

and taking

$$\begin{aligned}
& C_{\mathfrak{J}_B}^{(0,0;AB^{-1})}(w) \times_w T_{\mathfrak{J}_B, \mathfrak{J}_C, \mathfrak{J}_D}(w, u, v) \\
&= (q; q)(p; p) \oint \frac{dw}{4\pi iw} \frac{\prod_{j=1}^8 \Gamma_e((qp)^{\frac{1}{2}} \frac{1}{t} a_j^{-1} w^{\pm 1})}{\Gamma(w^{\pm 2})} C_{\mathfrak{J}_B}^{(0,0;AB^{-1})}(w) T_{\mathfrak{J}_B, \mathfrak{J}_C, \mathfrak{J}_D}(w, u, v) \\
&= (q; q)^4 (p; p)^4 \oint \frac{dw}{4\pi iw} \frac{\prod_{j=1}^8 \Gamma_e((qp)^{\frac{1}{2}} \frac{1}{t} a_j^{-1} w^{\pm 1})}{\Gamma(w^{\pm 2})} \Gamma_e(pqt^4) \prod_{j \neq i} \Gamma_e\left(\frac{pqt^2}{a_i a_j}\right) 0 \prod_{j=1}^8 \Gamma_e((pq)^{\frac{1}{2}} t a_j w^{\pm 1}) \\
&\quad \times \Gamma_e\left(\frac{(pq)^{\frac{1}{2}} w^{\pm 1}}{t a_i}\right) \Gamma_e\left(\frac{a_i w^{\pm 1}}{(pq)^{\frac{1}{2}} t^3}\right) \Gamma_e((qp)^{\frac{1}{2}} t (B^{-1} A)^{\pm 1} w^{\pm 1}) \Gamma_e\left(\frac{qp}{t^2}\right) \\
&\quad \times \oint \frac{dy}{4\pi iy} \frac{\Gamma_e\left(\frac{(pq)^{\frac{1}{2}}}{t^2} (AB^{-1})^{\pm 1} y^{\pm 1}\right)}{\Gamma_e(y^{\pm 2})} \Gamma_e(ty^{\pm 1} w^{\pm 1}) \oint \frac{dw_1}{4\pi iw_1} \oint \frac{dw_2}{4\pi iw_2} \frac{\Gamma_e\left(\frac{(pq)^{\frac{1}{2}}}{t^2} w_1^{\pm 1} w_2^{\pm 1}\right)}{\Gamma_e(w_2^{\pm 2}) \Gamma_e(w_1^{\pm 2})} \\
&\quad \times \Gamma_e((qp)^{\frac{1}{4}} t A^{\frac{1}{2}} B^{-\frac{1}{2}} y^{\frac{1}{2}} w_1^{\pm 1} u^{\pm 1}) \Gamma_e((qp)^{\frac{1}{4}} A^{\frac{1}{2}} B^{\frac{1}{2}} y^{-\frac{1}{2}} w_1^{\pm 1} D^{\pm 1}) \\
&\quad \times \Gamma_e((qp)^{\frac{1}{4}} t A^{-\frac{1}{2}} B^{\frac{1}{2}} y^{-\frac{1}{2}} w_2^{\pm 1} u^{\pm 1}) \Gamma_e((qp)^{\frac{1}{4}} A^{-\frac{1}{2}} B^{-\frac{1}{2}} y^{\frac{1}{2}} D^{\pm 1} w_2^{\pm 1}) \\
&\quad \times \Gamma_e((qp)^{\frac{1}{4}} t A^{-\frac{1}{2}} B^{\frac{1}{2}} y^{\frac{1}{2}} w_1^{\pm 1} v^{\pm 1}) \Gamma_e((qp)^{\frac{1}{4}} A^{-\frac{1}{2}} B^{-\frac{1}{2}} y^{-\frac{1}{2}} C^{\pm 1} w_1^{\pm 1}) \\
&\quad \times \Gamma_e((qp)^{\frac{1}{4}} t A^{\frac{1}{2}} B^{-\frac{1}{2}} y^{-\frac{1}{2}} w_2^{\pm 1} v^{\pm 1}) \Gamma_e((qp)^{\frac{1}{4}} A^{\frac{1}{2}} B^{\frac{1}{2}} y^{\frac{1}{2}} w_2^{\pm 1} C^{\pm 1}).
\end{aligned}$$

