Modelling the influence of rhizodeposits on root water uptake

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Abstract

Keywords—

1 Introduction

For decades, advancing crop performance has been a key pursuit within agricultural research and, with the coupled pressures of an increasing global population and climate change, the need for improvements in yield and stress resilience are only increasing. Improving plant water use efficiency, whether from precipitation or irrigation, is a central focus and 3 facets of achieving this were previously outlined in (Condon et al., 2004). The first two are to improve plant ability to convert transpired water into biomass, whilst 6 also having crops partition more of this biomass into harvestable product. The final process, and the one focused on by this paper, is to enable the plant to take up a greater proportion of any water that is added to the soil. In this context the aim is to minimise losses of water from the regions of soil where uptake is possible, which may occur through evaporation or drainage to unvegetated depths (Figure 1). The part of 10 the plant anatomy most relevant here is the root system, and an obvious morphological trait to consider 11 when aiming to maximise plant access to water is the root system architecture (RSA). From the literature, 12 the dominant ideotype proposed for stress-resistant rain-fed crops is a root system with sufficient lateral 13 span at shallow depths to catch rainfall entering from above, but where the majority of resources are 14 allocated to growing downward so that stores of water deep in the soil can be accessed during periods of 15 drought (Lynch, 2013; Uga et al., 2013; Lynch and Wojciechowski, 2015). Furthermore, the preference for 16 deep roots persists to some extent in less water-limited environments because crop irrigation strategies 17 involving access to deep soil water are less exposed to increasingly volatile rainfall patterns and facilitate 18 the economic management of industrial scale cultivation (Wasson et al., 2012). Opinion is more nuanced 19 when it comes to crops grown in environments where soil is shallow however. Here the priority is to 20 capture water during infiltration before it runs off at bedrock and becomes unavailable, regardless of root 21 length (Tardieu, 2012; Wasson et al., 2012). 22 Over a quarter of net fixed carbon among annual crops is apportioned to roots and, depending on species, 23 between 25 to 70 percent of this is released into the soil in the form of rhizodeposits (McGrail et al., 2020). 24 These rhizodeposits have been shown to materially affect the soil characteristics while also facilitating 25 microbial colonisation, and the zone of soil falling under this influence is referred to as the rhizosphere. 26 For example, rhizodeposit-induced changes to soil hydraulic properties have been frequently observed 27 across a number of crop species. For Wheat, Maize and Barley the surface tension of soil water has been 28 shown to decrease with increasing root exudate concentration (Read and Gregory, 1997; Read et al., 2003; 29 Naveed et al., 2019) and in Maize and Wheat an increasing concentration of sorbed exudates in the soil 30 was found to increase contact angle between water and the soil surface (Ahmed et al., 2016; Zickenrott 31 et al., 2016; Benard et al., 2018; Naveed et al., 2019). Reductions in surface tension generally increase 32 infiltration rates through the soil and increases in contact angle are known to impede soil-rewetting. The 33 viscosity of soil water has also been found to be altered by increasing rhizodeposit concentration with 34 increases reported for Maize and Barley (Naveed et al., 2019). From the mathematical description of 35 saturated hydraulic conductivity, an increase in viscosity should translate as a decrease in saturated soil 36 hydraulic conductivity, conversely however, for soils vegetated by Maize (Feki et al., 2018), Willow and 37 Grass (Leung et al., 2018) this has been observed as higher than that of fallow soil. Clearly, the combined 38 effects of rhizodeposits on soil hydraulics are hard to untangle and their net effect on the availability of 39 water to the root system, is difficult to ascertain and is likely to vary with environmental factors like 40 rainfall pattern, evaporation rate and soil depth, and morphological or physiological traits like root system 41 architecture and axial hydraulic conductivity. 42 Improved knowledge of what rhizodeposit effects on soil hydraulics are beneficial or detrimental and under 43 what conditions could prove useful to crop breeders in identifying target ideotypes for different agricultural 44 zones where levels of available water and methods of irrigation differ. This paper aims to address this by 45 taking a mathematical model for water transport and root water uptake in vegetated soil, which has been 46 calibrated against for the effect of winter wheat exudates on soil hydraulic properties using results from 47 an infiltration experiment, and investigating the effect of increased rhizodeposit concentration on uptake 48 performance. The effect is considered for root systems of different ages in environments with varying 49 levels of total rain and different patterns of rain delivery.

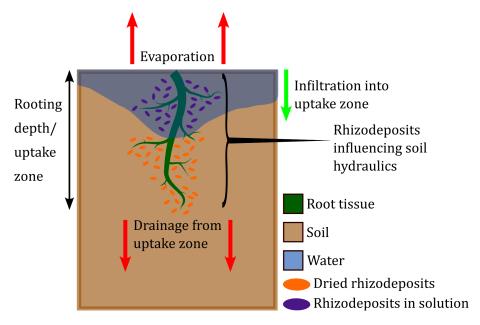


Figure 1: Rhizodeposits and root water uptake. The uptake performance of a plant is affected by the availability of water within the rooted regions of the soil. This figure shows the various processes that determine levels of water availability, all of which are influenced by the presence of rhizodeposits.

