Homework 5

```
In [180... #imports
    import numpy as np
    import pandas as pd
    import matplotlib.pyplot as plt

In [181... wage_raw = pd.read_csv('Wage.csv')
```

1. K-Means

- 1. Instead of just having an indicator for job class we add an indicator for each of the categorical variables. The categorical variables are:
- sex
- maritl
- race
- education
- region
- jobclass
- health
- health_ins

```
In [214... cat_var = ['sex', 'maritl', 'race', 'education', 'region', 'jobclass', 'health', 'h
    wage = pd.get_dummies(wage_raw, columns=cat_var, drop_first=True)
In [102... wage
```

	yea	r age	logwage	wage	maritl_2. Married	maritl_3. Widowed	maritl_4. Divorced	maritl_5. Separated	race_2. Black
	0 200	6 18	4.318063	75.043154	False	False	False	False	False
	1 200	4 24	4.255273	70.476020	False	False	False	False	False
	2 200	3 45	4.875061	130.982177	True	False	False	False	False
	3 200	3 43	5.041393	154.685293	True	False	False	False	False
	4 200	5 50	4.318063	75.043154	False	False	True	False	False
	 .								•••
299	95 200	8 44	5.041393	154.685293	True	False	False	False	False
299	96 200	7 30	4.602060	99.689464	True	False	False	False	False
299	97 200	5 27	4.193125	66.229408	True	False	False	False	True
299	98 200	5 27	4.477121	87.981033	False	False	False	False	False
299	99 200	9 55	4.505150	90.481913	False	False	False	True	False

3000 rows × 18 columns

2. Code

```
In [215...
rng = np.random.default_rng()
train_idx = rng.binomial(1, 0.8, size = wage.shape[0]).astype(bool)
wage_train = wage[train_idx]
wage_test = wage[~train_idx]
```

3. We assume that everyone has completed middle school for a minimum of 9 years of schooling. If someone is a High School Grad that counts for 4 more years. If they have some college, we assume that's an associate degree. The cases where someone drops out at 1 year or 3 years average out to 2 years (most of the time). Some college should count for 2 years. College grad counts for 4 years. Advanced degreees can be masters or phds or professional degrees. Masters usually are 2 years, and Phds are usually 5-6, but often take much longer. We assume it adds a bit more years of schooling, say 4 years on average.

```
# make education years column
education_years = 9 + wage['education_2. HS Grad'] * 4 + wage['education_3. Some Co
# make kmeans data_frame
```

```
wage_kmeans = pd.DataFrame({'jobclass': wage['jobclass_2. Information'], 'age': wag
# standardize
wage_kmeans[['age', 'education_years', 'logwage']] = (wage_kmeans[['age', 'educatio'])
# split
wage_kmeans_train = wage_kmeans[train_idx]
wage_kmeans_test = wage_kmeans[~train_idx]
wage_kmeans
```

Out[104...

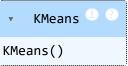
	jobclass	age	education_years	logwage
0	False	-2.115215	-1.888180	-0.954767
1	True	-1.595392	0.577880	-1.133275
2	False	0.223986	-0.038635	0.628727
3	True	0.050712	0.577880	1.101591
4	True	0.657171	-0.655150	-0.954767
•••				
2995	False	0.137349	-0.038635	1.101591
2996	False	-1.075570	-0.655150	-0.147391
2997	False	-1.335481	-1.888180	-1.309956
2998	False	-1.335481	-0.038635	-0.502580
2999	False	1.090356	-0.655150	-0.422897

3000 rows × 4 columns

5. Code

```
import sklearn.cluster
num_clusters = 8
kmeans_clf = sklearn.cluster.KMeans(n_clusters = num_clusters)
kmeans_clf.fit(wage_kmeans_train)
```

Out[105...



6. Predict

```
In [106...
kmeans_weights = np.zeros(num_clusters)
for i in range(num_clusters):
    kmeans_weights[i] = np.mean(wage_kmeans_train.iloc[kmeans_clf.labels_ == i]['jo
print(kmeans_weights)
```

```
[0.66666667 0.50743494 0.8 0.29299363 0.46285714 0.39732143 0.51923077 0.24096386]
```

7. Here is some code to investigate this:

As we can see, the first coordinate of each of the cluster centers (the part corresponding to the job) is exactly the fraction we calculated prior. This makes sense since each cluster center's should just be the mean of the group, otherwise the variance would increase.

