

## Homework 6: Counting

1. 38 Computer Science (including joints), 23 Mathematics (including joints), 7 joint majors?
  - a.  $38 + 23 - 7 = \mathbf{54 \text{ students}}$
  - b. The joint majors are double counted, so subtract 7 students to account for joint majors
2. Number of possible initials if someone has at least 2 but no more than 5 initials
  - a. Assuming repeat characters are allowed
  - b. If 2 initials, there are  $26^2$  possibilities
  - c. If 3 initials, there are  $26^3$  possibilities
  - d. If 4 initials, there are  $26^4$  possibilities
  - e. If 5 initials, there are  $26^5$  possibilities
  - f. Add all possibilities:  $26^2 + 26^3 + 26^4 + 26^5 = \mathbf{12356604 \text{ possible initials}}$
3. Boolean function of  $n$  variables returns true or false, where  $b_i$  is true or false. Number of distinct functions with  $n$  boolean variables?
  - a. Each boolean variable can take on two possible values, and there are  $n$  of them
  - b. Therefore, number of distinct functions with  $n$  boolean variables is  $2^n$ .