₁ 2 Materials and Methods

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2.1 A coupled model for soil water and rhizodeposit dynamics

Assuming a soil domain $\Omega = (-L, 0)$, with depth L and spatial variable x, and temporal interval with final time T > 0, the relationship between soil hydraulics, root rhizodeposits, and root water uptake is modelled by coupling a modified Richards equation for water transport (Richards, 1931):

$$\partial_{t}\theta(h; c_{W}, c_{D}) + \partial_{x}\mathbf{q}(h; c_{W}, c_{D}) = -S(x, t) & x \in \Omega, \ t \in (0, T],
\mathbf{q}(h; c_{W}, c_{D}) = g_{0}(h, t) & x = 0, \ t \in (0, T],
-\mathbf{q}(h; c_{W}, c_{D}) = g_{L}(h, t) & x = -L, \ t \in (0, T],
h = h_{0}(x) & x \in \Omega, \ t = 0,$$
(2.1)

with an advection diffusion equation for the dynamics of root rhizodeposits in solution

$$\partial_{t}\theta c_{W} - \partial_{x}(\theta D_{W}\partial_{x}c_{W} - \mathbf{q}c_{W}) = \rho \kappa_{W}c_{D} - \theta \kappa_{D}c_{W} + f(x,h) \qquad x \in \Omega, \ t \in (0,T],$$

$$-(\theta D_{W}\partial_{x}c_{W} - \mathbf{q}c_{W}) = 0 \qquad x = 0, \ t \in (0,T],$$

$$\theta D_{W}\partial_{x}c_{W} - \mathbf{q}c_{W} = 0 \qquad x = -L, \ t \in (0,T],$$

$$c_{W} = c_{W,0}(x) \qquad x \in \Omega, \ t = 0,$$

$$(2.2)$$

and an ordinary differential equation for dried rhizodeposit concentration

$$\rho \partial_t c_D = \theta \kappa_D c_W - \rho \kappa_W c_D \quad x \in \Omega, \ t \in (0, T],$$

$$c_D = c_{D,0} \qquad x \in \Omega, \ t = 0.$$
(2.3)

These component models (2.1), (2.2) and (2.3) are solved for soil water pressure head h [L], rhizodeposit concentration in solution c_W [ML⁻³] and rhizodeposit concentration dried to the soil surface c_D [MM⁻¹] respectively. In (2.1), soil water content is given by θ [L³L⁻³], root water uptake by S [T⁻¹], and the flux conditions at the soil upper surface and base by g_0 and g_L respectively. The movement of water through the soil is driven by the Darcy-Buckingham flux (Darcy, 1856)

$$\mathbf{q} = -K(h; c_W, c_D)\partial_x(h+x), \tag{2.4}$$

with K [LT⁻¹] being the hydraulic conductivity, and appears as the advective term in the flux of root rhizodeposits in solution. The remaining terms in (2.2) and (2.3) are the rhizodeposit diffusion coefficient D_W [L²T⁻¹], the soil bulk density ρ [ML⁻³], a source term f [ML⁻³T⁻¹] for the release of rhizodeposits into the soil solution by the plant, and the rates at which dried rhizodeposits join the soil solution κ_W [T⁻¹] and rhizodeposits in solution dry to the soil surface κ_D [T⁻¹]. The influence of rhizodeposits is incorporated into the water transport and uptake model (2.1) through

The influence of rhizodeposits is incorporated into the water transport and uptake model (2.1) through modifications to the Van Genuchten (1980) and Mualem (1976) formulations of the functions for water content and hydraulic conductivity:

$$\theta(h; c_W, c_D) = \theta_r + (\theta_s - \theta_r) S_e(h; c_W, c_D), \tag{2.5}$$

$$K(h; c_W, c_D) = K^* + \alpha_K K_s(c_W, c_D) K_r(h; c_W, c_D).$$
(2.6)

Here, the impact of rhizodeposits is built in through the effective soil saturation function S_e in (2.5), and the functions for saturated hydraulic conductivity K_s [LT⁻¹] and relative hydraulic conductivity K_r in (2.6). The terms θ_r and θ_s in (2.5) give the residual and saturated soil water contents respectively and parameters K^* [LT⁻¹] and α_K are included in (2.6) to account for the fact that water content and hydraulic conductivity values at a given pressure head are generally lower if a soil is wetting than if it is drying. This hysteresis exists because the processes that occur when a soil dries are generally governed by activity in the smaller pores whereas the wetting of a soil tends to be determined by the larger pores. Furthermore, the contact angles between the menisci and the soil surface are different depending on whether water is entering or draining from a pore (Van Genuchten and Pachepsky, 2011; Zhou, 2013). In (2.5) the phenomenon of hysteresis is incorporated by the effective saturation

$$S_e(h; c_W, c_D) = \frac{1}{(1 + |\alpha_{\theta}(c_W, c_D)h|^{n_{\theta}})^{m_{\theta}}}.$$
(2.7)

Here n_{θ} and $m_{\theta} = 1 - \frac{1}{n_{\theta}}$ are shape parameters and the parameter relating to inverse pore air entry pressure α_{θ} [L^{-1}] takes different values depending on whether the soil is wetting or drying such that

$$\alpha_{\theta}(c_W, c_D) = \begin{cases} \alpha_{\theta}^W(c_W, c_D) & \text{if wetting,} \\ \alpha_{\theta}^D(c_W, c_D) & \text{if drying,} \end{cases}$$
 (2.8)

with $\alpha_{\theta}^{W} \geq \alpha_{\theta}^{D}$ (Kool and Parker, 1987). Therefore, if at a given pressure head h_{Δ} and water content θ_{Δ} there is a switch from drying to wetting or vice versa, then the value of α_{θ} will also switch. To maintain the continuity of θ when this happens, the residual and saturated water contents also switch between different values for wetting and drying:

$$\theta_r = \begin{cases} \frac{(\theta_{\Delta} - \theta_{s,0} S_e(h_{\Delta}))}{1 - S_e(h_{\Delta})} & \text{if } \alpha_{\theta} = \alpha_{\theta}^W, \\ \theta_{r,0} & \text{if } \alpha_{\theta} = \alpha_{\theta}^D, \end{cases} \qquad \theta_s = \begin{cases} \theta_{s,0} & \text{if } \alpha_{\theta} = \alpha_{\theta}^W, \\ \frac{\theta_{\Delta} - \theta_{r,0} (1 - S_e(h_{\Delta}))}{S_e(h_{\Delta})} & \text{if } \alpha_{\theta} = \alpha_{\theta}^D. \end{cases}$$
(2.9)