8. Code

```
In [108...
kmeans_weights = kmeans_weights > 0.5
kmeans_preds_train = np.eye(num_clusters)[kmeans_clf.predict(wage_kmeans_train)] @
kmeans_err_train = np.mean(kmeans_preds_train != wage_kmeans_train['jobclass'])
print(f"The training error for the k-means classifier is {kmeans_err_train}")
```

The training error for the k-means classifier is 0.3831578947368421

9. Code

The test error for the k-means classifier is 0.384

2. Neural Networks

```
In [111...
          import torch
          import torch.nn as nn
          import torch.optim as optim
          import torch.functional as F
          import torch.utils.data as data
In [112...
          device = torch.accelerator.current_accelerator().type if torch.accelerator.is_avail
          print(f'Using device: {device}')
         Using device: cuda
In [113...
          class Net(nn.Module):
              def __init__(self):
                   super(Net, self).__init__()
                   self.linear_relu_logit_stack = nn.Sequential(
                      nn.Linear(3, 16),
                      nn.ReLU(),
                      nn.Linear(16, 16),
                      nn.ReLU(),
                      nn.Linear(16, 1),
                      nn.Sigmoid()
              def forward(self, x):
                   return self.linear relu logit stack(x)
In [114...
          model = Net().to(device)
          print(model)
         Net(
           (linear_relu_logit_stack): Sequential(
             (0): Linear(in_features=3, out_features=16, bias=True)
             (1): ReLU()
             (2): Linear(in_features=16, out_features=16, bias=True)
             (3): ReLU()
             (4): Linear(in_features=16, out_features=1, bias=True)
             (5): Sigmoid()
           )
         )
In [115...
         loss_fn = nn.BCELoss()
          optimizer = optim.Adam(model.parameters(), lr=10e-4)
          wage_nn_train = torch.tensor(wage_kmeans_train[['age', 'education_years', 'logwage'
In [116...
          jobclass_nn_train = torch.tensor(wage_kmeans_train['jobclass'].values, dtype=torch.
          jobclass_nn_train = jobclass_nn_train.view(-1, 1)
          wage_nn_test = torch.tensor(wage_kmeans_test[['age', 'education_years', 'logwage']]
          jobclass_nn_test = torch.tensor(wage_kmeans_test['jobclass'].values, dtype=torch.fl
          jobclass_nn_test = jobclass_nn_test.view(-1, 1)
          def train(X,y, model, loss_fn, optimizer):
In [150...
              model.train()
              for i in np.random.permutation(range(len(X))):
                  Xi, yi = X[i], y[i]
                  Xi, yi = Xi.to(device), yi.to(device)
                   # pred
```

```
pred = model(Xi)
                  loss = loss_fn(pred, yi)
                 # backprop
                 loss.backward()
                  optimizer.step()
                 optimizer.zero_grad()
                 # if i % 100 == 0:
                 # loss = loss.item()
                       print(f"loss: {loss:>7f} [{i:>5d}/{len(X)}]")
In [119... def test(X, y, model, loss_fn):
              model.eval()
              size = len(X)
              test_loss, correct = 0, 0
              with torch.no_grad():
                 for Xi, yi in zip(X, y):
                     Xi, yi = Xi.to(device), yi.to(device)
                     pred = model(Xi)
                     loss = loss_fn(pred, yi)
                     test_loss += loss.item()
                     correct += (pred.round() == yi).type(torch.float).item()
              test_loss /= size
              correct /= size
              print(f"Test Error: \n Accuracy: {(100*correct):>0.1f}%, Avg loss: {test_loss:>
In [120...
         epochs = 5
          for t in range(epochs):
              print(f"Epoch {t+1}\n----")
              train(wage_nn_train, jobclass_nn_train, model, loss_fn, optimizer)
              test(wage_nn_train, jobclass_nn_train, model, loss_fn)
```

loss: 0.812750 [0/2375] loss: 0.746969 [100/2375] loss: 0.719210 [200/2375] loss: 0.767752 [300/2375] loss: 0.660637 [400/2375] loss: 0.588416 [500/2375] loss: 0.458372 [600/2375] loss: 0.949831 [700/2375] loss: 0.394190 [800/2375] loss: 0.539203 [900/2375] loss: 0.386170 [1000/2375] loss: 0.609884 [1100/2375] loss: 0.383120 [1200/2375] loss: 0.563736 [1300/2375] loss: 0.398944 [1400/2375] loss: 0.876582 [1500/2375] loss: 0.573143 [1600/2375] loss: 0.538475 [1700/2375] loss: 0.820063 [1800/2375] loss: 0.761384 [1900/2375] loss: 0.695942 [2000/2375] loss: 0.564975 [2100/2375] loss: 0.765927 [2200/2375] loss: 0.652676 [2300/2375] Test Error:

Accuracy: 63.4%, Avg loss: 0.641555

Epoch 2

----loss: 0.210156 [0/2375] loss: 1.319807 [100/2375] loss: 0.639556 [200/2375] loss: 0.883472 [300/2375] loss: 0.550339 [400/2375] loss: 0.645365 [500/2375] loss: 0.297408 [600/2375] loss: 0.978406 [700/2375] loss: 0.312536 [800/2375] loss: 0.493559 [900/2375] loss: 0.265217 [1000/2375] loss: 0.656701 [1100/2375] loss: 0.341239 [1200/2375] loss: 0.505777 [1300/2375] loss: 0.353160 [1400/2375] loss: 0.948211 [1500/2375] loss: 0.579311 [1600/2375] loss: 0.542754 [1700/2375] loss: 0.892295 [1800/2375] loss: 0.833782 [1900/2375] loss: 0.703336 [2000/2375] loss: 0.573368 [2100/2375] loss: 0.643396 [2200/2375]

loss: 0.668942 [2300/2375]

Test Error:

Accuracy: 63.3%, Avg loss: 0.639839

Epoch 3

----loss: 0.197121 [0/2375] loss: 1.361679 [100/2375] loss: 0.602423 [200/2375] loss: 0.872241 [300/2375] loss: 0.527855 [400/2375] loss: 0.687093 [500/2375] loss: 0.291176 [600/2375] loss: 0.968406 [700/2375] loss: 0.314803 [800/2375] loss: 0.478695 [900/2375] loss: 0.256262 [1000/2375] loss: 0.670204 [1100/2375] loss: 0.338398 [1200/2375] loss: 0.477620 [1300/2375] loss: 0.352963 [1400/2375] loss: 0.971770 [1500/2375] loss: 0.587948 [1600/2375] loss: 0.553294 [1700/2375] loss: 0.931062 [1800/2375] loss: 0.866287 [1900/2375] loss: 0.728667 [2000/2375] loss: 0.576758 [2100/2375] loss: 0.640255 [2200/2375] loss: 0.661310 [2300/2375] Test Error:

Accuracy: 62.8%, Avg loss: 0.638866

Epoch 4

loss: 0.195810 [0/2375] loss: 1.353064 [100/2375] loss: 0.576642 [200/2375] loss: 0.875407 [300/2375] loss: 0.515771 [400/2375] loss: 0.709095 [500/2375] loss: 0.287706 [600/2375] loss: 0.964781 [700/2375] loss: 0.322479 [800/2375] loss: 0.477383 [900/2375] loss: 0.250386 [1000/2375] loss: 0.679712 [1100/2375] loss: 0.337413 [1200/2375] loss: 0.459359 [1300/2375] loss: 0.352589 [1400/2375] loss: 0.995823 [1500/2375] loss: 0.601121 [1600/2375] loss: 0.577461 [1700/2375] loss: 0.958010 [1800/2375] loss: 0.889349 [1900/2375] loss: 0.739539 [2000/2375] loss: 0.584371 [2100/2375] loss: 0.627556 [2200/2375]

```
loss: 0.667797 [ 2300/2375]
         Test Error:
         Accuracy: 63.1%, Avg loss: 0.638044
         Epoch 5
         -----
         loss: 0.195758 [ 0/2375]
         loss: 1.338283 [ 100/2375]
         loss: 0.564895 [ 200/2375]
         loss: 0.876744 [ 300/2375]
         loss: 0.506485 [ 400/2375]
         loss: 0.718385 [ 500/2375]
         loss: 0.284253 [ 600/2375]
         loss: 0.968909 [ 700/2375]
         loss: 0.323961 [ 800/2375]
        loss: 0.477185 [ 900/2375]
         loss: 0.249726 [ 1000/2375]
         loss: 0.676968 [ 1100/2375]
        loss: 0.332026 [ 1200/2375]
         loss: 0.453932 [ 1300/2375]
        loss: 0.347524 [ 1400/2375]
         loss: 1.008308 [ 1500/2375]
         loss: 0.610335 [ 1600/2375]
         loss: 0.592940 [ 1700/2375]
         loss: 0.972017 [ 1800/2375]
         loss: 0.903162 [ 1900/2375]
         loss: 0.749905 [ 2000/2375]
         loss: 0.587641 [ 2100/2375]
         loss: 0.618064 [ 2200/2375]
         loss: 0.675766 [ 2300/2375]
         Test Error:
         Accuracy: 63.0%, Avg loss: 0.637513
            2. Code
In [121...
         model.eval()
          wage_nn_train_err = ((model(wage_nn_train) > 0.5) == jobclass_nn_train).sum().item(
          print(f"The training error for the neural network is {1 - wage_nn_train_err}")
         The training error for the neural network is 0.3701052631578947
            3. Code
In [122...
          model.eval()
          wage_nn_test_err = ((model(wage_nn_test) > 0.5) == jobclass_nn_test).sum().item()/1
          print(f"The test error for the neural network is {1 - wage_nn_test_err}")
```

