

Testing fundamental theories with global fits

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Overview

1. Fundamental theories & global fits
2. Foundations
3. Pitfalls
4. Results from GAMBIT

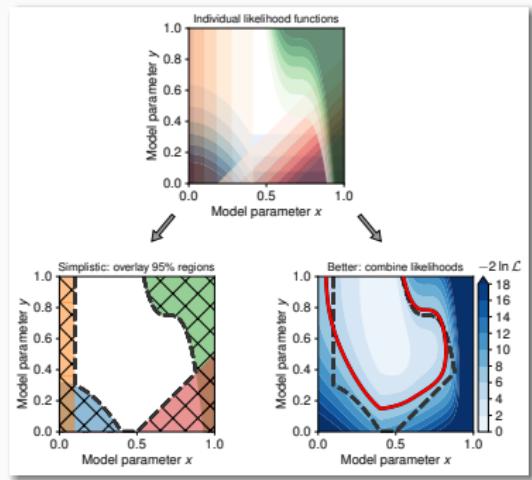
Fundamental theories & global fits

Fundamental theories – big models

- There are many motivations for physics beyond the Standard Model, e.g.,
 - Naturalness
 - Dark Matter
 - Gravity
 - Unification
 - Muon $g - 2$
- These models are not simple, as they typically contain many unknown parameters and scales
- E.g., even the minimal supersymmetric model adds hundreds of new soft-breaking parameters

Big data

- We are searching everywhere for new physics
- Inspire lists more than 800 “search” papers since 2010
- Searches at LHC, astrophysics, cosmology, etc.
- Each one with an independent statistical analysis
- Enormously powerful data.
We must make the most of it



Putting it all together

To make the most of this data, we must

- combine searches and measurements coherently
- model statistical, systematic and theory uncertainties
- explore an entire model — the whole parameter space
- test and compare models

These activities are **global fits**

What do I mean by parameter spaces?

- In science we build models to describe data
- These models usually come with several unknown parameters
 - e.g., the masses and couplings of new particles
- Models make a range of predictions, depending on the values that the parameters take
- We must consider all these possibilities in our **global fit**

GAMBIT



GAMBIT: The Global And Modular BSM Inference Tool

gambit.hepforge.org

github.com/GambitBSM

EPJC 77 (2017) 784

arXiv:1705.07908

- Extensive model database, beyond SUSY
- Fast definition of new datasets, theories
- Extensive observable/data libraries
- Plug&play scanning/physics/likelihood pack
- Various statistical options (frequentist /Bayesian)
- Fast LHC likelihood calculator
- Massively parallel
- Fully open-source



Members of: ATLAS, Belle-II, CLIC, CMS, CTA, Fermi-LAT, DARWIN, IceCube, LHCb, SHiP, XENON

Authors of: BubbleProfiler, Capt'n General, Contur, DarkAges, DarkSUSY, DDCalc, DirectDM, Diver, EasyScanHEP, ExoCLASS, FlexibleSUSY, gamLike, GM2Calc, HEPLike, IsaTools, MARTY, nuLike, PhaseTracer, PolyChord, Rivet, SOFTSUSY, SuperIso, SUSY-AI, xsec, Vevacious, WIMPSim

Recent collaborators: V Ananyev, P Athron, N Avis-Kozar, C Balázs, A Beniwal, LL Braseth, T Bringmann, A Buckley, J Butterworth, JE Camargo-Molina, C Chang, J Cornell, M Danninger, A Fowlie, T Gonzalo, W Handley, S Hoof, A Juelid, F Kahlhoefer, A Kvellestad, M Lecroq, C Lin, M Lucente, FN Mahmoudi, DJE Marsh, G Martinez, H Pacey, MT Prim, T Procter, F Rajec, A Raklev, R Ruiz, A Scafidi, P Scott, W Shorrock, C Sierra, P Stöcker, W Su, J Van den Abeele, A Vincent, M White, A Woodcock, Y Zhang ++

70+ participants in many experiments and numerous major theory codes

What is GAMBIT?

Software framework

- Combines collider, flavor, astrophysics, cosmological data
- Joint analysis of dark matter, neutrinos & BSM physics
- MPI + OpenMP parallelisation (record of 115,000 CPUs)
- Combines libraries & codes written in: C++, Fortran, Python, Mathematica...
- Highly modular Bits
- Often with several alternatives

