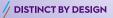


Professional Program in DATA SCIENCE

Algorithmic Bias



What is Bias?

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- **In common usage:** A tendency to favor or dislike a particular person, thing or idea that often affects our actions.
- In statistical analysis: Any time the results of an analysis are not consistent with what's really true.
- These are not unrelated! Often, one leads to the other, in either order!

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- **Truthiness Bias:** Easier-to-understand statements, statements that "seem" right, or statements repeated multiple times tend to be believed more easily.

Statistical Bias is the difference between an estimator's expected value and a true parameter value.

	Pop.		
Name	Param.	Estimator	Bias
Mean	μ	$\bar{\chi}$	$E(\bar{x}) - \mu$
Std. Dev.	σ	S	$E(s) - \sigma$
Variance	σ^2	s ²	$E(s^2) - \sigma^2$
Proportion	р	ρ̂	$E(\hat{p})-p$
Generically	θ	$\hat{m{ heta}}$	$E(\hat{\theta}) - \theta$

• An estimator whose bias is zero is called an *unbiased estimator*.

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- An estimator whose bias is zero is called an *unbiased estimator*.
- \bar{x} and s^2 are unbiased, but s is not.
- A mathematical statistics class might explore what makes a good estimator, and that knowledge can be helpful in applied machine learning.

Sources of Bias

Data collection is part of the calculation of any statistic, and can lead to bias!

Who is in the population?



How do we take a sample?



How do we ask a question?



Statistic(s):
As simple as \overline{x} ,
or as complicated as ML parameters.

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 - Sometimes respondents just don't tell the truth.

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- Do we understand the direction of causal relationships between predictor and response?
- Have we thought through the possible lurking variables?
- Does a response variable have the real-world meaning that we think it does?

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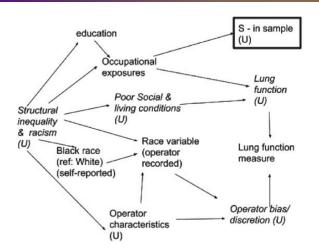
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 - Ill-defined, and usually a stand-in for other variables.
 - Promotes a view that race is causally related to outcomes.

Example: What are the causal connections between race and lung function?



Source: Teaching Yourself about Structural Racism Will Improve Your Machine Learning (nih.gov)

See also: Race, Ethnicity and Lung Function: A Brief History (nih.gov)

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- Patients likely to have higher health-care costs were recommended for these programs. (Cost was presumably easier to measure than "need for care.")
- Context: Patients who are not white have historically generated lower costs because they have more barriers to accessing health care.
- Result: Non-white patients had to be sicker before they were referred to support programs.

Source: A Health Care Algorithm Offered Less Care to Black Patients (arstechnica.com)

Example: Bias in recidivism risk assessments illustrates the importance of algorithm evaluation on subgroups.

 Pro Publica published an evaluation of the proprietary COMPAS risk assessment algorithm.

Race	Actual	Low Risk	High Risk	True %	Accuracy
All	Didn't Recidivate	2681	1281	68%	65%
All	Recidivated	1216	2035	63%	
Black	Didn't Recidivate	990	805	55%	64%
Black	Recidivated	532	1369	72%	
White	Didn't Recidivate	1139	349	77%	67%
White	Recidivated	461	505	52%	

Source: Machine Bias (propublica.org)

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- Contingency tables compare risk assessment to actual recidivism within two years of arrest.

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- Algorithms get out of date, losing accuracy over time.
- Algorithms can create feedback loops: negative decisions can create negative outcomes which reinforce negative decisions.

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 - Right to challenge decisions.
- Diversify data science teams to help eliminate blind spots.