This affects the value of K through the relative hydraulic conductivity

$$K_{r}(h; c_{W}, c_{D}) = \left(\frac{2(\theta_{s,0} - \theta_{r,0})S_{e}(h_{\Delta}; c_{W}, c_{D}) + \varepsilon(1 - 2S_{e}(h_{\Delta}; c_{W}, c_{D}))}{2(\theta_{s,0} - \theta_{r,0})}\right)^{l} \cdot \left(1 - \left(1 - \left(\frac{2(\theta_{s,0} - \theta_{r,0})S_{e}(h_{\Delta}; c_{W}, c_{D}) + \varepsilon(1 - 2S_{e}(h_{\Delta}; c_{W}, c_{D}))}{2(\theta_{s,0} - \theta_{r,0})}\right)^{\frac{1}{m_{\theta}}}\right)^{m_{\theta}}\right)^{2},$$
(2.10)

where the parameter l denotes the tortuosity of the porous structure. Moreover, hysteresis is also incorporated into K through a saturated hydraulic conductivity term that switches between values for wetting and drying soil (Vogel et al., 1996):

$$K_s(c_W, c_D) = \begin{cases} K_s^W(c_W, c_D) & \text{if wetting,} \\ K_s^D(c_W, c_D) & \text{if drying,} \end{cases}$$
 (2.11)

where $K_s^D > K_s^W$. Like (2.9), the parameters K^* and α_K in (2.6) are also formulated so as to maintain the continuity of K if a switch between wetting and drying occurs at $(h_{\Delta}, \theta_{\Delta}, K_{\Delta})$ (Vogel et al., 1996):

$$K^* = \begin{cases} K_s^W K_r(0) \left(1 - \frac{K_\Delta - K_s^W K_r(0)}{K_s^W K_r(h_\Delta) - K_s^W K_r(0)} \right) & \text{if } K_s = K_s^W, \\ 0 & \text{if } K_s = K_s^D, \end{cases}$$

$$\alpha_K = \begin{cases} \frac{K_\Delta - K_s^W K_r(0)}{K_s^W K_r(h_\Delta) - K_s^W K_r(0)} & \text{if } K_s = K_s^W, \\ \frac{K_\Delta}{K_s^D K_r(h_\Delta)} & \text{if } K_s = K_s^D. \end{cases}$$

$$(2.12)$$

The surface tension of soil water γ and the contact angle ϑ of its menisci with the pore surfaces have been shown by numerous studies to vary considerably with the concentration of rhizodeposits from a range of plant species (Ahmed et al., 2016; Naveed et al., 2018, 2019). This study will focus on wheat plants and in this case there is evidence that rhizodeposits increase the soil-water contact angle (Zickenrott et al., 2016), and decrease the surface tension of the soil solution (Read et al., 2003). To account for this within θ , the approach of Karagunduz et al. (2001) is employed and scaling factors are introduced into α_{θ} , such that for $(c_W, c_D) \in [0, \infty)^2$,

$$\alpha_{\theta}^{W}(c_W, c_D) = \frac{\gamma(c_W)\cos(\vartheta_0)}{\gamma_0\cos(\vartheta(c_D))} \alpha_{\theta,0}^{W}, \quad \text{and} \quad \alpha_{\theta}^{D}(c_W) = \frac{\gamma_0}{\gamma(c_W)} \alpha_{\theta,0}^{D}, \tag{2.13}$$

where γ_0 and ϑ_0 are the surface tension and contact angle values in the absence of rhizodeposits, and $\alpha_{\theta,0}^W$ and $\alpha_{\theta,0}^D$ are the corresponding wetting and drying values of α_{θ} . In the formulations of (2.13) a rhizodeposit-induced reduction in surface tension will decrease α_{θ}^W and increase α_{θ}^D , which means the associated pressure head to a given water content will be decreased in wetting soil and increased in drying soil. Moreover, the assumption is made that soil-water contact angle will only have a material effect during the wetting of the soil, where an increase in contact angle will mean that the pressure head associated to a given water content during wetting is increased. In a similar way, to incorporate the effect of rhizodeposit-induced decreased surface tension and soil-water contact angle on K, the saturated hydraulic conductivities are formulated so that, for $(c_W, c_D) \in [0, \infty)^2$,

$$K_s^Z = K_{s,0}^Z \left(\frac{\gamma_0}{\gamma(c_W)}\right)^\beta \frac{\cos(\vartheta(c_D))}{\cos(\vartheta_0)},\tag{2.14}$$

where Z = W, D. This formulation was informed by the experimental work in (Cite Emma's paper) where rhizodeposit induced reductions in surface tension increased hydraulic conductivity and this effect dominated over any rhizodeposit-induced increases in contact angle. The parameter β in (2.14) determines the extent to which such a rhizodeposit-induced reduction in surface tension will increase saturated hydraulic conductivity.

As in (Simunek and Hopmans, 2009), root water uptake in (2.1) is modelled with a macroscopic sink term S incorporating water availability, root distribution, and potential plant transpiration \mathcal{T}_{p} [LT^{-1}]:

$$S(x,h) = \alpha_F(h)NRLD(x)\mathcal{T}_p \frac{1}{\max(\omega(t), \omega_c)}.$$
 (2.15)

The dependence of uptake on the level of soil saturation is included in S through the dimensionless stress response function $0 \le \alpha_f \le 1$, and the plant's capacity to reach the water within the soil is accounted for by the normalised root length density NRLD $[L^{-3}]$, which is a continuous function that gives the distribution of root length within the soil. A measure of the global water stress experienced by the plant is given by the function

$$\omega(t) = \int_{\Omega} \alpha_f(h(x,t)) NRLD(x) dx \qquad (2.16)$$

and the capacity of the plant to compensate for poor water availability in one soil region by increasing uptake in zones of higher saturation is reflected by ω_c (Cai et al., 2018). The boundary condition at the soil surface is

$$g_0(h,t) = K_e(h)ET_0 + RO(h,t) - P(t)$$
 (2.17)

where K_e [-] is a function that determines the proportion of total evapotranspiration that comes from evaporation, ET₀ [LT⁻¹] is the reference evapotranspiration, P [LT⁻¹] the precipitation rate and RO [LT⁻¹]

is a function for the run-off of water that occurs when precipitation cannot enter the soil due to the surface already being fully saturated:

$$RO(h,t) = P(t) \left(1 + \frac{\exp(a(\theta(h) - \theta_{s,0})) - 1}{\exp(a(\theta(h) - \theta_{s,0})) + 1} \right).$$
 (2.18)