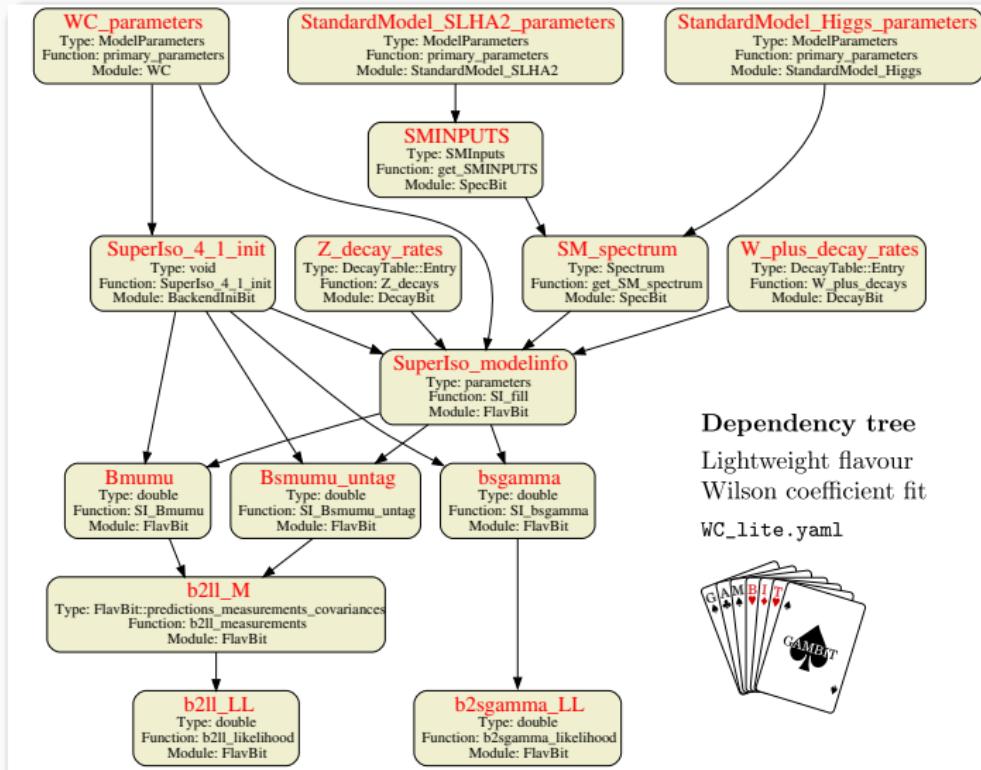
Community

- Particle physicists, cosmologists & statisticians (> 80 members)
- Generates interdisciplinary expertise & inspires new techniques
- Develop and maintain open source software
- Access to massive computing resources — 40 M CPU hours / year
- In-person meetings every 9 months

The *Bits

- **ColliderBit** – Collider searches for new particles at LHC and LEP
- **DarkBit** – Direct and indirect searches for dark matter
- **FlavBit** – Measurements of flavour physics observables
- **SpecBit** – Precision calculations of mass spectrum and RG running
- **DecayBit** – Precision calculations of particle decay widths and branching ratios
- **PrecisionBit** – Tests of precision observables and rare processes
- **NeutrinoBit** – Neutrino physics
- **CosmoBit** – Cosmology, e.g., Planck

GAMBIT structure



Foundations

Let the data speak for itself

Gould 1981

“ inanimate data can never speak for themselves, and we always bring to bear some conceptual framework, either intuitive and ill-formed, or tightly-formed and structured, to the task of investigation, analysis and interpretation ”

Tukey et al. 1977

“ No body of data tells us all we need to know about its own analysis ”

Jaynes 2003

“ The data cannot speak for themselves; and they never have, in any real problem of inference ”

Testing and estimation

Roughly speaking, statistical tasks separate into

1. Model testing or comparison
2. Estimating or inferring the model's parameters

I will focus on first. In my opinion, first we should establish whether a phenomena exists, and then infer its parameters or properties.

Testing

Jeffreys and Fisher agree!

Jeffreys 1939

“ [I]n what circumstances do observations support a change of the form of the law itself? This question is really logically prior to the estimation of the parameters, since the estimation problem presupposes that the parameters are relevant ”

Fisher 1925

“ It is a useful preliminary before making a statistical estimate ... to test if there is anything to justify estimation at all ”

Discoveries!

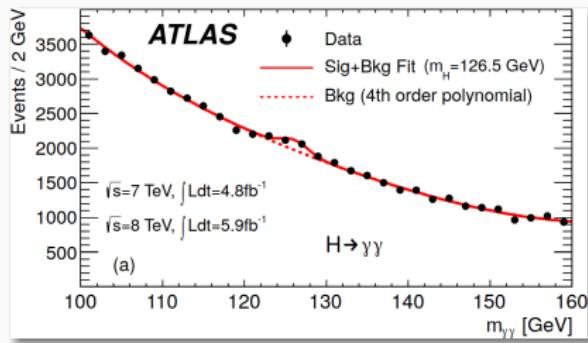
Classic example. Higgs discovery in 2012.



How do we judge when the data indicates the presence of a new particle or phenomena?

Discoveries!

Di-photon spectrum contains a resonance (Aad et al. 2012).



Discovery was announced based on a particular choice of statistical methodology.

Methodology

We need a statistical methodology to judge evidence for a discovery. In the time available, let's consider

1. Frequentist; see e.g., Lyons 1989; Cowan 1998; James 2006; Behnke et al. 2013. Two schools
 - Error control
 - Evidential
2. Bayesian; see e.g., D'Agostini 2003; Gregory 2005; Sivia and Skilling 2006; Trotta 2008; Linden, Dose, and Toussaint 2014; Bailer-Jones 2017

Likelihood

Methods typically require at least the likelihood (see e.g., Cousins 2020)

$$\mathcal{L}(\Theta) = p(D | M, \Theta)$$

This tells us the probability (density) of the observed data, D , given a particular model, M , and choice of parameters.

This is a function of the model's parameters, Θ , for fixed, observed data.

P-values

P-value (Wasserstein and Lazar 2016)

The p -value, p , is the probability of observing data as or more extreme than that observed, given the null hypothesis, H_0 , i.e.,

$$p = P(\lambda \geq \lambda_{\text{Observed}} \mid H_0)$$

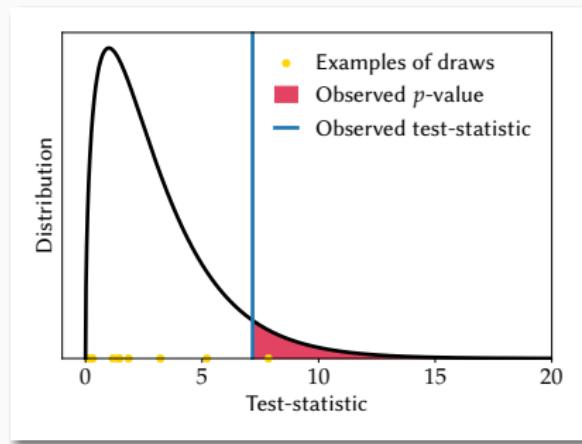
where λ is a test-statistic that summarises the data and defines extremeness, and H_0 specifies the distribution of λ

See Demortier 2008 for discussion about composite null hypotheses that don't uniquely specify the distribution of λ .

