

Homework #1

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By

Andrew Hutzal (915841776)

1) Find instruction count, CPI, and clocks

A)

Instruction	Count	CPI	Clocks
Or \$16,\$16,\$0	1	1	1
Lw \$21, (\$20)	10	3	30
Loop: Lw \$19,(\$18)	10	3	30
Add \$21,\$21,\$19	10	1	10
Addi \$16,\$16,1	10	3	30
Addi \$18,\$18,4	10	1	10
Slti \$17,\$16,10	10	1	10
Bne \$17,\$0,loop	10	1	10
Sw \$21,(\$20)	10	2	20
Sum of Count, CPI, and Clocks	81	16	151

B1) On CPU_base with the given values, It will take the program exactly 151 clock cycles to be executed.

B2) Calculating the number of cycles it takes for this code fragment to execute on CPU_base is exactly 81.

2) Recreating problem 1...

Instruction	Count	CPI	Clocks
Or \$16,\$16,\$0	1	1	1
Lw \$21, (\$20)	1	3	3
Loop: Lw \$19,(\$18)	10	3	30
Add \$21,\$21,\$19	10	1	10
Addi \$16,\$16,1	10	1	10
Addi \$18,\$18,4	10	1	10
Slti \$17,\$16,10	10	1	10
Bne \$17,\$0,loop	10	2	20
Sw \$21,(\$20)	1	3	3
Sum of Count, CPI, and Clocks	63	16	97

We now have a count of 63, CPI of 16, and Clocks of 97.

157/97, there is a 1.56 speed up in the program time which is pretty substantial.

3) Exercise 1.5 on page 55

1.5 [4] <§1.6> Consider three different processors P1, P2, and P3 executing the same instruction set. P1 has a 3 GHz clock rate and a CPI of 1.5. P2 has a 2.5 GHz clock rate and a CPI of 1.0. P3 has a 4.0 GHz clock rate and has a CPI of 2.2.

- a. Which processor has the highest performance expressed in instructions per second?

Work)

$$x = \frac{\text{speed}}{\text{CPI}}$$

- 1) $P1 = (3 \times 10^9) / 1.5 = 2.0 \times 10^9$
 2) $P2 = (2.5 \times 10^9) / 1 = 2.5 \times 10^9$
 3) $P3 = (4.0 \times 10^9) / 2.2 = 1.8 \times 10^9$

Answer)

And so we know that P2 has the highest performance expressed in instructions per second.

- b. If the processors each execute a program in 10 seconds, find the number of cycles and the number of instructions.

Work / Answer)

$$\begin{aligned} \text{Instructions for ten sec} &= \text{Part A} \times 10 \\ \text{Cycles for ten sec} &= \text{Speed} \times 10 \end{aligned}$$

Instructions for ten sec

- $P1 = (3 \times 10^9 \times 10) = 3 \times 10^{10}$
 $P2 = (2.5 \times 10^9 \times 10) = 2.5 \times 10^{10}$
 $P3 = (4.0 \times 10^9 \times 10) = 4.0 \times 10^{10}$

Cycles for ten sec

- $P1 = (2.0 \times 10^9 \times 10) = 2 \times 10^{10}$
 $P2 = (2.5 \times 10^9 \times 10) = 2.5 \times 10^{10}$
 $P3 = (1.8 \times 10^9 \times 10) = 1.8 \times 10^{10}$

- c. We are trying to reduce the execution time by 30% but this leads to an increase of 20% in the CPI. What clock rate should we have to get this time reduction?

Work)

$$(\text{Execution time} \times 0.7 = (\# \text{ of instructions} \times \text{CPI} \times 1.2) / (\text{Clock rate}))$$

$$\text{Clock rate} = \text{Clock rate} \times 1.2 / 0.7 = 1.71 \times \text{Clock rate}$$

Apply this following eq to find the answers...