Here the constant a>0 is set to a large enough value so that if the surface is fully saturated $(\theta=\theta_{s,0})$ then RO(t)=P(t). On the lower boundary x=-L, the condition of free drainage is assumed, which translates as $g_L(h)=K(h)$. The source term f in (2.2) for the release of rhizodeposits into the soil is formulated as follows:

$$f(x,h) = \lambda \theta(h) SAD(x), \tag{2.19}$$

where λ [ML⁻²T⁻¹] is the rate at which rhizodeposits are released from the surface of the root and SAD [L⁻¹] is the root surface area density, a continuous function representing the distribution of root surface area throughout the soil. Expressions for any functions that have not been explicitly discolsed in this paper can be found in the supplementary material.

2.2 Parametrisation and Calibration

To explicitly model the ways in which rhizodeposits induce a reduction in soil water surface tension γ , and an increase in the contact angle ϑ between menisci and the soil pore surface, the data of Read et al. (2003) and Zickenrott et al. (2016) was used to fit the following functions:

$$\gamma(c_W) = 47.5 + \frac{72.86 - 47.5}{1 + \exp(18.79(c_W - 0.36))},$$
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$$\vartheta(c_D) = \frac{3.529}{18} \pi (1 + \exp(-1879.14c_D))^{-4.39}.$$
 (2.21)

These functions return $\gamma_0 = \gamma(0) = 72.86 \text{mNm}^{-1}$ and $\vartheta_0 = \vartheta(0) = 0.0294 \text{rad}$ as the surface tension and contact angle when there are no rhizodeposits present. The soil type and crop species considered in all model simulations were sandy loam and winter wheat, and the majority of the values that were required to parametrise the models accordingly were taken from existing literature, see supplementary material for the specific values and from where they were sourced.

The remaining parameter values to source were then the rates at which dried rhizodeposits join the soil water solution κ_W and rhizodeposits in solution dry to the pore surface κ_D , and also the parameter β that controls the size of the increase in saturated hydraulic conductivity that is brought about by a rhizodeposit-induced reduction in surface tension. However, the values of these 3 parameters were recently approximated in the work of EMMA ET AL. In that study, an experimental setup was used in which 4 chambers were filled with 3 distinctly treated layers of Nafion a transparent artificial soil. The top layer was saturated with water and dye, the layer at the bottom was saturated with only water and the particles of the central layer were completely dry. In one of the chambers winter wheat rhizodeposits were then added to the water and dye solution of the upper layer. In the second chamber dried exudates were added only to the dry middle layer of the chamber. The third chamber had rhizodeposits in the solution in the upper layer as well as dried rhizodeposits in the central layer, and the fourth chamber was left as the control with no rhizodeposits added. Infiltration was left to occur for 5 days within these 4 chambers and, to assess the effect of rhizodeposits, the dye concentration in the lower layer of each chamber was recorded at regular intervals. To approximate κ_D , κ_W and β , EMMA ET AL used the model system (2.1)-(2.3), along with an advection diffusion equation for dye concentration within the chamber, to simulate their experimental procedure. Bayesian optimisation Brochu et al. (2010) was then employed to run simulations of these models and search the parameter space of $(\kappa_D, \kappa_W, \beta)$ to approximate the values that allowed the model system to best reproduce the results of the experiment. Further details of this experimental setup and the calibration procedure involving Bayesian optimisation can be found in (EMMA ET AL) and the supplementary material.

The functions for normalised root length density NRLD and surface area density SAD were constructed for 3 winter wheat root systems of ages 6, 15 and 30 days (ADD FIGURE?). Architectures of these root systems were generated from CRootBox (Schnepf et al., 2018) and the methods previously employed and described in (Mair et al., 2022, 2023; Mair, 2023) were used to convert this architecture data into density

functions for the distributions of root length and surface area within the 3-dimensional spatial domain that enclosed all 3 root systems. These functions were then averaged laterally across the 3D domain to produce NRLD and SAD as functions of 1D space (-L,0) where L=52.973cm is the greatest depth reached by any root of the 3 systems. The exact parameter settings that were used within CRootBox to simulate the different root systems are shown in the supplementary material.

2.3 Simulated scenarios

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To investigate the impact of rhizodeposits on root water uptake performance, the model system (2.1), (2.2) and (2.3) was separately parametrised for each age of root system. For every root system parametrisation, 6 precipitation regimes were considered. In 3 of these regimes the precipitation function P was formulated to deliver a total of 0.12cm rainfall over a time period of T=3d days, delivered in either 1, 2 or 3 rainfall events. In order to ensure total precipitation remained the same across all patterns, each time the total number of rainfall events was increased by 1 the duration of each rainfall event decreased by 25%, along with a corresponding decrease in the rainfall rate. The other 3 precipitation regimes were defined in the same way, but with total rainfall set to 0.28cm. Figures 2 and 3 (a)-(c) provide a visual representation of the precipitation function P for the 6 different rainfall patterns. In each scenario, initial water content was set to a uniform value of $\theta(h_0) = 0.69$ throughout the domain. In the non-control scenarios that included rhizodeposits, the initial concentration of rhizodeposit in solution was set so that in the depths of soil occupied by roots $C_{W,0} = 2.5 \text{mgcm}^{-3}$ but in the depths without roots $C_{W,0} = 0 \text{mgcm}^{-3}$. Assuming an initial equilibrium between the dynamics of dried rhizodeposits and rhizodeposits in solution, initial dried rhizodeposit concentration was set so that $C_{D,0} = 5.2 \times 10^{-4} \mathrm{mg cm^{-3}}$ in domain depths with roots, and $C_{D,0} = 0 \text{mgcm}^{-3}$ in depths without vegetation. Explicit mathematical formulations for all of these initial conditions and of P for each precipitation regime is given in the supplementary material. Infiltration simulations were then obtained for each root system and precipitation pattern combination, both with and without the incorporation of rhizodeposit influence, and data on soil water distribution and root water uptake were gathered.