The test error for the neural network is 0.35840000000000005

3. Regression Trees

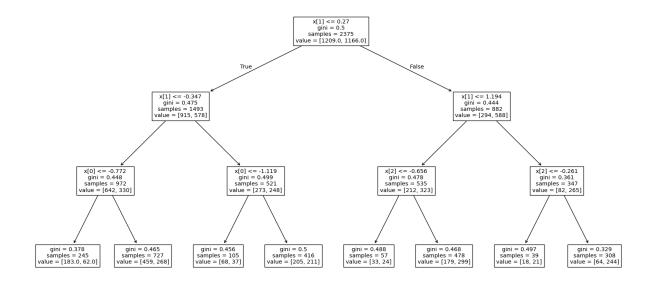
1. Code

```
In [123...
wage_dt_train = wage_kmeans_train[['age', 'education_years', 'logwage']]
jobclass_dt_train = wage_kmeans_train['jobclass']
wage_dt_test = wage_kmeans_test[['age', 'education_years', 'logwage']]
jobclass_dt_test = wage_kmeans_test['jobclass']
```

import sklearn.tree
dt_clf = sklearn.tree.DecisionTreeClassifier(max_depth = 3)
dt_clf.fit(wage_dt_train, jobclass_dt_train)

2. Code

```
In [125... plt.figure(figsize=(20,10))
    sklearn.tree.plot_tree(dt_clf)
    plt.show()
```



3. Code

```
In [126... wage_dt_train_err = 1 - dt_clf.score(wage_dt_train, jobclass_dt_train)
print(f"The training error for the decision tree is {wage_dt_train_err}")
```

The training error for the decision tree is 0.36084210526315785

```
In [127... wage_dt_test_err = 1 - dt_clf.score(wage_dt_test, jobclass_dt_test)
    print(f"The test error for the decision tree is {wage_dt_test_err}")
```

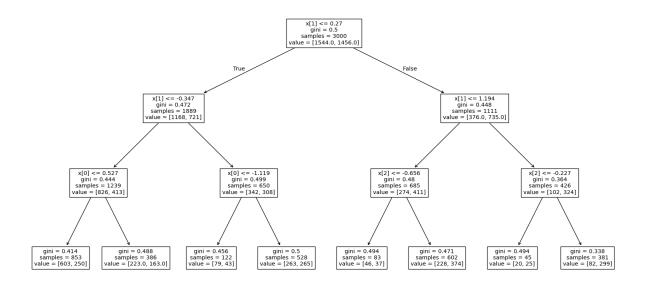
The test error for the decision tree is 0.36639999999999999

5. Code

```
In [128...
wage_dt = wage_kmeans[['age', 'education_years', 'logwage']]
jobclass_dt = wage_kmeans['jobclass']
dt_full_clf = sklearn.tree.DecisionTreeClassifier(max_depth = 3)
dt_full_clf.fit(wage_dt, jobclass_dt)
```