Test-statistic often based on (profiled) likelihood ratio (Neyman and Pearson 1933)

P-values

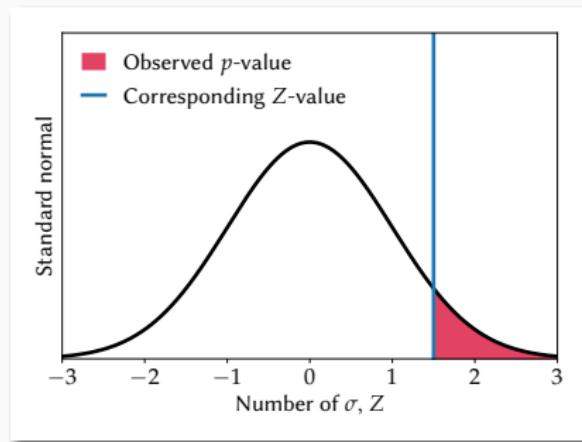
Thus p is a tail probability.



Thus p is uniformly distributed under H_0 (or dominated by uniform in discrete settings or composite null)

Z-values

In particle physics, it's common to translate p -values into Z -values.
 5σ corresponds to about $p = 10^{-7}$. This is just a convention



through the equation

$$Z = \Phi^{-1}(1 - p)$$

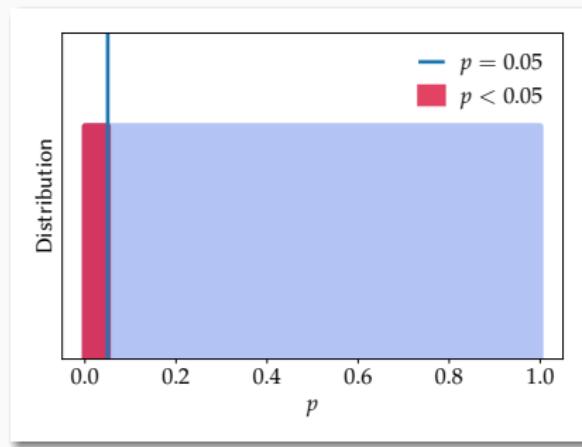
Interpreting p -values

P -values are popular in particle physics and elsewhere. Two possibly contradictory interpretations (Hubbard and Bayarri 2003):

- P is a **measure of evidence** against H_0 (Fisher 1925): small $p \Rightarrow H_0$ implausible. See e.g., Hubbard and Lindsay 2008; Schervish 1996; Berger and Sellke 1987; Senn 2001; Murtaugh 2014
- P is a **means to control error rate** (Neyman and Pearson 1933): if we reject null when p -value ≤ 0.05 , for example, becomes error theoretic approach with type 1 error rate $\alpha = 0.05$

Controlling type-1 error rate

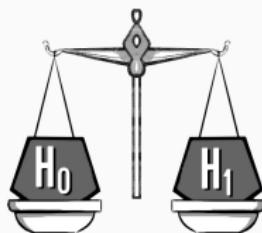
The p -value enables us to control type-1 error rate because it is uniformly distributed under the null



Placing a threshold $p < \alpha$ controls the type-one error rate to be α

Example from high-energy physics

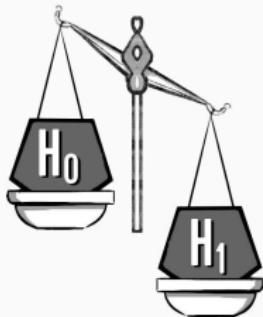
Original artwork Viktor Beekman and concepts Eric-Jan Wagenmakers



In high-energy physics, we want to discover new phenomena and new particles. Perform null hypothesis test:

- H_0 – Standard Model (SM) backgrounds only
- H_1 – SM + new physics, e.g. Higgs boson or supersymmetric particles

Example from high-energy physics

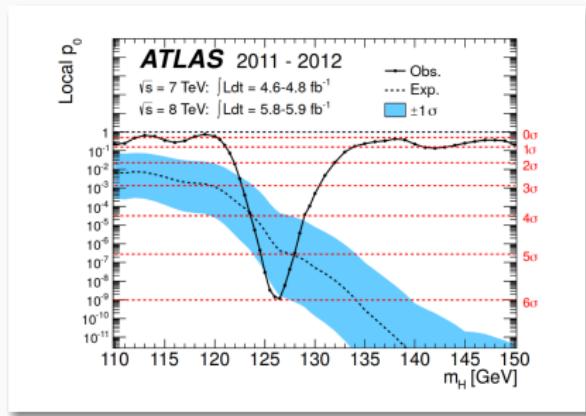


For a discovery we conventionally require a tiny global p -value of

$$p \lesssim 10^{-7} (5\sigma)$$

i.e., $\alpha \simeq 10^{-7}$ (Lyons 2013). Dual interpretation: threshold in evidence — extraordinary claims require extraordinary evidence — and imposes a 10^{-7} type-1 error rate.

Example from high-energy physics



Discovery of Higgs boson announced by ATLAS and CMS once significance greater than 5σ .

Some scares — e.g., 2015 diphoton excess (Strumia 2016) — but so far 5σ criterion prevented false discoveries (though think about flavor anomalies).

Misconceptions

Misconceptions galore by public and scientists, see e.g., Goodman 2008; Greenland et al. 2016

1. P is not probability of null hypothesis
2. P is not the probability that the data were produced by chance alone
3. P is not an error rate

Wagenmakers and al 2017

“The fact that academics don’t know what p means is a symptom of the fact that p doesn’t tell anything worth knowing”

Though see Murtaugh 2014; Lakens et al. 2018; Cousins 2018; Lakens 2021; Mayo 2018.

Bayes factors

Forget long-run errors rates and data we don't have. Compute the change in plausibility of models in light of the data we have

- With this and priors for the models, we could compute the posterior plausibility of each model
- If you like, you can compute the probability that you are making an error in the case at hand (cf. long-run error rates that are independent of the observed data)
- We just apply probability theory to the problem (Jeffreys 1939). Simple in theory; in practice there are difficulties.