Answer)

$$P1: 3 \text{ Ghz} \times 1.71 = 5.13 \text{ Ghz}$$

$$P2: 2.5 \text{ Ghz} \times 1.71 = 4.27 \text{ Ghz}$$

$$P3: 4 \text{ Ghz} \times 1.71 = 6.84 \text{ Ghz}$$

4)

1.6 [20] Consider two different implementations of the same instruction set architecture. The instructions can be divided into four classes according to their CPI (class A, B, C, and D). P1 with a clock rate of 2.5 GHz and CPIs of 1, 2, 3, and 3, and P2 with a clock rate of 3 GHz and CPIs of 2, 2, 2, and 2. Given a program with a dynamic instruction count of 1.0E6 instructions divided into classes as follows: 10% class A, 20% class B, 50% class C, and 20% class D, which implementation is faster?

- a. What is the global CPI for each implementation?
Work)

$$\frac{\text{clock cycles}}{\text{total \# of instructions}}$$

$$(10^6 \times ((1 \times 1) + (2 \times 2) + (3 \times 5) + (3 \times 2))) / 10^6 = 2.6$$

$$\text{Global CPI P1} = 2.6$$

$$(10^6 \times ((2 \times 1) + (2 \times 2) + (2 \times 5) + (2 \times 2))) / 10^6 = 2$$

$$\text{Global CPI P2} = 2$$

- b. Find the clock cycles required in both cases.

$$\text{P1: } (10^6 \times ((1 \times 1) + (2 \times 2) + (3 \times 5) + (3 \times 2))) = 2.6 \times 10^6$$

$$\text{P2: } (10^6 \times ((2 \times 1) + (2 \times 2) + (2 \times 5) + (2 \times 2))) = 2 \times 10^6$$

5)

The Pentium 4 Prescott processor, released in 2004, had a clock rate of 3.6 GHz and voltage of 1.25 V. Assume that, on average, it consumed 10 W of static power and 90 W of dynamic power.

The Core i5 Ivy Bridge, released in 2012, had a clock rate of 3.4 GHz and voltage of 0.9 V. Assume that, on average, it consumed 30 W of static power and 40 W of dynamic power.

5a)

Find for each processor the average capacitive loads.

$$\text{Cap Load} = \frac{2 \times \text{Power}}{\text{Freq} \times \text{Volt}^2}$$

$$\frac{2 \times 90}{3.6 \times 10^9 \times 1.25^2} = 2.9 \times 10^{-8}$$

5b)

[5] <§1.7> Find the percentage of the total dissipated power comprised by static power and the ratio of static power to dynamic power for each technology.

First processor:

$$\text{Total Power} = \text{Static Power} + \text{Dynamic Power} = 10 + 90 = 100 \text{ Watts}$$

$$\% \text{ of dissipation} = \frac{10}{100} = 10\%$$

$$\text{Ratio} = \frac{10}{90} = \frac{1}{9}$$

Second processor:

$$\text{Total power} = 30 + 40 = 70W$$

$$\% \text{ of disappation} = \frac{30}{70} = 42.8\%$$

$$\text{Ratio} = \frac{30}{40} = \frac{3}{4}$$

5c)

[15] <§1.7> If the total dissipated power is to be reduced by 10%, how much should the voltage be reduced to maintain the same leakage current? Note: power is defi ned as the product of voltage and current.

First processor

$$P = V * C$$

$$C = \frac{P}{V}$$

$$\frac{100}{1.25} = 80$$

$$\text{And so power} = 100 - \left(\frac{10}{100} \times 100 \right) = 100 - 10 = 90$$

$$\text{Account for leakage ... } P = V \times C$$

$$V = \frac{P}{C}$$

$$\frac{90}{\frac{100}{1.25}} = 1.125$$

Check for errors:

$$\text{Reduction} = \frac{1.25 - 1.125}{1.25} * 100 = 10\%$$

Second Processor

$$C = \frac{P}{V}$$

$$\text{Current} = \frac{70}{0.9}$$

$$\text{Reduced power} = 70 - \left(\frac{10}{100} \times 70 \right) = 70 - 7 = 63$$

$$\text{Leakage} = \text{Voltage} = \frac{P}{V}$$

$$\frac{63}{\frac{70}{0.9}} = 0.81$$

Check for errors:

$$\text{Reduction} = \frac{0.91 - 0.81}{0.9} \times 100 = 10\%$$

6)

Assume a 15 cm diameter wafer has a cost of 12, contains 84 dies, and has 0.020 defects/cm². Assume a 20 cm diameter wafer has a cost of 15, contains 100 dies, and has 0.031 defects/cm².