6. Code

```
In [129... plt.figure(figsize=(20,10))
    sklearn.tree.plot_tree(dt_full_clf)
    plt.show()
```



7. Code

```
In [130... wage_dt_full_train_err = 1 - dt_full_clf.score(wage_dt, jobclass_dt)
print(f"The error on the training set for the decision tree is {wage_dt_full_train_
```

The error on the training set for the decision tree is 0.362

```
In [131... wage_dt_full_test_err = 1 - dt_full_clf.score(wage_dt_test, jobclass_dt_test)
print(f"The error on the test set for the decision tree is {wage_dt_full_test_err}"
```

The error on the test set for the decision tree is 0.3663999999999999

4. Compare All Methods

1. Code

```
results = pd.DataFrame({
    'kmeans': [kmeans_err_train, kmeans_err_test],
    'neural_network': [1 - wage_nn_train_err, 1 - wage_nn_test_err],
    'decision_tree': [wage_dt_train_err, wage_dt_test_err],
    'decision_tree_full': [wage_dt_full_train_err, wage_dt_full_test_err]
}, index = ['train', 'test'])
results
```

Out[133... kmeans neural_network decision_tree decision_tree_full

train	0.383158	0.370105	0.360842	0.3620
test	0.384000	0.358400	0.366400	0.3664

- 2. All of the methods performed incredibly close to each other. They were all within 3e-2 of each other. The neural network did the best, which was expected, but all methods performed well. In theory, we should have expected the full decision tree to perform better than the standard decision tree, however, we only had 3 features, with max depth of 8, so the decision tree was quite constrained. The neural network performed the best, but not by as well as I expected. I chalk this up to there not being enough data and not using enough features.
- 3. (Optional) We are going to train a neural net with one more hidden layer and more intermediary nodes. We are also going to cross validate for the learning rate in the SGD optimizer and we are going to use the entire data set with the one-hot encoding.

```
In [ ]: wage = wage.astype('float64')
    wage_train = wage_train.astype('float64')
    wage_test = wage_test.astype('float64')
    wage
```

```
nn.ReLU(),
                      nn.Linear(32, 32),
                      nn.ReLU(),
                      nn.Linear(32, 1),
                      nn.Sigmoid()
              def forward(self, x):
                  return self.linear_relu_logit_stack(x)
          model = Net().to(device)
          print(model)
         Net(
           (linear_relu_logit_stack): Sequential(
             (0): Linear(in_features=17, out_features=32, bias=True)
             (1): ReLU()
             (2): Linear(in_features=32, out_features=32, bias=True)
             (3): ReLU()
             (4): Linear(in_features=32, out_features=32, bias=True)
             (5): ReLU()
             (6): Linear(in_features=32, out_features=1, bias=True)
            (7): Sigmoid()
           )
         )
In [145...
          wage_nn_train = torch.tensor(wage_train.drop(columns = 'jobclass_2. Information').v
          jobclass_nn_train = torch.tensor(wage_train['jobclass_2. Information'].values, dtyp
          jobclass_nn_train = jobclass_nn_train.view(-1, 1)
          wage_nn_test = torch.tensor(wage_test.drop(columns = 'jobclass_2. Information').val
          jobclass_nn_test = torch.tensor(wage_test['jobclass_2. Information'].values, dtype=
          jobclass_nn_test = jobclass_nn_test.view(-1, 1)
          optimizer = optim.Adam(model.parameters(), lr=10e-5)
In [151...
          epochs = 25
In [152... for t in range(epochs):
              print(f"Epoch {t+1}\n----")
              train(wage_nn_train, jobclass_nn_train, model, loss_fn, optimizer)
              test(wage_nn_train, jobclass_nn_train, model, loss_fn)
```

Epoch 1
Test Error: Accuracy: 57.2%, Avg loss: 0.677338
Epoch 2
Test Error: Accuracy: 57.1%, Avg loss: 0.673603
Epoch 3
Test Error: Accuracy: 59.4%, Avg loss: 0.667718
Epoch 4
Test Error: Accuracy: 57.2%, Avg loss: 0.672373
Epoch 5
Test Error: Accuracy: 59.5%, Avg loss: 0.668015
Epoch 6
Test Error: Accuracy: 56.8%, Avg loss: 0.676829
Epoch 7
Test Error: Accuracy: 59.7%, Avg loss: 0.668202
Epoch 8
Test Error: Accuracy: 57.7%, Avg loss: 0.668597
Epoch 9
Test Error: Accuracy: 57.5%, Avg loss: 0.670710
Epoch 10
Test Error: Accuracy: 59.6%, Avg loss: 0.667262
Epoch 11
Test Error: Accuracy: 57.4%, Avg loss: 0.673629