Bayes factors

The Bayes factor (Kass and Raftery 1995) relates the relative plausibility of two models after data to their relative plausibility before data;

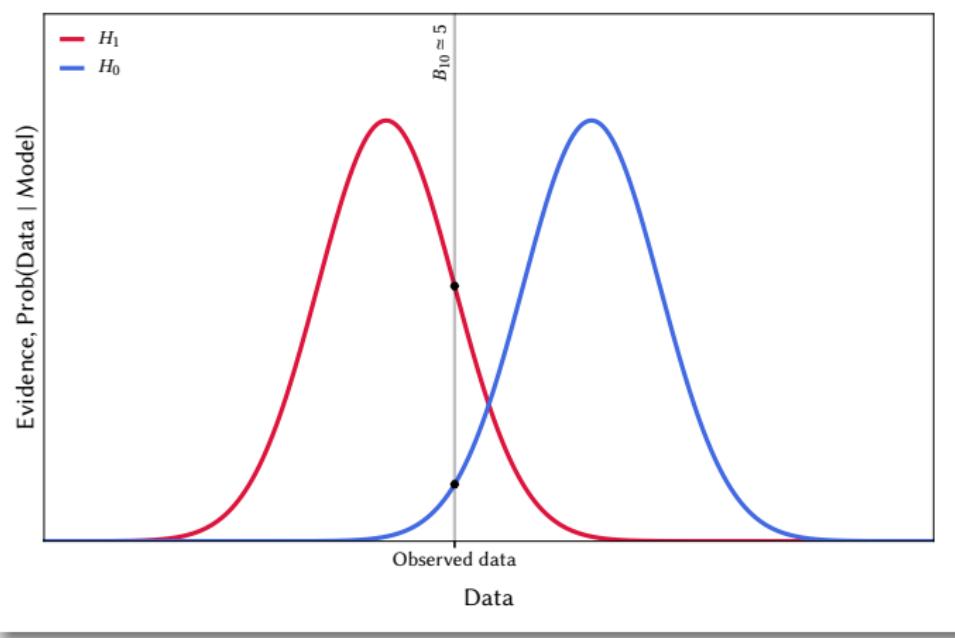
$$\text{Posterior odds} = \text{Bayes factor} \times \text{Prior odds}$$

where

$$\text{Bayes factor} = \frac{p(\text{Observed data} \mid \text{Model } a)}{p(\text{Observed data} \mid \text{Model } b)}$$

By applying laws of probability, we see that models should be compared by nothing other than **their ability to predict the observed data.**

Bayes factors



Bayesian evidence

The factors in the ratio are Bayesian evidences

$$\mathcal{Z} \equiv p(D | M) = \int_{\Omega_\Theta} \mathcal{L}(\Theta) \pi(\Theta) d\Theta,$$

where D is the observed data, $\mathcal{L}(\Theta) = p(D | \Theta, M)$ is the likelihood and $\pi(\Theta) = P(\Theta | M)$ is our prior, and Θ are the model's parameters.

The prior describes what we knew about the parameters before seeing the data

The evidence is the likelihood averaged over the prior — the averaging penalises fine-tuned models

Sensitivity to priors

Evidences are the likelihoods averaged over priors.

Many consider the resulting dependence of the Bayes factor on the priors to be a major and perhaps fatal problem; see e.g., Berger and Pericchi 2001; Cousins 2008

- **No priors, no predictions.** I need to compare your model's predictions with data. If you don't tell the plausible parameters, how am I to know what it predicts?
- **Sensitive to arbitrary choices.** If the inference changes dramatically within a class of reasonable priors, we can't draw reliable conclusions.

Sensitivity to priors

Evidences are the likelihoods averaged over priors.

Many consider the resulting dependence of the Bayes factor on the priors to be a major and perhaps fatal problem; see e.g., Berger and Pericchi 2001; Cousins 2008

Paraphrasing Hill 1975

“the lack of a concrete theory for choosing priors no more implies that one should not use Bayesian statistics than does the lack of a theory that tells us the right price to pay for groceries implies we should not use money”

Subjective & Objective

There are different approaches to constructing priors, leading to different flavors of Bayesian inference

Subjective

Priors reflect state of knowledge and could be constructed by e.g., consulting experts (see e.g., Goldstein 2006; Mikkola et al. 2021)

Dictated by state of knowledge

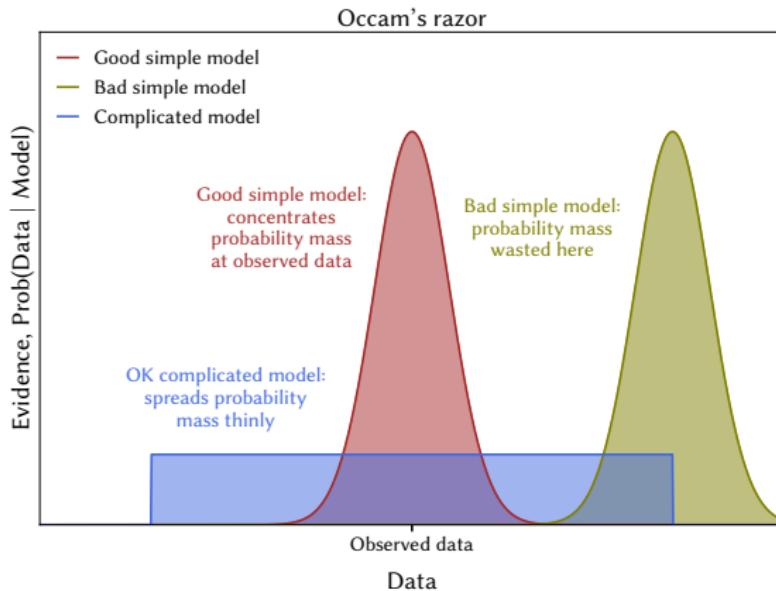
Priors could be dictated by e.g., a symmetry (Jaynes 1968)

Formal rules for selecting priors

Construct priors that e.g., maximise what we expect to learn about a model's parameters (Kass and Wasserman 1996; Consonni et al. 2018)

Occam's razor

Evidence automatic Occam razor (MacKay 1992; Jefferys and Berger 1992)



Likelihood principle

Originated by considering stopping rules (Barnard 1949). Proven by Birnbaum 1962

Berger and Wolpert 1988

“ all evidence, which is obtained from an experiment, about an unknown quantity θ , is contained in the likelihood function of θ for the given data $[\mathcal{L}(\theta)]$ ”

- Forbids evidential interpretations of frequentist statistics and p -values — since they depend on considering data other than that observed
- Implicitly obeyed by Bayesian statistics (though violated by reference priors)

Intuition for likelihood principle

Pratt 1962

“ An engineer draws a random sample of electron tubes and measures the plate voltage under certain conditions with a very accurate volt-meter ...

