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1 Basic Concepts

1.1 Probability and Relative Frequency

$$P(A) = \frac{N(A)}{N} \tag{1}$$

where N is the total number of outcomes of the experiment and $N(A)$ is the number of outcomes leading to the occurrence of event A