217 2.4 Computations

Numerical solutions for pressure head, rhizodeposits in solution and dried rhizodeposits were obtained 218 from the model system (2.1), (2.2), (2.3) using a conformal finite element method and an implicit Euler 219 discretisation in time. The cells of the 1D domain discretisation were each 0.59273cm in length, and the 220 time step size was 0.001d. Linearisation of the functions for water content and hydraulic conductivity 221 in (2.1) was carried out using the L-scheme of List and Radu (2016). The numerical method was imple-222 mented using the FEniCS library Alnæs et al. (2015) and the algorithms to construct NRLD and SAD 223 from CRootBox architectures were run in Python 3 using the libraries NumPy and SciPy (Harris et al., 224 2020). The visualisations of 1D root density profiles, water distributions and flux strength were generated 225 from Paraview (Ahrens et al., 2005). 226

227 3 Results

3.1 General rhizodeposit effects on soil water dynamics and uptake

For all rainfall patterns in the regimes of both lower and higher total precipitation, and all root sys-229 tem ages, following the onset of a rainfall event, the presence of rhizodeposits within soil was found to 230 induce a boost in uptake to a rate higher than that exhibited in the situation without rhizodeposits (Fig-231 ures 2 and 3 (g)-(i)). Moreover, for all root systems in all precipitation conditions the presence of 232 rhizodeposits in the soil was shown to reduce evaporation from the upper soil surface to a lower rate, 233 and this effect was maintained for the remainder of the entire simulation time (Figures 2 and 3 (g)-(i)). 234 Despite this, however, it was not true in all scenarios that uptake in the presence of rhizodeposits was 235 maintained at a higher rate than without rhizodeposits for the entire simulation. 236 Figures 4 and 5 show that the presence of rhizodeposits increased the strength of the downward water 237 flux in the scenarios of a lower total precipitation delivered over 3 rainfall events and a higher total 238 precipitation delivered in one event. It can also be seen that this increased flux led to an accelerated

arrival of water to the rooted zone compared to the non-rhizodeposit case, and a greater proportion of

water reaching deeper regions of the soil at earlier times. This was true for all total rainfall quantities

242 and delivery patterns but Figures 4 and 5 show the regimes under which this effect was most weakly and 243 strongly observed respectively.

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Considering root systems of all ages, there was a general trend that the percentage positive change in total water uptake, which came from including rhizodeposits in the model, decreased as the amount of total rainfall in the 3 day simulation was increased (Figure 6). In addition, when fixing total rainfall and considering the pattern by which it was delivered, it is also true that the positive effect of rhizodeposits on total water uptake was reduced as the quantity of precipitation delivered per event increased.

The remaining subsections of this results section provide more precise detail on how the strength and consequences of these rhizodeposit effects were felt differently for root systems of different ages.

3.2 Rhizodeposits and the uptake performance of plants with shallower root systems

In all 3 rainfall patterns of the regime with lower total rainfall (0.12cm), the uptake rates of the 6 and

15-day old wheat plants, which have shallower root architectures (Figure 4/MATLAB Figure), are higher 254 when rhizodeposits are present than when they are not, and this is true at all time points (Figure 2). However, in the precipitation pattern where all 0.12cm is delivered in a single event, it can also be seen 256 from Figure 2 that this difference in uptake rate had almost closed by the end of the 3 day period. 257 Nevertheless, in all these conditions, with total rainfall at 0.12cm, total water uptake over the 3 day 258 period is obviously still higher for the root systems where rhizodeposits are present than those where 259 they are not (Table 1). 260 In the regime where a higher total precipitation is delivered, if the 0.28cm is split between 2 or 3 rainfall 261 events, then the 6 and 15-day old root systems with rhizodeposits also had higher total root water uptake 262 than without rhizodeposits (Table 1). But, although under all 3 different precipitation patterns of the 263 0.28cm the uptake of these shallower root systems with rhizodeposits initially assumes a rate that is 264 higher than that for when rhizodeposits are not present, eventually the uptake rates of the systems 265 without rhizodeposits overtake and maintain a higher value until the end of the simulation (Figure 3). 266 The timing of this overtake is earliest for the precipitation pattern in which all 0.28cm are delivered in 267 one event, and, in this case, the difference in the uptake rates becomes so large that the 6 and 15-day old 268 root systems actually return larger total water uptakes without rhizodeposits than with them (Table 2). 269 This effect can also be seen in Figure 6 which shows that the percentage change in total water uptake 270 271 that is induced by the presence of rhizodeposits is negative in the case where root systems are shallow and 0.28cm of precipitation is delivered in one event. 272

3.3 Rhizodeposits and the uptake performance of plants with deeper root systems

For the 30-day old root system, which had the deepest rooting depth, the uptake rate when rhizodeposits were present was higher, at all points in time, than when rhizodeposits were not considered, and this was true for the regimes with both lower and higher total rainfall and across all precipitation patterns. As a result, total root water uptake for these deeper root systems over the 3 day period was greater when rhizodeposits were present than when they were not (Figures 2 and 3).

A seemingly more anomalous result, however, was that within certain time intervals of the 3 day simulations (if not the entire simulation), for systems with and without rhizodeposits, the uptake rate of the 15-day old root system was higher than that of the 30-day old (Figures 2 and 3). In fact, when rhizodeposits were not present, for every case where total rainfall was 0.28cm or where all 0.12cm of total rainfall was delivered in one event, the greatest total uptake over the 3 days was by the 15-day old root system (Table 1 column 2 and, Table 2 columns 2, 4, 6). Furthermore, the rhizodeposit-enhanced water flux in the soil vegetated by the 15-day old root system was stronger than in the soil vegetated by the 30-day old plant (Figure 5).