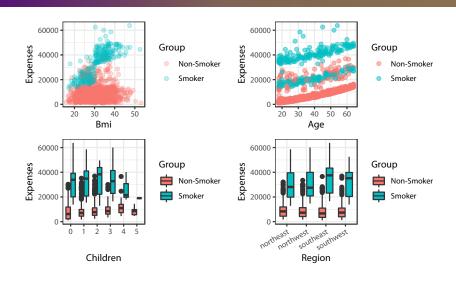
Some Technical Approaches: Balancing Data

Example: Balancing Data in Predicting Insurance Expense for Smokers and Non-Smokers

```
# Load the data.
ins <- read.csv("data/Insurance A.csv", stringsAsFactors=TRUE) %>%
 mutate(smoker = factor(if_else(smoker=="yes", "Smoker", "Non-Smoker"))) %>
 rename(Group = smoker)
names(ins) = str_to_title(names(ins))
                                     # Just nice graph labels.
head(ins, 2)
   Age Sex Bmi Children Group Region Expenses
##
## 1 19 female 27.9 0 Smoker southwest 16884.92
## 2 18 male 33.8 1 Non-Smoker southeast 1725.55
# Make a training and test set.
set.seed(892)
                                                # For repeatability
ind <- sample(1:nrow(ins), round(0.7*nrow(ins)))</pre>
ins.train <- ins[ind, ]</pre>
ins.test <- ins[-ind, ]</pre>
```

Data set in the public domain, from Machine Learning with R by Brett Lantz. See here for deatils (github.com)

Expenses depend most strongly on BMI and Age.



A Helpful Visualization Function for Bias and RMSE

Initial Random Forest Fit with Original Data Set

fit.orig <- randomForest(Expenses ~ ., data=ins.train)</pre>

table(ins.train\$Group) %>%
 kable()

Var1	Freq
Non-Smoker	750
Smoker	187

fit.stats(fit.orig, ins.test) %>
kable()

Group	Bias	RMSE
Non-Smoker	-411.5110	5438.676
Smoker	-772.9750	3384.287
ALL	-489.9334	5064.254

Initial Random Forest Fit with Non-Smokers Downsampled

table(ins.train.ds\$Group) %>%
 kable()

fit.stats(fit.ds, ins.test) %>%
 kable()

Var1	Freq
Non-Smoker	187
Smoker	187
•	

Group	Bias	RMSE
Non-Smoker	255.7121	5395.480
Smoker	-321.5732	2957.973
ALL	130.4657	4969.266

Initial Random Forest Fit with Smokers Upsampled

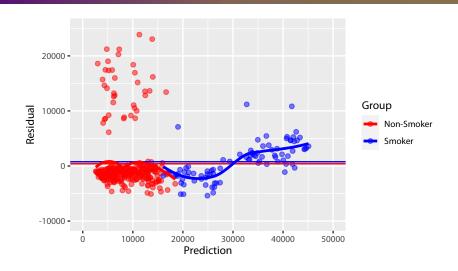
table(ins.train.us\$Group) %>% kable()

Freq
er 750
750

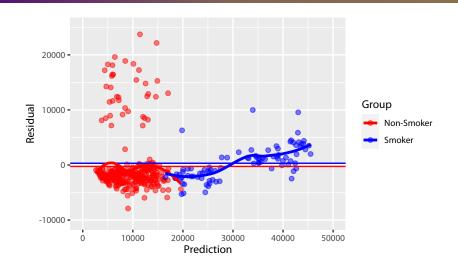
<pre>it.stats(fit.us,</pre>	<pre>ins.test)</pre>	%>%
<pre>kable()</pre>		

Group	Bias	RMSE
Non-Smoker	-355.9894	5436.022
Smoker	-379.3473	2760.703
ALL	-361.0571	4979.227