A statistician examines the measurements, which look normally distributed and vary from 75 to 99 volts with a mean of 87 and a standard deviation of 4 ... ”

Intuition for likelihood principle

Pratt 1962

“Later he visits the engineer’s laboratory, and notices that the volt meter used reads only as far as 100, so the population appears to be “censored.” This necessitates a new analysis, if the statistician is orthodox. ”

Intuition for likelihood principle

Pratt 1962

“ However, the engineer says he has another meter, equally accurate and reading to 1000 volts, which he would have used if any voltage had been over 100. This is a relief to the orthodox statistician, because it means the population was effectively uncensored after all. ”

Intuition for likelihood principle

Pratt 1962

“ But the next day the engineer telephones and says: “I just discovered my high-range volt-meter was not working the day I did the experiment you analyzed for me.” The statistician ascertains that the engineer would not have held up the experiment until the meter was fixed, and informs him that a new analysis will be required. The engineer is astounded. ”

Intuition for likelihood principle

Pratt 1962

“... “Next you’ll be asking me about my oscilloscope.””

Status of likelihood principle

At the time, considered profound by some though not universally accepted

Savage 1962

“Without any intent to speak with exaggeration or rhetorically, it seems to me that this is really a historic occasion.”

Over time limited practical impact: ignored by Bayesian because it's automatically satisfied; ignored by frequentists because it's automatically violated.

Likelihood land

Key part of Bayesian analysis

$$\text{Likelihood} \times \text{Prior density} = \text{Evidence} \times \text{Posterior density}$$

in which we marginalise over unknown parameters by multi-dimensional integration over the likelihood function.

Frequentist analysis, on the other hand, usually involves finding the best-fit parameters by finding the maximum of the likelihood function.

Pitfalls

Pitfall – the likelihood is not enough?

- Frequentist analysis violates **likelihood principle** (Berger and Wolpert 1988) and in fact requires whole **sampling distribution**

$$p(\textcolor{red}{D} \mid M, \Theta)$$

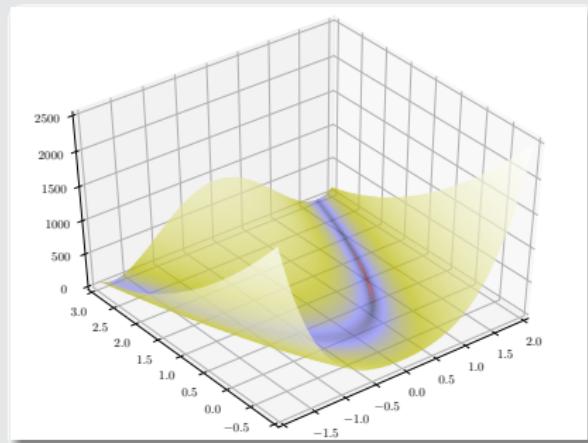
as a distribution in the data, $\textcolor{red}{D}$.

- Often we make asymptotic approximations (Wilks 1938; Chernoff 1954) for the sampling distribution that only require the likelihood, e.g., $2 \times \log$ likelihood ratio follows a χ^2 distribution. See e.g. Cowan et al. 2011.
- What if those assumptions don't apply? See e.g., Algeri et al. 2020. **We need public sampling distributions.**

Common pitfalls

Shape

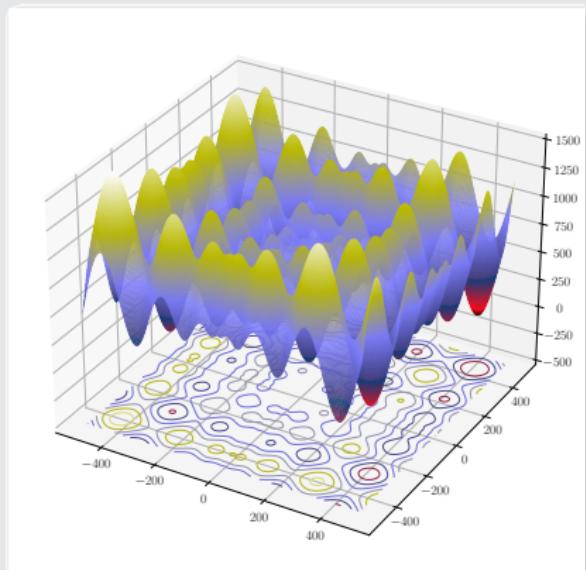
Likelihood could contain non-convex features, e.g., the classic Rosenbrock banana shape. Challenging for traditional optimisation and MCMC algorithms



Common pitfalls

Multi-modal

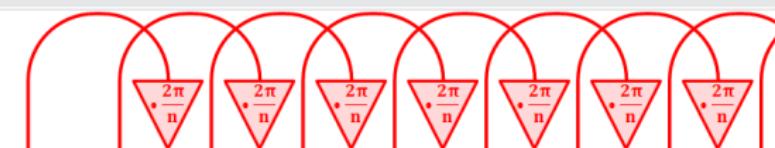
Likelihood could contain several distinct modes – how to find them all and the best one? (figure from Balázs et al. 2021)