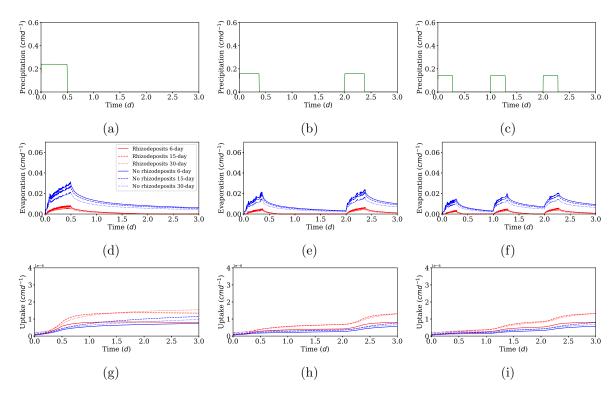


Figure 2: The influence of rhizodeposits on root water uptake under different precipitation regimes of a lower-rainfall environment. Plots (a)-(c) show the precipitation patterns considered. The plots (d)-(f) lying directly below show the evaporation rates corresponding to each pattern and for soils occupied by each age of root system with or without rhizodeposits present. Similarly plots (g)-(i) show the corresponding uptake rates of each root system, with and without rhizodeposits present

Total rainfall	0.12cm								
Rainfall distribution	1 event		2 events		3 events				
Rhizodeposits	No	Yes	No	Yes	No	Yes			
Total uptake: 6-day	1.67×10^{-6}	2.12×10^{-6}	8.35×10^{-7}	1.31×10^{-6}	8.49×10^{-7}	1.32×10^{-6}			
old plant (cm)									
Total uptake: 15-day	2.38×10^{-6}	3.44×10^{-6}	1.10×10^{-6}	2.05×10^{-6}	1.12×10^{-6}	2.06×10^{-6}			
old plant (cm)									
Total uptake: 30-day	2.08×10^{-6}	3.55×10^{-6}	1.16×10^{-6}	2.02×10^{-6}	1.17×10^{-6}	2.03×10^{-6}			
old plant (cm)									

Table 1: Total uptake of each root system with and without rhizodeposits for each rainfall distribution of the lower-rainfall regime.

Total rainfall	0.28cm							
Rainfall distribution	1 event		2 events		3 events			
Rhizodeposits	No	Yes	No	Yes	No	Yes		
Total uptake: 6-day	5.66×10^{-6}	4.71×10^{-6}	2.88×10^{-6}	3.19×10^{-6}	2.86×10^{-6}	3.22×10^{-6}		
old plant (cm)								
Total uptake: 15-day	8.85×10^{-6}	8.25×10^{-6}	4.22×10^{-6}	5.23×10^{-6}	4.18×10^{-6}	5.26×10^{-6}		
old plant (cm)								
Total uptake: 30-day	7.83×10^{-6}	1.01×10^{-5}	3.49×10^{-6}	5.47×10^{-6}	3.49×10^{-6}	5.52×10^{-6}		
old plant (cm)								

Table 2: Total uptake of each root system with and without rhizodeposits for each rainfall distribution of the higher-rainfall regime.

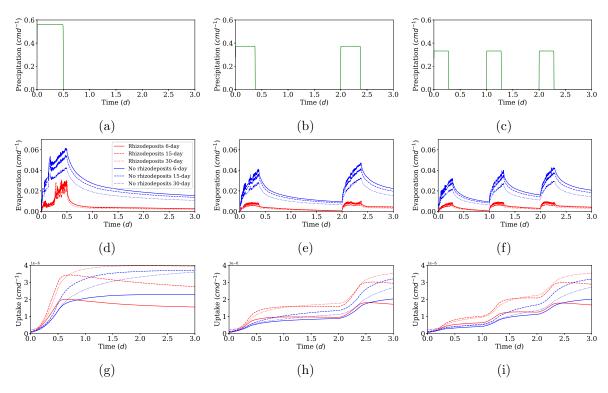


Figure 3: The influence of rhizodeposits on the evolution of soil water content and flux over time under the single-event pattern of the higher total rainfall regime. The figures of the leftmost column shows the normalised root length density profiles of each plant with age increasing downwards. The remaining columns show snapshots of the water content dynamics (with and without rhizodeposits) at different time points of the simulation where each row relates to soil vegetated by the roots of each age of plant. The arrows illustrate the strength of the flow at each time point of the various conditions

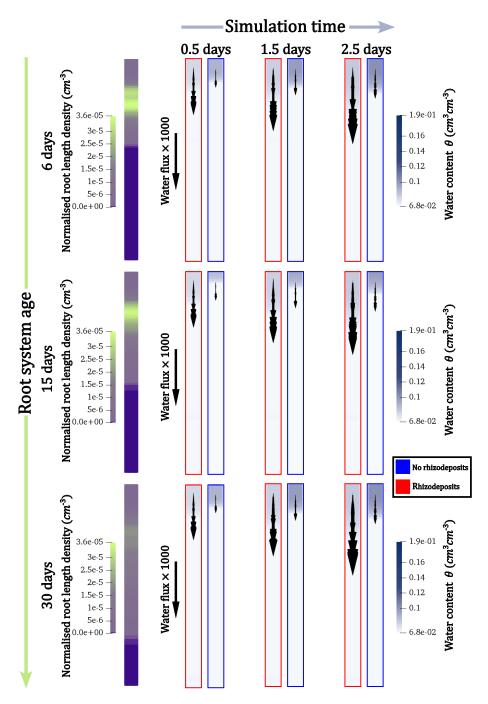


Figure 4: The influence of rhizodeposits on the evolution of soil water content and flux over time under the 3-event pattern of the lower total rainfall regime. The figures of the leftmost column shows the normalised root length density profiles of each plant with age increasing downwards. The remaining columns show snapshots of the water content dynamics (with and without rhizodeposits) at different time points of the simulation where each row relates to soil vegetated by the roots of each age of plant. The arrows illustrate the strength of the flow at each time point of the various conditions