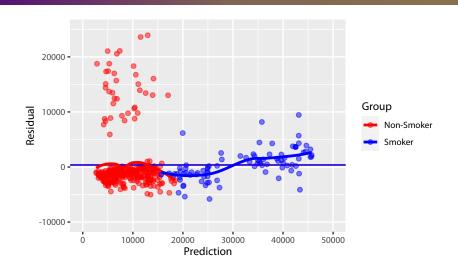
Residuals vs. Fit for Original Data



Residuals vs. Fit for Downsampled Data



Residuals vs. Fit for Upsampled Data



Example: Weighting a Categorical Response

Our data set has measurements of several varieties of dry beans.

```
beans <- read.csv("data/dry bean dataset.csv")</pre>
names(beans)
    [1] "Area"
                                              "MajorAxisLength"
##
                           "Perimeter"
                                                                 "MinorAxisLenath"
                                              "ConvexArea"
                                                                 "EquivDiameter"
##
    [5] "AspectRation"
                           "Eccentricity"
    [9] "Extent"
                           "Solidity"
                                              "roundness"
                                                                 "Compactness"
##
## [13] "ShapeFactor1"
                           "ShapeFactor2"
                                              "ShapeFactor3"
                                                                 "ShapeFactor4"
## [17] "Class"
table(beans$Class)/sum(table(beans$Class))
##
##
     BARBUNYA
                   BOMBAY
                                CALI
                                        DERMASON
                                                      HOROZ
                                                                  SEKER
                                                                               SIRA
## 0.09712732 0.03835133 0.11975608 0.26052458 0.14165014 0.14892366 0.19366689
```

KOKLU, M. and OZKAN, I.A., (2020), "Multiclass Classification of Dry Beans Using Computer Vision and Machine Learning Techniques," Computers and Electronics in Agriculture, 174, 105507, DOI: https://doi.org/10.1016/i.compag.2020.105507

Example: Weighting a Categorical Response

- Our data set has measurements of several varieties of dry beans.
- We'd like to predict whether a bean is of the "Sira" variety.

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Example: Weighting a Categorical Response

- Our data set has measurements of several varieties of dry beans.
- We'd like to predict whether a bean is of the "Sira" variety.
- Note that Sira makes up only about 19% of the data.

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```

An unweighted model has good accuracy, but

```
library(e1071)
# Focus only on Sira.
beans$Class <- fct_other(beans$Class, keep="SIRA")</pre>
summary(beans$Class)
## STRA Other
## 2636 10975
# Create training and test set.
set.seed(9084)
ind <- sample(1:nrow(beans), round(0.70*nrow(beans)))</pre>
beans.train <- beans[ind, ]
beans.test <- beans[-ind, ]</pre>
unweighted.svm <- svm(Class ~ ., data=beans.train)</pre>
unweighted.pred <- predict(unweighted.svm, newdata=beans.test)</pre>
```

An unweighted model has good accuracy, but is better at predicting beans that aren't Sira.

```
cm <- confusionMatrix(unweighted.pred, beans.test$Class, positive="SIRA")</pre>
cm$table
##
             Reference
## Prediction STRA Other
        SIRA
               660
##
                     102
##
        Other 101 3220
c(cm$overall["Accuracy"], cm$byClass[c("Sensitivity", "Specificity")])
      Accuracy Sensitivity Specificity
##
##
     0.9502817
                 0.8672799
                             0.9692956
```

We can balance the model's predictions by weighting the levels of the categorical response.

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- Most predictive model commands allow this with a command option.
- Weights determine how much each element counts towards the cost function that determines the model's fit.
- You might try weights inverse to each category's proportion.

The weighted model improved sensitivity at the cost of sensitivity and overall accuracy.

```
cm <- confusionMatrix(weighted.pred, beans.test$Class, positive="SIRA")</pre>
cm$table
##
             Reference
## Prediction STRA Other
        SIRA
               721
##
                     251
##
       Other
                40 3071
c(cm$overall["Accuracy"], cm$byClass[c("Sensitivity", "Specificity")])
     Accuracy Sensitivity Specificity
##
##
     0.9287289
                0.9474376
                             0.9244431
```

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- Weighting may reduce overall performance to predict one group better. You can't really create something out of nothing.
- Weighting can accentuate any problems with subgroup data.
- **Remember:** bias doesn't always have a technical solution!

The Final Case Weighting Example from the Lecture

An unweighted data set might contain more beans grown in wet conditions that are not Sira variety. To counteract that imbalance, we might weight each case, or row, perhaps with the inverse of its frequency.

Moisture	Variety	Weight
Dry	Other	1/1=1.0
Dry	Sira	1/1=1.0
Wet	Other	1/5=0.2
Wet	Other	1/5=0.2
Wet	Other	1/5=0.2
Wet	Sira	1/1=1.0
Wet	Other	1/5=0.2
Wet	Other	1/5=0.2