Common pitfalls

Curse of dimensionality

Performance of numerical algorithms deteriorate exponentially with dimension

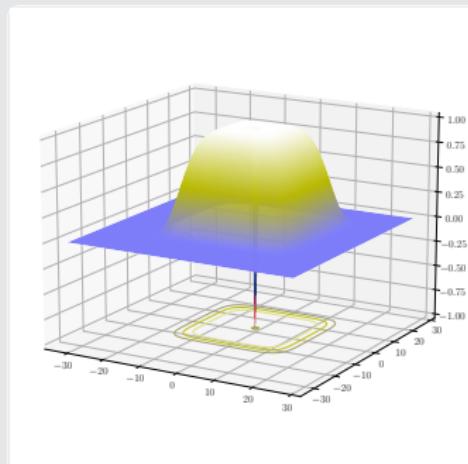


VOLUME (V_n)	$2R$	πR^2	$\frac{4}{3}\pi^2 R^3$	$\frac{1}{2}\pi^2 R^4$	$\frac{8}{15}\pi^2 R^5$	$\frac{1}{6}\pi^3 R^6$	$\frac{16}{105}\pi^3 R^7$	$\frac{1}{24}\pi^4 R^8$	$\frac{32}{945}\pi^4 R^9$
Number of Dimensions	$n = 1$	$n = 2$	$n = 3$	$n = 4$	$n = 5$	$n = 6$	$n = 7$	$n = 8$	$n = 9$
SURFACE AREA (S_{n-1})	2	$2\pi R$	$4\pi R^2$	$2\pi^2 R^3$	$\frac{8}{3}\pi^2 R^4$	$\pi^3 R^5$	$\frac{16}{15}\pi^3 R^6$	$\frac{1}{3}\pi^4 R^7$	$\frac{32}{105}\pi^4 R^8$

Common pitfalls

Compression

If the best-fit is a flagpole in the Atlantic ocean, it could easily be missed (Balázs et al. 2021)

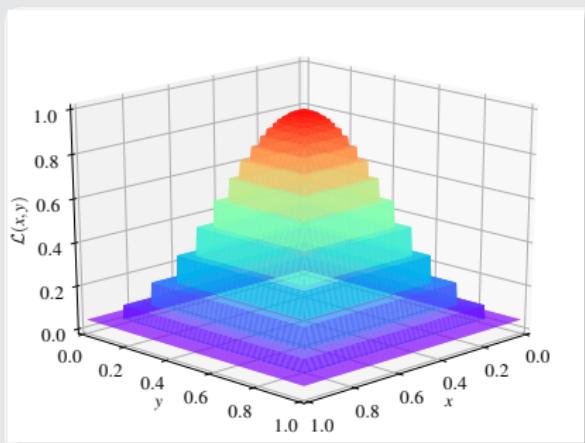


If sampling from the prior or if estimating the compression is important, convergence could be slow (**skilling2006**)

Common pitfalls

Plateaus

Likelihood functions involving plateaus may pose unexpected problems, see e.g., Schittenhelm and Wacker 2020; Fowlie, Handley, and Su 2021



A suite of statistical computation and optimization tools to overcome these challenges

1. Scanning algorithms

- Local — MINUIT2 — and global optimization — particle swarm, differential evolution
- Mark Chain Monte Carlo — Metropolis-Hastings and affine-invariance
- Nested sampling — PolyChord, MultiNest

2. Python Scanners

- Allows easy incorporation of new scanning algorithms into GAMBIT — e.g., emcee
- Modern machine learning techniques
- Embarassingly easy to incorporate

Pitfall – incomplete information

What if we don't know the form of the likelihood? What if an experiment only reports an asymmetric error (see e.g., Barlow 2004 for further discussion)

$$x = 45^{+5}_{-8}$$

or a bound

$$x < 62 \text{ @ 95% CL}$$

or an interval etc. Actually, what if they only report a symmetric error

$$x = 45 \pm 10$$

It's a Gaussian, $\mathcal{N}(45, 10^2)$, right? or is it?

Experimentalists know more, and they should tell us

Pitfall – intractable likelihood

What if we just can't work out the likelihood — it's intractable?

Fine — if we can draw pseudo data from the sampling distribution we can use likelihood-free inference methods, e.g., ABC (Diggle and Gratton 1984).

Public sampling distributions?

Pitfall – noisy estimate of likelihood

Consider case of LHC likelihoods. The likelihood might be a Poisson involving the expected number of events.

The expected number of events, though, can often only be computed through forward simulations of the whole experiment, involving MC simulations in e.g., Pythia and detector simulations

So we end up with a **noisy estimate of the likelihood**, $\hat{\mathcal{L}}$.

Pitfall – noisy estimate of likelihood

Careful! — if we run an optimiser, it will favour points with upward fluctuations in estimate of likelihood. Fitting noise.

If we run MCMC, we might get correct inferences if we have an unbiased estimator of the likelihood, $\langle \hat{\mathcal{L}} \rangle = \mathcal{L}$ — this is pseudo-marginal MCMC (Andrieu and Roberts 2009).

However, common MLE estimator of \mathcal{L} is biased.

Pitfall – posterior of null versus p

Of course,

$$\text{Posterior of null} \neq p\text{-value}$$

However, well-known that typically

$$\text{Posterior of null} \gg p\text{-value}$$

for broad classes of priors. P typically overstates the evidence against the null

Pitfall – posterior of null versus p

Bounds

Famous bound (Vovk 1993; Sellke, Bayarri, and Berger 2001) that under mild assumptions

$$B_{10} \leq \frac{1}{-ep \ln p}$$

With equal priors for null and alternative, $p = 0.05$ corresponds to at least about 30% posterior probability of the null (see e.g., Berger and Sellke 1987; Berger and Delampady 1987; Benjamin et al. 2018)

Examples from high-energy physics

I see this in high-energy physics. B for some Z (read papers for discussion of priors etc)