Plugging in the values of a_j from where $a_i = AB^{-1}$ and using the identity $\Gamma_e\left(\frac{pq}{z}\right) \Gamma_e(z) = 1$ we get

$$\begin{aligned}
& (q; q)^4 (p; p)^4 \oint \frac{dw}{4\pi iw} \frac{1}{\Gamma(w^{\pm 2})} \Gamma_e(pqt^4) \Gamma_e(pqt^2) \Gamma_e(pqt^2 B^2) \Gamma_e(pqt^2 A^{-2}) \\
& \times \Gamma_e(pqt^2 A^{-1} B C^{\pm 1} D^{\pm 1}) \Gamma_e\left(\frac{AB^{-1} w^{\pm 1}}{(pq)^{\frac{1}{2}} t^3}\right) \Gamma_e((qp)^{\frac{1}{2}} t A^{-1} B w^{\pm 1}) \Gamma_e\left(\frac{qp}{t^2}\right) \\
& \quad \times \oint \frac{dy}{4\pi iy} \frac{\Gamma_e\left(\frac{(pq)^{\frac{1}{2}}}{t^2} (AB^{-1})^{\pm 1} y^{\pm 1}\right)}{\Gamma_e(y^{\pm 2})} \Gamma_e(ty^{\pm 1} w^{\pm 1}) \\
& \quad \times \oint \frac{dw_1}{4\pi iw_1} \oint \frac{dw_2}{4\pi iw_2} \frac{\Gamma_e\left(\frac{(pq)^{\frac{1}{2}}}{t^2} w_1^{\pm 1} w_2^{\pm 1}\right)}{\Gamma_e(w_2^{\pm 2}) \Gamma_e(w_1^{\pm 2})} \Gamma_e((qp)^{\frac{1}{4}} t A^{\frac{1}{2}} B^{-\frac{1}{2}} y^{\frac{1}{2}} w_1^{\pm 1} u^{\pm 1}) \\
& \quad \times \Gamma_e((qp)^{\frac{1}{4}} A^{\frac{1}{2}} B^{\frac{1}{2}} y^{-\frac{1}{2}} w_1^{\pm 1} D^{\pm 1}) \Gamma_e((qp)^{\frac{1}{4}} t A^{-\frac{1}{2}} B^{\frac{1}{2}} y^{-\frac{1}{2}} w_2^{\pm 1} u^{\pm 1}) \\
& \quad \times \Gamma_e((qp)^{\frac{1}{4}} A^{-\frac{1}{2}} B^{-\frac{1}{2}} y^{\frac{1}{2}} D^{\pm 1} w_2^{\pm 1}) \Gamma_e((qp)^{\frac{1}{4}} t A^{-\frac{1}{2}} B^{\frac{1}{2}} y^{\frac{1}{2}} w_1^{\pm 1} v^{\pm 1}) \\
& \quad \times \Gamma_e((qp)^{\frac{1}{4}} A^{-\frac{1}{2}} B^{-\frac{1}{2}} y^{-\frac{1}{2}} C^{\pm 1} w_1^{\pm 1}) \Gamma_e((qp)^{\frac{1}{4}} t A^{\frac{1}{2}} B^{-\frac{1}{2}} y^{-\frac{1}{2}} w_2^{\pm 1} v^{\pm 1}) \\
& \quad \times \Gamma_e((qp)^{\frac{1}{4}} A^{\frac{1}{2}} B^{\frac{1}{2}} y^{\frac{1}{2}} w_2^{\pm 1} C^{\pm 1}).
\end{aligned}$$