6a)

Find the yield for both wafers.

Wafer 1:

$$\text{area} = \pi \times \left(\frac{15}{2} \right)^2 = 176.625 \text{ cm}^2$$

$$\text{defects} = \text{area} \times \text{defects per unit} = 176.625 \times 0.02 = 3.53$$

$$\text{good dies in Wafer 1} = \text{Total dies} - \text{defect dies} = 84 - 3.53 = 80.47$$

$$\text{Wafer 1 yield} = \frac{80.47}{84} = 95.8\%$$

Wafer 2:

$$\text{area} = \pi \times \left(\frac{20}{2} \right)^2 = 314 \text{ cm}^2$$

$$\text{defects} = \text{area} \times \text{defects per unit} = 314 \times 0.031 = 9.74$$

$$\text{good dies in wafer 2} = \text{Total dies} - \text{defect dies} = 100 - 9.74 = 90.26$$

$$\text{Wafer 2 yield} = \frac{90.26}{100} = 90.26\%$$

6b)

Find the cost per die for both wafers.

Cost per die:

$$\text{Cost per die for wafer 1} = \frac{\text{Total cost}}{\text{Number of good dies}} = \frac{12}{80.47} = 0.15$$

$$\text{Cost per die for wafer 2} = \frac{\text{Total cost}}{\text{Number of good dies}} = \frac{15}{90.26} = 0.17$$

6c)

If the number of dies per wafer is increased by 10% and the defects per area unit increases by 15%, find the die area and yield.

Wafer 1

$$8.4 \times 1.1 = 9.24 \text{ dies per wafer}$$

$$0.02 \times 1.15 = 0.023 \text{ Defects}$$

$$\text{area} * \text{defects} = 176.625 \times 0.023 = 4.06$$

$$\text{good dies in Wafer 1} = \text{Total dies} - \text{defect dies} = 9.24 - 4.06 = 5.18$$

$$\text{Wafer 1 yield} = \frac{5.18}{9.24} = 56.1\%$$

$$\text{Wafer 1 die area} = \frac{176.625}{9.24} = 19.11 \text{ cm}^2$$

Wafer 2

$$\text{Wafer 2} = 100 \times 1.1 = 110 \text{ dies per wafer}$$

$$\text{Defects percentage} = 0.031 \times 1.15 = 0.036$$

$$\text{Defects} = 110 \times 0.036 = 3.96$$

$$\text{Good dies in Wafer 2} = \text{Total dies} - \text{defect dies} = 110 - 3.96 = 106.04$$

$$\text{Wafer 2 yield} = \frac{106.04}{110} = 96.4\%$$

$$\text{Wafer 2 die area} = \frac{314}{110} = 2.85 \text{ cm}^2$$

6d)

Assume a fabrication process improves the yield from 0.92 to 0.95. Find the defects per area unit for each version of the technology given a die area of 200 mm².

$$0.92 \text{ to } 0.95 = 103.3\% \text{ increase}$$

Wafer 1

$$\text{Wafer 1 yield} = 95.6 \times 1.033 = 98.75$$

$$\text{Wafer 1 die area} = \frac{176.62}{2} = 88.3$$

$$\text{Wafer 1 good dies} = \text{Yield} \times \text{die area} = .9875 \times 88.36 = 87.26$$

$$\text{Wafer 1 defects} = \text{Total dies} - \text{good dies} = 88.3 - 87.26 = 1.04$$

Wafer 2

$$\text{Wafer 2 yield} = 89.8 \times 1.033 = 92.78$$

$$\text{Wafer 2 die area} = \frac{176.62}{2} = 88.3$$

$$\text{Wafer 2 good dies} = .9278 \times 157 = 145$$

$$\text{Wafer 2 defects} = 157 - 145.74 = 11.26$$