- Higgs discovery — posterior of null about 100 times greater than p (Fowlie 2019)
- ATLAS 2015 diphoton — $Z = 2.1\sigma$ and $B \simeq 7$ (Fowlie 2017)
- DAMPE — $Z = 2.3\sigma$ and $B \simeq 2$ (Fowlie 2018)
- 2020 XENON — $Z = 3.5\sigma$ and $B \simeq 3$ (Athron et al. 2020)

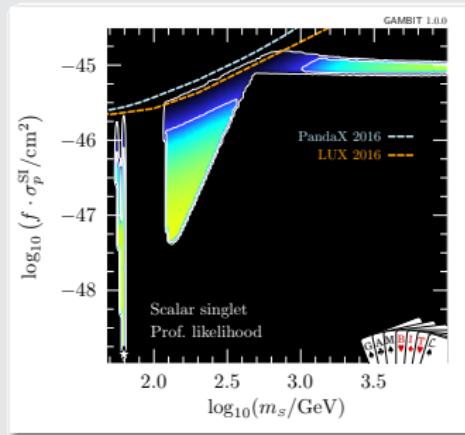
Results from GAMBIT

First results – 2017

Scalar singlet dark matter – 1705.07931

Mass and coupling + 13 nuisance parameters

LUX, XENON100, PandaX, SuperCDMS, IceCube, relic density, and Higgs width data

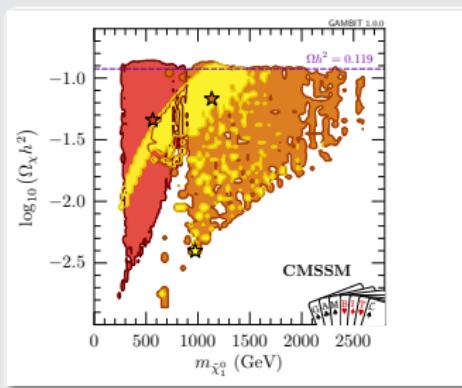


First results – 2017

Constrained MSSM – 1705.07935

4 GUT parameters + 5 nuisances

LUX, PandaX, and direct simulation of LHC Run 1 and early Run 2 searches

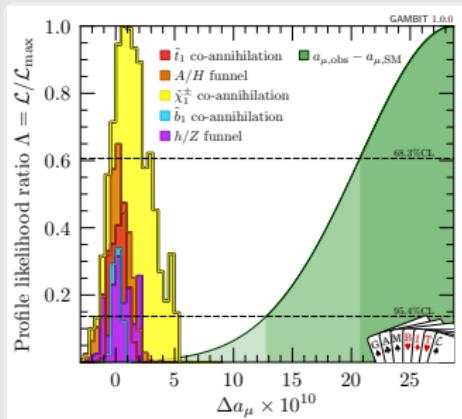


First results – 2017

Weak-scale MSSM – 1705.07917

Many parameters + 5 nuisances

LUX, PandaX, and direct simulation of LHC Run 1 and early Run 2 searches



Electroweakinos

Global collider physics fit of the electroweakino spectrum, using data from LEP, ATLAS and CMS – 1809.02097

Combined collider constraints on neutralinos and charginos

The GAMBIT Collaboration: Peter Athron^{1,2}, Csaba Balázs^{1,2},
Andy Buckley³, Jonathan M. Cornell⁴, Matthias Dannerger⁵, Ben Farmer⁶,
Andrew Fowlie^{1,2,9}, Tomás E. Gonzalo¹⁰, Julia Harz¹¹, Paul Jackson^{12,2},
Rose Kudzman-Blais⁵, Anders Kvellestad^{10,6,a}, Gregory D. Martinez¹³,
Andreas Petridis^{12,2}, Are Raklev¹⁰, Christopher Rogan¹⁴, Pat Scott⁶,
Abhishek Sharma^{12,2}, Martin White^{12,2,b}, Yang Zhang^{1,2}

Combine available leptonic SUSY search analysis likelihoods, and
scan a larger phenomenological model space than in experimental
papers

Decouple neutralinos and charginos

Name	Spin	P_R	Gauge Eigenstates	Mass Eigenstates
Higgs bosons	0	+1	$H_u^0 \ H_d^0 \ H_u^+ \ H_d^-$	$h^0 \ H^0 \ A^0 \ H^\pm$
squarks	0	-1	$\tilde{u}_L \ \tilde{u}_R \ \tilde{d}_L \ \tilde{d}_R$ $\tilde{s}_L \ \tilde{s}_R \ \tilde{b}_L \ \tilde{b}_R$ $\tilde{t}_L \ \tilde{t}_R \ b_L \ \tilde{b}_R$	(same) (same) $\tilde{t}_1 \ \tilde{t}_2 \ \tilde{b}_1 \ \tilde{b}_2$
selectrons	0	-1	$\tilde{e}_L \ \tilde{e}_R \ \tilde{\nu}_e$ $\tilde{\mu}_L \ \tilde{\mu}_R \ \tilde{\nu}_\mu$ $\tilde{\tau}_L \ \tilde{\tau}_R \ \tilde{\nu}_\tau$	(same) (same) $\tilde{\tau}_1 \ \tilde{\tau}_2 \ \tilde{\nu}_\tau$
neutralinos	1/2	-1	$\tilde{B}^0 \ \tilde{W}^0 \ \tilde{H}_u^0 \ \tilde{H}_d^0$	$\tilde{\chi}_1^0 \ \tilde{\chi}_2^0 \ \tilde{\chi}_3^0 \ \tilde{\chi}_4^0$
charginos	1/2	-1	$\tilde{W}^\pm \ \tilde{H}_u^+ \ \tilde{H}_d^-$	$\tilde{\chi}_1^\pm \ \tilde{\chi}_2^\pm$
gluino	1/2	-1	\tilde{g}	(same)

