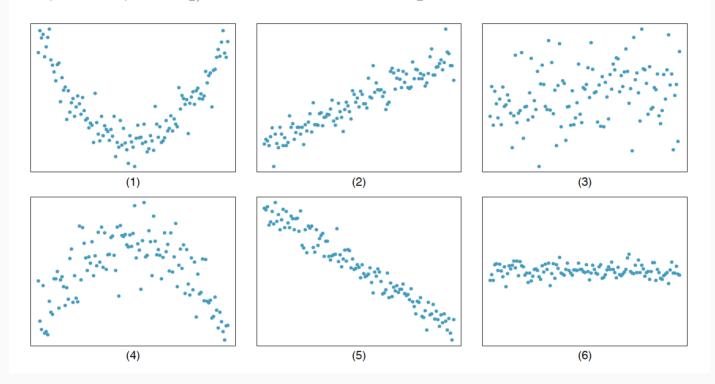
Simple Linear Regression II

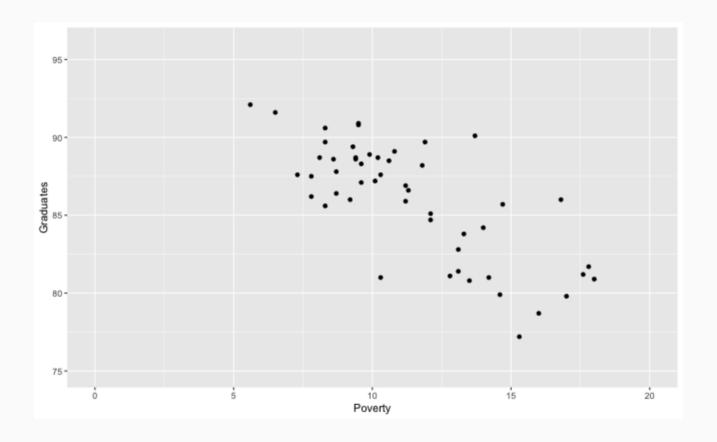
Identify relationships For each of the six plots, identify the strength of the relationship (e.g. weak, moderate, or strong) in the data and whether fitting a linear model would be reasonable.



Finding the best line

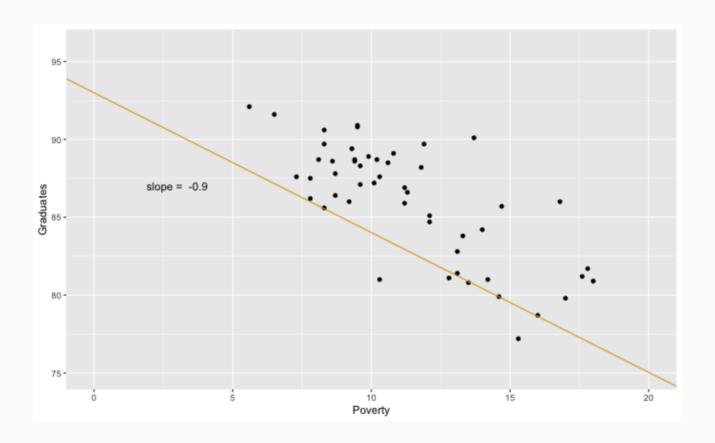
Calculating the least-squares estimates

Estimating eta_1



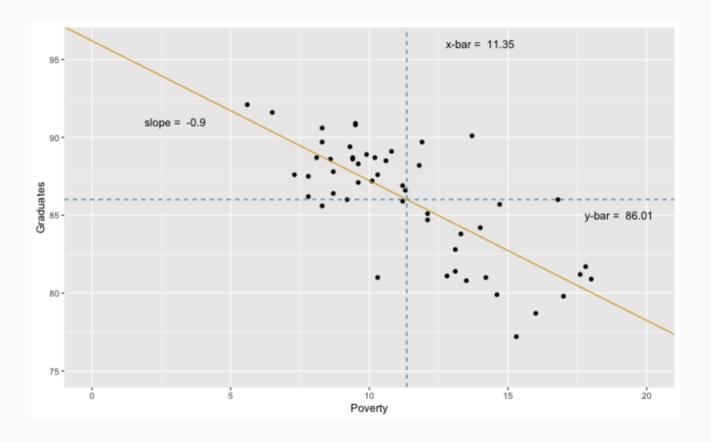
We use s_x, s_y , and R to calculate b_1 .

Estimating eta_1



We use s_x, s_y , and R to calculate b_1 .