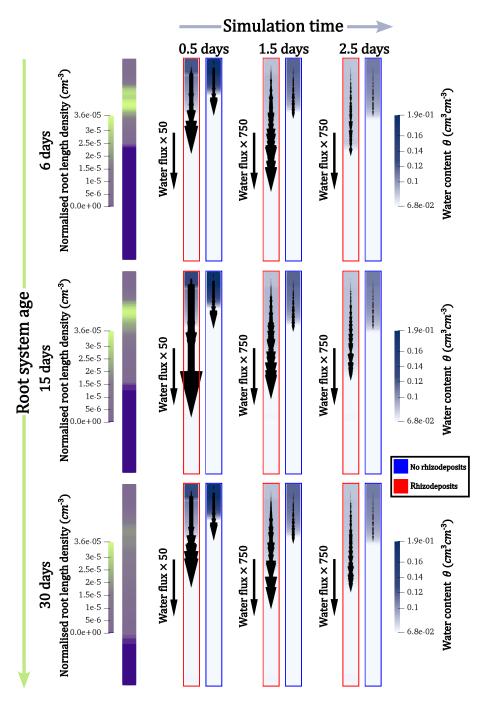


Figure 5: The influence of rhizodeposits on the evolution of soil water content and flux over time under the 3-event pattern of the low-rainfall regime. The figures of the leftmost column shows the normalised root length density profiles of each plant with age increasing downwards. The remaining columns show snapshots of the water content dynamics (with and without rhizodeposits) at different time points of the simulation, where each row relates to soil vegetated by the roots of a different age of plant. The arrows illustrate the strength of the flow at each time point of the various conditions

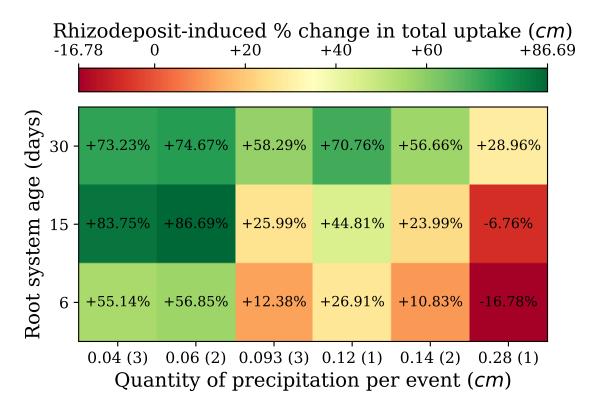


Figure 6: The strength of the positive or negative effect of rhizodeposits on total water uptake of a root system in relation to root system age/depth and the quantity of precipitation delivered in each rainfall event of the precipitation regime.

4 Discussion

4.1 Understanding the mixed impact of rhizodeposit-facilitated infiltration on root water uptake

Mucilage from wheat has been shown to have a surfactant affect when present in the soil water solution (Read et al., 2003), and the effect of this within the water transport model (2.1) is to increase the soil hydraulic conductivity and alter the water retention curve so that the downward flux of soil water is facilitated. As a result, in our simulations where rhizodeposits were present, water infiltrated more quickly after the onset of precipitation, and this explains the reductions in evaporation rate that were observed. Moreover, for an interval of time during and after rainfall, the rhizodeposit-induced early arrival of water to the root zone promoted the higher uptake rate compared to soils without rhizodeposits. For less intense rainfall events, the gradients in water potential that develop between the more saturated surface and the drier rooted zone are less severe and the total amount of water delivered is smaller. Consequently, in these simulations the rhizodeposit-facilitated infiltration remained gradual enough, and the quantities of water that arrived early to the uptake zone sufficiently small, so that the shallower-rooted 6-day and 15-day old plants could enjoy rhizodeposit-boosted uptake rates for the entire simulation time, and not overly suffer from water bypassing their roots.

As the rates of rainfall during each event of our simulations were increased, however, the gradients driving water flux became greater and with time the added influence of rhizodeposits caused larger quantities of water to more quickly reach greater depths, thus becoming inaccessible to the root systems of the 6 and 15-day old plants. As a result, despite an early boost, uptake rates sooner or later dropped below those observed when rhizodeposits were not present (Figure 3), and their net effect on total water uptake can became negative (Figure 6).

The deeper root system possessed by the 30-day old plant meant that when rhizodeposits facilitated the transport of water to greater depths, it still remained accessible to the plant. Because of this, there was no trade off between reduced evaporation losses and a loss of water in the downward direction, and uptake rates with rhizodeposits are consistently higher than if there were no rhizodeposits present. It should be noted though that if, as reported for some species, root axial hydraulic conductivity decreases with root depth Clément et al. (2022), then this more unconditional benefit of rhizodeposits to deeper root systems may no longer hold.

In summary, the findings of this study suggest that the consequences on plant water uptake of infiltration-facilitating rhizodeposits may not be universally positive and depend upon the precipitation or irrigation conditions considered. Specifically, if total precipitation over a given time arrives in fewer more intense events, then the uptake of less developed or naturally shallow root systems may be hindered by excessive surfactant-induced acceleration of downward water transport. This is consistent with knowledge on optimal irrigation practices for soils that exhibit generally high infiltration rates, where methods that promote more gradual surface water application are promoted in order to avoid losses by leaching (Blackwell, 2000; Alhammadi and Al-Shrouf, 2013). Nevertheless, in environments where precipitation is less intense and more regular, rhizodeposits that facilitate infiltration are more likely to improve water availability and have a positive influence on uptake and crop performance (Oostindie et al., 2010; Chaichi et al., 2015).