Epoch 12

Test Error: Accuracy: 59.2%, Avg loss: 0.668041
Epoch 13
Test Error: Accuracy: 59.7%, Avg loss: 0.671024
Epoch 14
Test Error: Accuracy: 59.5%, Avg loss: 0.666076
Epoch 15
Test Error: Accuracy: 58.1%, Avg loss: 0.668596
Epoch 16
Test Error: Accuracy: 54.1%, Avg loss: 0.718041
Epoch 17
Test Error: Accuracy: 58.5%, Avg loss: 0.667357
Epoch 18
Test Error: Accuracy: 56.8%, Avg loss: 0.675292
Epoch 19
Test Error: Accuracy: 60.0%, Avg loss: 0.665352
Epoch 20
Test Error: Accuracy: 58.4%, Avg loss: 0.670422
Epoch 21
Test Error: Accuracy: 56.4%, Avg loss: 0.676622
Epoch 22
Test Error: Accuracy: 60.3%, Avg loss: 0.664770
Epoch 23

```
Test Error:
    Accuracy: 59.6%, Avg loss: 0.664290

Epoch 24
-----
Test Error:
    Accuracy: 59.4%, Avg loss: 0.664646

Epoch 25
----
Test Error:
    Accuracy: 56.8%, Avg loss: 0.675412
```

```
In [153...
model.eval()
wage_nn_train_err = ((model(wage_nn_train) > 0.5) == jobclass_nn_train).sum().item(
print(f"The training error for the neural network is {1 - wage_nn_train_err}")
wage_nn_test_err = ((model(wage_nn_test) > 0.5) == jobclass_nn_test).sum().item()/l
print(f"The test error for the neural network is {1 - wage_nn_test_err}")
```

It's clear that our nn is suffering. We will drop wages because they are codependent with logwages. We also demean year and age, since only the relative age and years matter

```
In [216... # education_years = 9 + wage['education_2. HS Grad'] * 4 + wage['education_3. Some
# wage.drop(columns=['education_2. HS Grad', 'education_3. Some College', 'educatio
# wage['education_years'] = education_years
wage = wage.astype('float64')
wage = wage.drop(columns = 'wage')
wage['year'] = wage['year'] - wage['year'].min()
# wage['age'] = wage['age'] - wage['age'].min()
wage_train = wage[train_idx]
wage_test = wage[~train_idx]
wage
```

	year	age	logwage	maritl_2. Married	maritl_3. Widowed	maritl_4. Divorced	maritl_5. Separated	race_2. Black	race_3. Asian	rac O
0	3.0	18.0	4.318063	0.0	0.0	0.0	0.0	0.0	0.0	
1	1.0	24.0	4.255273	0.0	0.0	0.0	0.0	0.0	0.0	
2	0.0	45.0	4.875061	1.0	0.0	0.0	0.0	0.0	0.0	
3	0.0	43.0	5.041393	1.0	0.0	0.0	0.0	0.0	1.0	
4	2.0	50.0	4.318063	0.0	0.0	1.0	0.0	0.0	0.0	
•••										
2995	5.0	44.0	5.041393	1.0	0.0	0.0	0.0	0.0	0.0	
2996	4.0	30.0	4.602060	1.0	0.0	0.0	0.0	0.0	0.0	
2997	2.0	27.0	4.193125	1.0	0.0	0.0	0.0	1.0	0.0	
2998	2.0	27.0	4.477121	0.0	0.0	0.0	0.0	0.0	0.0	
2999	6.0	55.0	4.505150	0.0	0.0	0.0	1.0	0.0	0.0	

3000 rows × 17 columns

```
In [217... wage_nn_train = torch.tensor(wage_train.drop(columns = 'jobclass_2. Information').v
jobclass_nn_train = torch.tensor(wage_train['jobclass_2. Information'].values, dtyp
jobclass_nn_train = jobclass_nn_train.view(-1, 1)
wage_nn_test = torch.tensor(wage_test.drop(columns = 'jobclass_2. Information').val
jobclass_nn_test = torch.tensor(wage_test['jobclass_2. Information'].values, dtype=
jobclass_nn_test = jobclass_nn_test.view(-1, 1)
```

