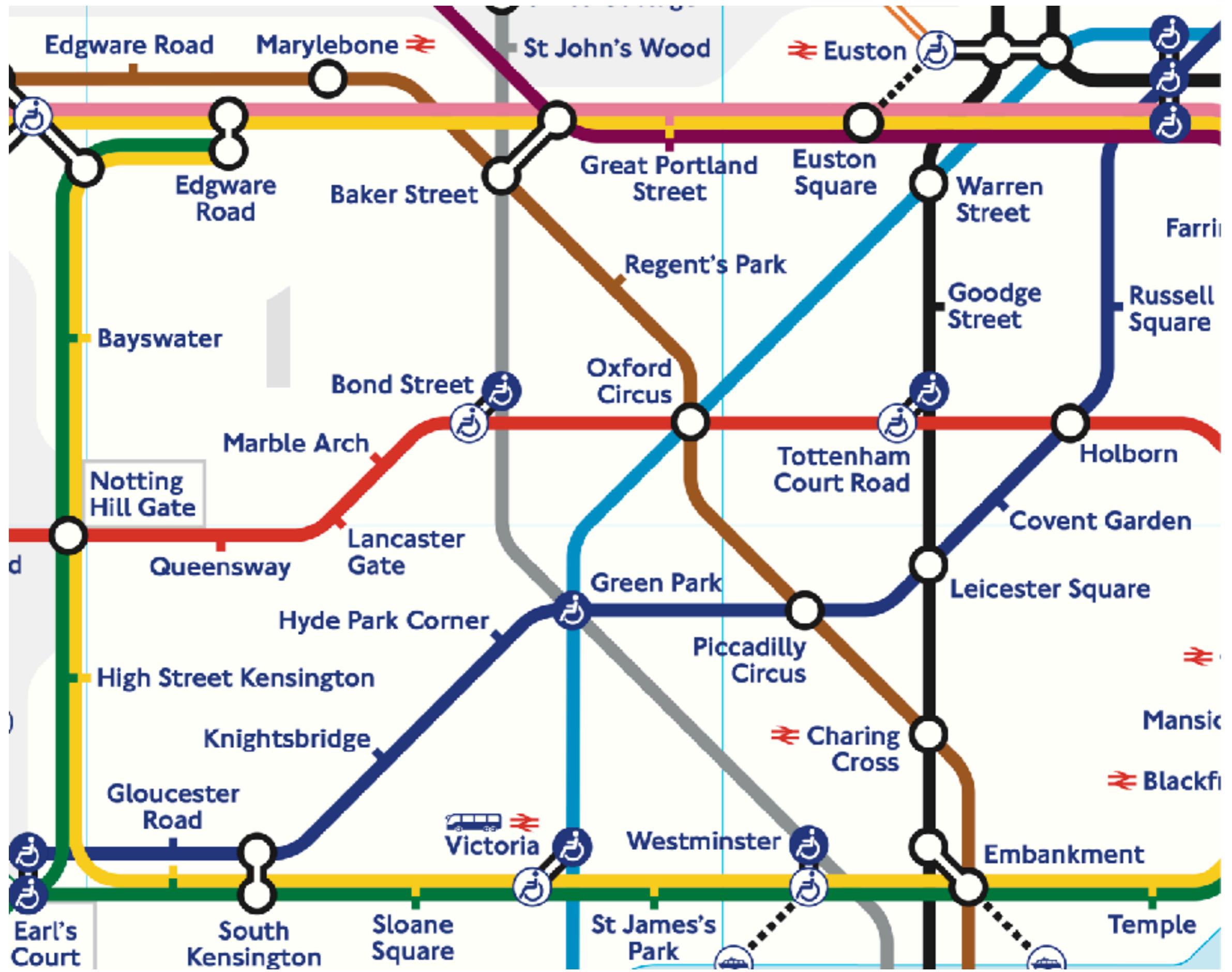
Adding constraints prunes models thus hypotheses

Popper can learn **recursive** hypotheses

# Recursion



**Grand challenge in ILP for 30 years**



edge(oxford\_circus, bond\_street).

edge(oxford\_circus, piccadilly\_circus).

edge(south\_kensington, gloucester\_road).

# Old ILP

connected(A,B) :- ?

# Old ILP

```
connected(A,B) :- edge(A,B).
```

A and B are connected if there is an edge between them

# Old ILP

```
connected(A,B) :- edge(A,C), edge(C,B).
```

A and B are connected via an intermediate edge C

# Old ILP

```
connected(A,B) :- edge(A,C), edge(C,D), edge(D,B).
```

A and B are connected via intermediate edges C and D

# Old ILP

```
connected(A,B) :- edge(A,B).  
connected(A,B) :- edge(A,C), edge(C,B).  
connected(A,B) :- edge(A,C), edge(C,D), edge(D,B).  
connected(A,B) :- edge(A,C), edge(C,D), edge(D,E), edge(E,B).  
....
```

# Old ILP

```
connected(A,B) :- edge(A,B).  
connected(A,B) :- edge(A,C), edge(C,B).  
connected(A,B) :- edge(A,C), edge(C,D), edge(D,B).  
connected(A,B) :- edge(A,C), edge(C,D), edge(D,E), edge(E,B).  
.... .
```

**Cannot generalise to arbitrary depth**

# Old ILP

```
connected(A,B) :- edge(A,B).  
connected(A,B) :- edge(A,C), edge(C,B).  
connected(A,B) :- edge(A,C), edge(C,D), edge(D,B).  
connected(A,B) :- edge(A,C), edge(C,D), edge(D,E), edge(E,B).  
.... .
```

**Difficult to learn because of its size**

# Old ILP

```
connected(A,B) :- edge(A,B).  
connected(A,B) :- edge(A,C), edge(C,B).  
connected(A,B) :- edge(A,C), edge(C,D), edge(D,B).  
connected(A,B) :- edge(A,C), edge(C,D), edge(D,E), edge(E,B).  
.... .
```

**Need to see an example of all path lengths**

# Popper

```
connected(A,B):- edge(A,B).
```

A and B are connected if there is an edge between them

# Popper

```
connected(A,B) :- edge(A,C), connected(C,B).
```

A and B are connected if there is an edge between A and C and C is **connected** to B

# Popper

```
connected(A,B) :- edge(A,B).  
connected(A,B) :- edge(A,C), connected(C,B).
```

**Generalises to arbitrary depth**

# Popper

```
connected(A,B) :- edge(A,B).  
connected(A,B) :- edge(A,C), connected(C,B).
```

**Reduces sample complexity**