Decoupled

Decouple neutralinos and charginos

Neutralinos

$$\psi^0 = (\tilde{B}, \tilde{W}^0, \tilde{H}_d^0, \tilde{H}_u^0)$$

$$M_N = \begin{pmatrix} M_1 & 0 & -\frac{1}{2}g'vc_\beta & \frac{1}{2}g'vs_\beta \\ 0 & M_2 & \frac{1}{2}gv c_\beta & -\frac{1}{2}gv s_\beta \\ -\frac{1}{2}g'vc_\beta & \frac{1}{2}gv c_\beta & 0 & -\mu \\ \frac{1}{2}g'vs_\beta & -\frac{1}{2}gv s_\beta & -\mu & 0 \end{pmatrix}$$

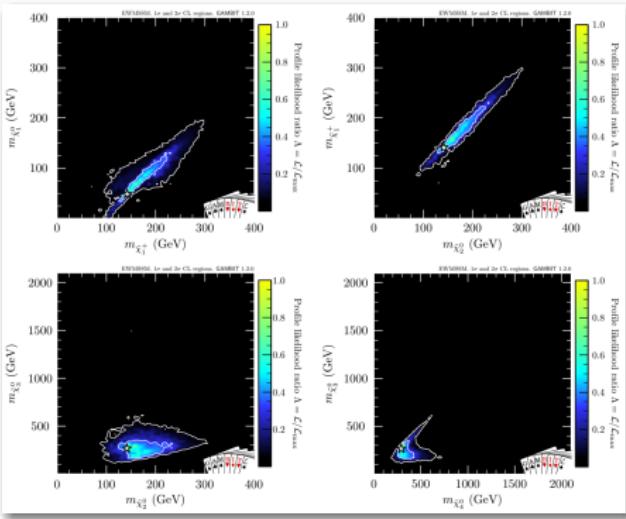
Charginos

$$\psi^\pm = (\tilde{W}^+, \tilde{H}_u^+, \tilde{W}^-, \tilde{H}_d^-)$$

$$M_C = \begin{pmatrix} 0 & X^T \\ X & 0 \end{pmatrix}, \text{ where } X = \begin{pmatrix} M_2 & \frac{gv s_\beta}{\sqrt{2}} \\ \frac{gv c_\beta}{\sqrt{2}} & \mu \end{pmatrix}$$

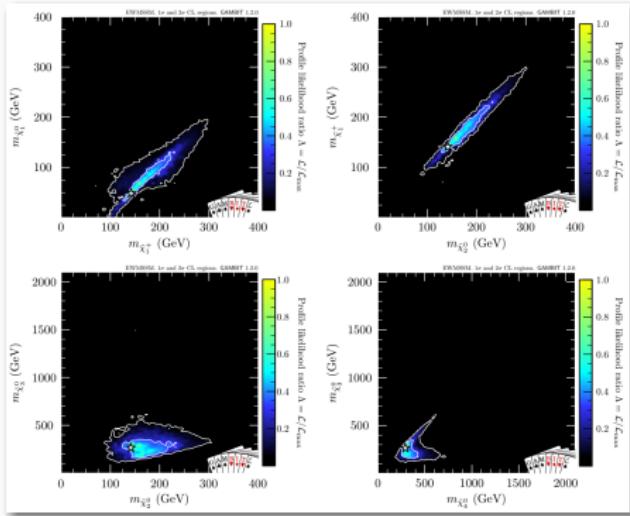
Results

- Combination of searches reveals mild excesses, local $\approx 3.3\sigma$
- Neutralinos and charginos $\lesssim 500$ GeV: is this light SUSY?
- Hidden from simplified models



Results

- Combination of searches reveals mild excesses, local $\approx 3.3\sigma$
- Neutralinos and charginos $\lesssim 500$ GeV: is this light SUSY?
- **Hidden from simplified models**



Anomaly gone in later datasets; update forthcoming

Open

Everything's open – code, data, plot scripts

The screenshot shows a Zenodo dataset page. At the top, there is a search bar, an upload button, and a communities section. Below the header, the date 'September 7, 2018' is displayed. The main title is 'Supplementary Data: Combined collider constraints on neutralinos and charginos' by 'The GAMBIT Collaboration'. A 'Dataset' button is highlighted in green, indicating the type of record. The file is labeled 'Open Access'. The description below the title reads: 'Combined collider constraints on neutralinos and charginos.' It notes that the files contain data for the EW MSSM model considered in the GAMBIT paper on constraints on electroweakinos. A 'Preview' section is visible, showing the 'Supplementary Data' heading and a brief description of the constraints. The bottom part of the screenshot lists the contents of the dataset, including YAML files, a universal YAML fragment, a final hdf5 file containing combined results, and a final hdf5 file from a postprocessed run including Dark Matter constraints.

September 7, 2018

Dataset Open Access

Supplementary Data: Combined collider constraints on neutralinos and charginos

The GAMBIT Collaboration

Supplementary Data

Combined collider constraints on neutralinos and charginos.

The files in this record contain data for the EW MSSM model considered in the [GAMBIT](#) paper on constraints on electroweakinos.

Preview

Supplementary Data

Combined collider constraints on neutralinos and charginos.

The files in this record contain data for the EW MSSM model considered in the [GAMBIT](#) paper on constraints on electroweakinos.

The files consist of

- A number of YAML files corresponding to different sets of sampling parameters and/or priors
- StandardModel_SLHA2_defaults.yaml, a universal YAML fragment included from other YAML files
- A final hdf5 file, MSSMEW.hdf5, containing the combined results of all sampling runs with collider constraints with the following
 - 241794 samples
 - At least 4M Pythia events per point for the LHC likelihood calculation. (More for the highest-likelihood points.)
 - The dataset "MSSMEW/LogLike" contains the combined collider likelihood (LHC + LEP + Z/h invisible widths)
- A final hdf5 file, MSSMEW_DM.hdf5 from a postprocessed run including Dark Matter constraints, with

For every GAMBIT paper, see <https://gambit.hepforge.org/pubs>

Summary

- There are many motivations for new physics
- Testing models of new physics requires complicated statistical and computational machinery — GAMBIT
- There are many subtleties in model testing
- Many public GAMBIT results and many more on the way!

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