In [218... wage_nn_train.shape

Out[218... torch.Size([2396, 16])

```
In [219...
          device = torch.accelerator.current_accelerator().type if torch.accelerator.is_avail
          class Net(nn.Module):
              def __init__(self, d_in = 17):
                   super(Net, self).__init__()
                   self.linear_relu_logit_stack = nn.Sequential(
                      nn.Linear(d_in, 32),
                      nn.ReLU(),
                      nn.Linear(32, 32),
                      nn.ReLU(),
                      nn.Linear(32, 1),
                      nn.Sigmoid()
              def forward(self, x):
                   return self.linear_relu_logit_stack(x)
          model = Net(d_in = 16).to(device)
          print(model)
```

```
Net(
          (linear_relu_logit_stack): Sequential(
            (0): Linear(in_features=16, out_features=32, bias=True)
            (1): ReLU()
            (2): Linear(in_features=32, out_features=32, bias=True)
            (3): ReLU()
            (4): Linear(in_features=32, out_features=1, bias=True)
            (5): Sigmoid()
          )
        )
In [220...
         optimizer = optim.Adam(model.parameters(), lr=10e-4)
          epochs = 25
In [221... for t in range(epochs):
             print(f"Epoch {t+1}\n----")
             train(wage_nn_train, jobclass_nn_train, model, loss_fn, optimizer)
             test(wage_nn_train, jobclass_nn_train, model, loss_fn)
```

Epoch 1
Test Error: Accuracy: 61.7%, Avg loss: 0.670983
Epoch 2
Test Error: Accuracy: 62.4%, Avg loss: 0.646089
Epoch 3
Test Error: Accuracy: 62.4%, Avg loss: 0.643450
Epoch 4
Test Error: Accuracy: 63.4%, Avg loss: 0.647053
Epoch 5
Test Error: Accuracy: 63.9%, Avg loss: 0.640471
Epoch 6
Test Error: Accuracy: 61.6%, Avg loss: 0.651038
Epoch 7
Test Error: Accuracy: 63.8%, Avg loss: 0.638435
Epoch 8
Test Error: Accuracy: 63.4%, Avg loss: 0.639214
Epoch 9
Test Error: Accuracy: 63.6%, Avg loss: 0.638327
Epoch 10
Test Error: Accuracy: 63.9%, Avg loss: 0.641005
Epoch 11
Test Error: Accuracy: 63.8%, Avg loss: 0.636597

Epoch 12

Test Error:
Accuracy: 63.3%, Avg loss: 0.643140
Epoch 13
Test Error: Accuracy: 64.7%, Avg loss: 0.633007
Epoch 14
Test Error:
Accuracy: 63.2%, Avg loss: 0.638376
Epoch 15
Test Error:
Accuracy: 61.6%, Avg loss: 0.661419
Epoch 16
Test Error:
Accuracy: 63.9%, Avg loss: 0.633139
Epoch 17
Test Error:
Accuracy: 63.4%, Avg loss: 0.638465
Epoch 18
Test Error:
Accuracy: 64.0%, Avg loss: 0.634474
Epoch 19
Test Error:
Accuracy: 64.5%, Avg loss: 0.634486
Epoch 20
Test Error:
Accuracy: 64.5%, Avg loss: 0.630806
Epoch 21
Test Error:
Accuracy: 63.8%, Avg loss: 0.637442
Epoch 22
Test Error:
Accuracy: 64.7%, Avg loss: 0.630708
Epoch 23

```
In [222...
wage_nn_train_err = ((model(wage_nn_train) > 0.5) == jobclass_nn_train).sum().item(
print(f"The training error for the neural network is {1 - wage_nn_train_err}")
wage_nn_test_err = ((model(wage_nn_test) > 0.5) == jobclass_nn_test).sum().item()/1
print(f"The test error for the neural network is {1 - wage_nn_test_err}")
```

The training error for the neural network is 0.3505843071786311 The test error for the neural network is 0.3178807947019867

This test error beats our other test error by more than 4%!