

Suppose we have the following definition of a Node:

```
class Node<T> {  
    public T data;  
    public Node<T> next;  
  
    public Node<T>(T data, Node<T> next) {  
        this.data = data  
        this.next = next  
    }  
}
```

### Diagramming Question

Suppose that I have the following code. Diagram the objects allocated and the links between them.

```
Node<String> a = new Node<String>("a", null);  
Node<String> b = new Node<String>("b", a);  
Node<String> c = new Node<String>("c", b);  
Node<String> d = new Node<String>("d", c);  
Node<String> e = new Node<String>("e", d);  
Node<String> f = new Node<String>("f", d); // Note the difference here!
```

### Implementation Question

Write a function called `average` which gets the average of a singly linked lists of doubles (or more specifically `Double`, which is a pointer to a double and acts like a double for all purposes here). We are given the head node. It will likely return a divide by zero error if head is null:

```
public double average(Node<Double> head) {
```

```
}
```

What is the big-Oh running time of your function?

### Implementation Question

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public double average(Node<Double> head) {
```

```
}
```

What is the big-Oh running time of your function?

### Diagramming Question

Suppose that I have an array of arrays (remember that's an array of pointers, all pointing to other arrays)

```
int[][] arr = { {1, 2, 3}, {}, null, {10, 11, 12} };
```

Diagram how this is stored in memory.

## Running Time

What is the big-Oh running time of the following function in terms of  $n$ ?

```
int countingOnAStack(int n) {  
    Stack<Integer> stack = new ArrayStack(1000);  
    stack.push(n);  
    return countingOnAStack(new ArrayStack(1000));  
}
```

```
int countingOnAStack(Stack<Integer> stack) {  
    while (!stack.isEmpty())  
        int item = stack.pop();  
  
    if (item >= 0) {  
        stack.push(item - 1);  
        stack.push(item - 1)  
    }  
}  
}
```

## Running Time

What is the running time of the following code in terms of  $n$ ?

```
// arr is an array of length n
int currentMax = 0;
for(i = 0; i < n; i++) {
    if (arr[i] > currentMax) {
        currentMax = arr[i];
    }

    // Increase the rest of the array
    for(j = i + 1; j < n; j++) {
        arr[j] += 1
    }
}
```

## Running Time + Coding

What is the worst case running time of findAll in terms of  $n$ , which is the length of an array?

// int[] arr is an array of length  $n$

```
int findInArray(int element) {  
    for(i = 0; i < n; i++) {  
        if (element == i) return i;  
    }  
    return i;  
}
```

```
int[] findAll() {  
    int[] answer = new int[n]; // Allocate an array of length  $n$   
  
    for(int i = 0; i < n; i++) {  
        answer[i] = findInArray(i)  
    }  
  
    return answer;  
}
```

**Could you write a better version of findAll that accomplishes the same thing with a better big-Oh running time?**

## **Coding**

You are given a linked list. Construct another Linked List that is your input in reverse order.

What is the big-Oh running time of your algorithm?



## Stacks (Basic)

What gets printed out by the following code?

```
Stack<Integer> stack = new ListStack<Integer>()
stack.push(2)
stack.push(8)
int x = stack.pop()
stack.push(10)
stack.push(x)
stack.push(x)
stack.push(12)
x = stack.pop();
stack.push(x + 1)

while(!stack.isEmpty()) {
    System.out.println(stack.pop())
}
```

## Queue (Basic)

You have a queue of Integers stored in a circular array of length 5. Draw the values of the Queue after the following operation. Shade in the space in the array that is unused.

```
Queue<Integer> q = new ArrayQueue(5);
```

```
q.enqueue(4)
```

```
q.enqueue(3)
```

```
q.enqueue(2)
```

--	--	--	--	--

```
q.dequeue()
```

```
q.enqueue(8)
```

```
q.enqueue(10)
```

--	--	--	--	--

```
int x = q.dequeue()
```

```
q.dequeue()
```

```
q.enqueue(x)
```

```
q.enqueue(x * 2)
```

(also draw the starting and ending elements of the queue)

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### **Coding (Stack)**

Given a stack with at least two elements, implement `addAndRestack`, which pops 2 elements, adds them together, and pushes the sum back onto the stack.

Write a `sumUntil(int stop)` function that calls `sum` on the stack until a stopping value is found. In that case, leave the stopping value on the stack, and push the sum on top of it.

**Code (Stack)**

You are given a headed Singly-linked list, and nodes a and b.

Describe a function called `exchange(Node<> a, Node<> b)` which exchanges the place of the nodes `a.next` and `b.next`. Your algorithm may only modify links, and may not allocate new nodes (you must work with the nodes you have, only changing the next values)

What is the Big-Oh running time of your algorithm?

## Array Scheme

You have an array of arrays.

`int[][] arr.`

The array is of length  $n$ , and `arr[i]` is always of length  $2^i$

Describe a scheme to store this entire data structure in a single array, and how you would access `arr[i][j]` in this single array.