

## Readings

- [Grauman](#) 3.1, 3.2 Intro, Detection of Interest Points & Regions
- [Klette](#) 9.1 Invariance, Features and Sets of Features
- [Szeliski](#) 4.1, 4.1.1 Points & Patches, Feature Detectors

## Summary

### Motivation

- How can we stitch two images together?
  - matching the parts which are the same on both image
  - aligning the images based on the matches

### Image Matching

- three step process: finding key points, computing descriptors, matching descriptors
- “features”: catch-all term for key points + descriptors
- Good local features are repeatable yet distinct, efficient to compute and local in extent

### Harris Corner Detection

- A local area is distinct if it has a high SSD error wrt surrounding; this occurs at “corners”
- Computing SSD is inefficient; instead, estimate indirectly via  $H$ , the second moment matrix
- Corners are found where eigenvalues of  $H$  matrix are both sufficiently large
- For efficiency, approximate with a response function  $R = \det(H) - k \text{trace}^2(H)$ , which does not require explicit eigenvalue decomposition
- Areas with high  $R$  are likely corners – localize to single pixels via non-maximum suppression

### Invariances

- Invariance vs. equivariance
- Harris corners are equivariant to geometric transformations such as translation, rotation, semi-invariant to photometric transformations and not invariant to scaling
- Can use automatic scale selection to find keypoints by sweeping over a range of scales and searching for the scale with a local maximum
- Laplacian of Gaussian (LoG) is a scale-sensitive key point detector which detects “blobs”

## FAQs

**Q:** Is the H-matrix positive semi-definite by definition?

A: Yes. H by definition is a positive semi-definite matrix because  $\begin{bmatrix} u & v \end{bmatrix} H \begin{bmatrix} u \\ v \end{bmatrix} = E$  where E is the SSD error and the SSD error is  $\geq 0$ . This means that we will always have non-negative eigenvalues. Actually, the only way for  $E = 0$  for a local patch is a perfectly constant / flat region but this does not occur in real images.

**Q:** In slide 18, to find the corner(s) in an image, we will have one  $E(u,v)$  value per window  $W$ , which we will know if a corner exists in a  $W$  with the H matrix. The  $u$  and  $v$  used for all the  $W$  are the same right?

A: We evaluate each window to see if it contains a corner or not. The window is located at  $x,y$ . To find out if that window has a corner, we use image content within that window, denoted by  $w(x,y)$  and shifting it around (in theory). The shifting is indexed by  $(u,v)$ . In that sense we use the same (amount of) shifts for each window. In practice, we don't do any actual shifting, we simply compute the H matrix associated with the pixel at  $x,y$ , from which we will evaluate if a corner exists there or not.

**Q:** Is the visualization in slide 19 illustrating the computation of  $E(u,v)$  for the various  $W$  in an image? Is the  $u,v$  used in this slide showing the shift in  $W$ ?

A. No the animations were illustrating the  $E(u,v)$  for only 1  $w$ .

**Q:** Why is DoG approximation of LoG cheaper?

A: The LoG is not a separable kernel so it needs to be applied in 2D whereas Gaussians (and therefore DoG) is a separable kernel that can be applied twice in 1D. Therefore, we can apply a DoG as 4 1D kernels rather than apply the LoG as a single 2D kernel.

Where do we gain then? Suppose the kernel dimensions are  $m \times m$ . Any time  $m \times m > 4 \times m$ , so any time our kernel dimension  $m > 4$ .

More details here: <https://dsp.stackexchange.com/questions/51971/how-is-laplacian-of-gaussian-log-implemented-as-four-1d-convolutions/54279#54279>

**Q:** Is computing SSD equivalent to doing auto-correlation?

A: The two are not equivalent. If you expand the original definition,

$$\begin{aligned} E(u, v) &= \sum_{x,y} [I(x+u, y+v) - I(x, y)]^2 \\ &= \sum_{x,y} [I^2(x+u, y+v) - I(x+u, y+v)I(x, y) + I^2(x, y)] \\ &= K_1 - \sum_{x,y} [I(x+u, y+v)I(x, y)] + K_2 \end{aligned}$$

Only the second term would be the autocorrelation.