4.2 Macroscopic uptake modelling for root systems of differing biomass

In this work, a so-called macroscopic approach (Simunek and Hopmans, 2009; Cai et al., 2018) was taken to incorporate root water uptake into the model for rhizodeposit-influenced soil water transport (2.1). The uptake function S integrates over the soil domain to give the transpiration rate of the plant, with adjustments made for local soil water stress. The potential contribution to this transpiration rate from each region of the soil domain is weighted according to the normalised root length density function NRLD, and NRLD is formulated so that for any root system it integrates to 1 over the entire soil domain. For smaller root systems, the vegetated region of the domain, where the NRLD function takes non-zero values, will be smaller. Hence, in order to have a unit integral over the soil, these NRLD functions of smaller root systems have to reach larger values than those corresponding to bigger root systems who take non-zero values over a greater portion of the domain. If the transpiration rate is the same for the plants of both the smaller and larger root systems, then this means that if water spends more time in the shallower depths, which contain the roots of both the smaller and larger root systems, then under the macroscopic uptake function the uptake rate of the smaller root system will be greater than that

of the larger. In our model, the transpiration rate associated to each root system increases with age in accordance with the data on basal crop coefficients in (Allen et al., 1998). However, this increase is not enough to counteract this effect of the normalised root length density and, under the conditions of more intense rainfall and without rhizodeposits to boost the downward flow of water, uptake rates and total uptake are greater for the 15-day old root system than the 30-day old one. This feature of the macroscopic approach means that model (2.1) may underestimate the uptake of larger root systems. One method of rectifying this is would be to simultaneously model water flow within the root and shoot system as well as the soil, with a boundary condition between the two domains for the passage of water into the root cells. However, this method is very computationally expensive at large scales. If continuing with macroscopic NRLD-based uptake terms going forward, then the transpiration rates in S needs to be formulated so that they increase with increases in the biomass of roots and corresponding shoots and leaves above-ground.

4.3 Rhizodeposits for resilient crop ideotypes

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The Green Revolution of the 1960s, with the increased use of chemical fertilisers, pesticides and precise irrigation, shifted the attention of crop breeders towards the question of maximising yield under conditions where stresses from water and nutrient shortages or competition were minimal (Preece and Penuelas, 2020). This approach led to a focus on optimal above ground traits, where one direction was to breed for crops that maximised the ratio of harvestable above ground biomass to total above ground biomass (the harvest index) (Richards et al., 1993). Since progress in this aspect rapidly became marginal, improvements to total above ground biomass were then sought and achieved through breeding for rapid leaf area development, to reduce evaporation losses from the soil, and enhanced leaf-level water use efficiency. Within the context of roots, however, the aim of many was to maintain root development at the necessary minimum so as to maximise resource allocation to harvestable biomass under ideal growing conditions (Condon et al., 2004). Nevertheless, with the increasing incidence of global drought, breeding strategies for resilient crops have come to also consider more developed root system architectures for boosting water use efficiency. Genes have been identified that control gravitropic response and radial growth (Hafeez et al., 2024) and there is a consensus that increasing rooting depth should be the target of breeders. This is firstly because it allows rain-fed crops to access deep stores of water during periods of drought (Lynch, 2013; Uga et al., 2013), and secondly because, in wheat systems specifically, root arrival at theses deep water stores tends to coincide with grain-filling season thus boosting biomass before harvesting (Palta et al., 2011; Wasson et al., 2012; Ober et al., 2021).

Moreover, as mentioned in a previous section, other rhizodeposits have been shown to improve retention of water (CITATION NEEDED) and facilitate rhizosphere colonisation by potentially symbiotic mycorrhizal fungi and bacteria Iannucci et al. (2021). Evidence has been shown of a genome effect on rhizodeposit and microbiome features (Iannucci et al., 2021), and it has been tentatively proposed that crops could be bred to promote the development of microbiomes that are specifically beneficial under certain stresses Ober et al. (2021). Despite this, however, few breeding programmes are yet to incorporate exudate characteristics in there selections (Preece and Peñuelas, 2020). This is because the interactions between root rhizodeposits and other actors in the microbiome are very complex and vary in nature between plant growth stages (Bakker et al., 2012; Oburger and Jones, 2018). Moreover, non-destructively extracting rhizodeposits from roots grown in the field is massively challenging, and there are also issues with the more simple approach of extracting rhizodeposits from roots grown in hydroponic systems, as it is doubtful if their observed properties would be the same if extracted from roots grown in soil (Oburger and Jones, 2018). Both of these factors mean that high throughput methods of effectively verifying that a given crop genotype induces the microbiome characteristics they are purported to require development. The same is true when it comes to models for validating the effects of these rhizodeposit and microbiome features on processes like water and nutrient availability. Within the modelling field there are differing approaches to incorporating rhizodeposit influence into models for water transport and uptake. Like in (Vogel et al., 1996; Karagunduz et al., 2001), our model assumes that the effect of rhizodeposit induced changes on contact-angle and surface tension can be incorporated into water retention (2.5) and hydraulic conductivity (2.6) by using the same effective saturation function (2.7) with an appropriately scaled air entry pressure term (2.13). However, this was not the case in (Cooper et al., 2017, 2018), where the influence of root exudates was incorporated into Richards equation through a rigorous multi-scale derivation and the effect of increasing contact angle resulted in retention and conductivity curves that no longer resembled the common functions of Brooks and Corey (1964) or Mualem (1976) and Van Genuchten

- (1980). Additionally, in (Landl et al., 2021) the effect of mucilage on water uptake is modelled, and a third different method, that of Kroener et al. (2014), is used to incorporate mucilage-induced changes in water retention. In both our work and that of Landl et al. (2021) many model parameters had to be taken from a wide range of existing publication and this also indicate the challenges in model calibration that arise from the fact that extracting exudates and reliably observing their effects is a complicated and expensive process.

 The results of this work suggest that root rhizodeposits, with a chemical composition that makes them
- The results of this work suggest that root rhizodeposits, with a chemical composition that makes them act as surfactants, can reduce evaporation losses from the soil and improve uptake performance of deeply 403 rooted systems. However, for the reasons above, the insights that can be drawn from this are modest and much work is required before such insights can be incorporated into the more simple large scale models for 405 crop yield. For breeding for rhizodeposit characteristics to be a viable option, the future work is needed 406 to progress to a stage where: there is more consensus on the correct approach to model the effect of 407 rhizodeposit induced changes to soil hydraulics on water transport, experiments for the effect of exudates 408 on the hydraulic parameters of these models can be more easily carried out and, finally, genotypes can 409 be identified which correspond to these exudate effects. 410

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