Estimating β_0



If the line of best fit *must* pass through (\bar{x}, \bar{y}) , what is b_0 ?

Estimating β_0 , cont.

Since (11.35, 86.01) is on the line, the following relationship holds.

$$86.01 = b_0 - 0.9(11.35)$$

Then just solve for b_0 .

$$b_0 = 86.01 + 0.9(11.35) = 96.22$$

More generally:

$$b_0=ar{y}-b_1ar{x}$$

Estimation in R

```
m1 <- lm(Graduates ~ Poverty, data = poverty)</pre>
summary(m1)
##
## Call:
## lm(formula = Graduates ~ Poverty, data = poverty)
##
## Residuals:
## Min 10 Median 30 Max
## -5.954 -1.820 0.544 1.515 6.199
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 96.202 1.343 71.65 < 2e-16 ***
## Poverty -0.898 0.114 -7.86 3.1e-10 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0
##
## Residual standard error: 2.5 on 49 degrees of freedom
```

The lm object

##

```
attributes(m1)
## $names
                      "residuals" "effects"
## [1] "coefficients"
##
  [7] "qr"
                       "df.residual" "xlevels"
##
## $class
## [1] "lm"
m1$coef
## (Intercept)
                  Poverty
       96.202
                   -0.898
##
m1$fit
```

11

10 10/1811

8

Interpretation of b_1

The **slope** describes the estimated difference in the y variable if the explanatory variable x for a case happened to be one unit larger.

```
m1$coef[2]
## Poverty
## -0.898
```

For each additional percentage point of people living below the poverty level, we expect a state to have a proportion of high school graduates that is 0.898 lower.

Be Cautious: if it is observational data, you do not have evidence of a *causal link*, but of an association, which still can be used for prediction.

Interpretation of b_0

The **intercept** is the estimated y value that will be taken by a case with an x value of zero.

```
m1$coef[1]

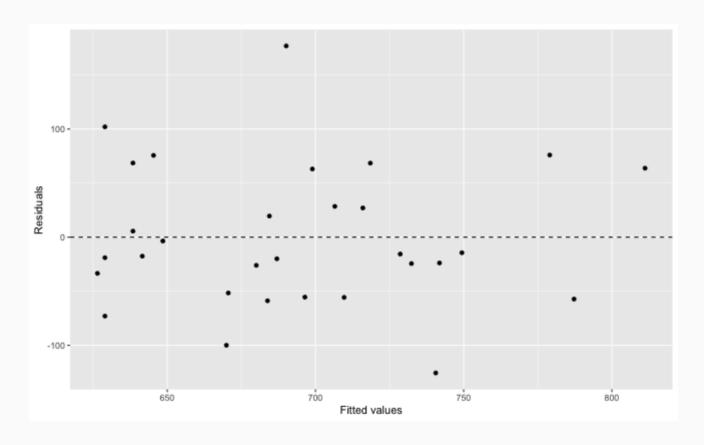
## (Intercept)
## 96.2
```

While necessary for prediction, the intercept often has no meaningful interpretation.

Visualizing the residuals

Residual plot

Residual plot

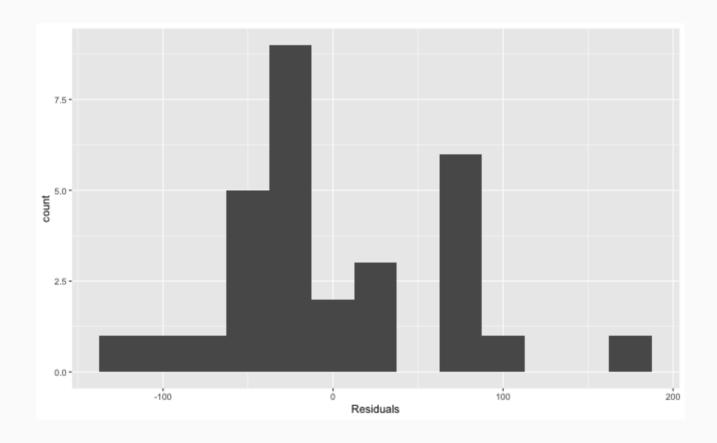


Distribution of the residuals

```
ggplot(m1, aes(x = .resid)) +
  geom_histogram(binwidth = 25) +
  xlab("Residuals")

ggplot(m1, aes(sample = .resid)) +
  geom_point(stat = "qq")
```

Distribution of the residuals



QQ plot

