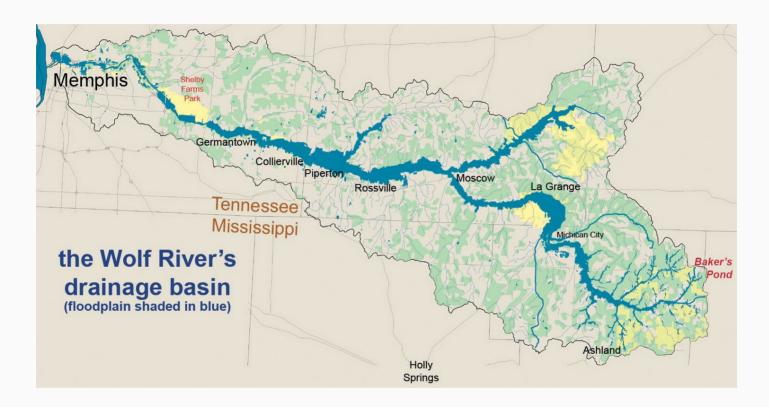
ANOVA

Wolf River



- The Wolf River in Tennessee flows past an abandoned site once used by the pesticide industry for dumping wastes, including hexachlorobenzene (HCB).
- HCB known to cause various cancers and birth defects.

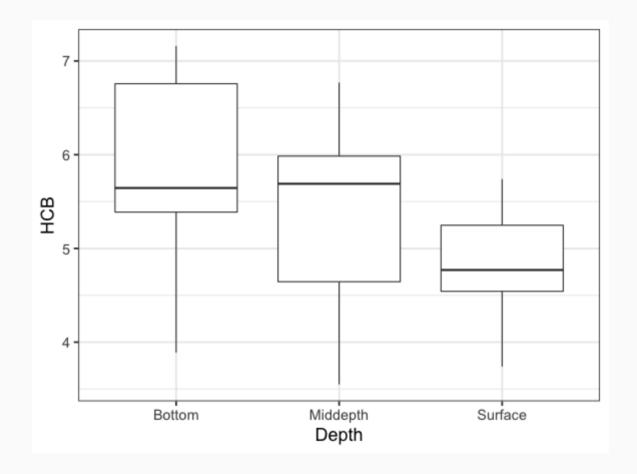
Wolf River study

Depth Aldrin HCB
1 Surface 3.08 3.74

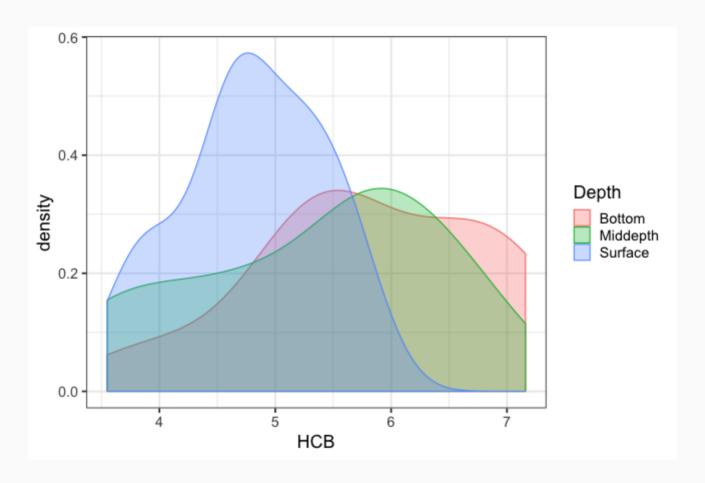
- Standard method to test whether HCB is present in a river is to take samples at middepth.
- HCB is denser than water, so is it found at different concentrations at different depths?

```
## 'data.frame': 30 obs. of 3 variables:
## $ Depth : Factor w/ 3 levels "Bottom","Middepth",..:
## $ Aldrin: num 3.08 3.58 3.81 4.31 4.35 4.4 3.67 5.17
## $ HCB : num 3.74 4.61 4 4.67 4.87 5.12 4.52 5.29 5
head(wolf)
```

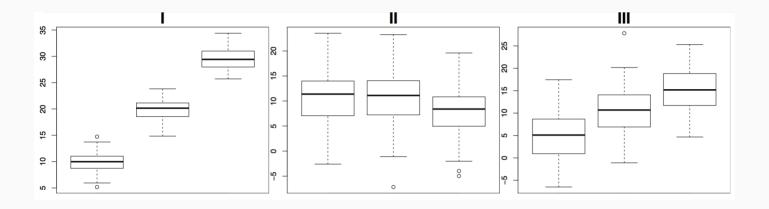
Wolf River data



Wolf River data, cont.



Which of the following plots shows groups with means that are *most* and *least* likely to be significantly different from each other?



1. most: I, least: II

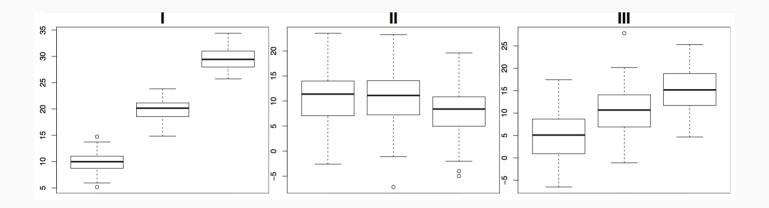
2. most: II, least: III

3. most: I, least: III

4. most: III, least: II

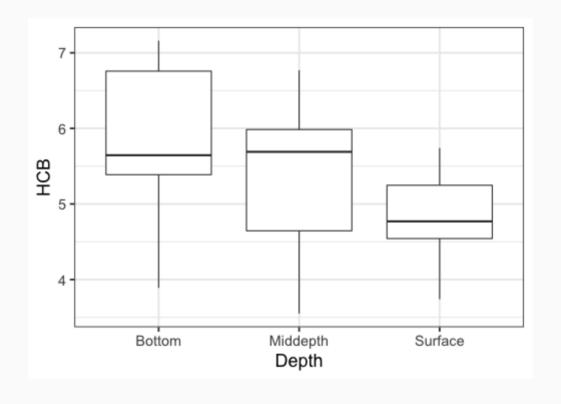
boardwork

Which of the following plots shows groups with means that are *most* and *least* likely to be significantly different from each other?



- I has a high F.
- II has a low F.
- III has a middling F.

Wolf River data



```
## Depth 2 5.36 2.678 3.03 ## Residuals 27 23.85 0.883
```

How big is 3.032?

ANOVA F-test

$$H_0: \mu_1=\mu_2=\ldots=\mu_k$$

 H_A : At least one μ_j is different

We can find the distribution of the F-statistic under the null hypothesis by

- Randomization
- Mathematical approximation

Sampling dist for F via Randomization

```
wolf %>%
  specify(response = HCB, explanatory = Depth) %>%
  hypothesize(null = "independence") %>%
  generate(reps = 1000, type = "permute") %>%
  calculate(stat = "F")
```

```
## # A tibble: 1,000 x 2
     replicate stat
##
##
        <int> <dbl>
## 1
            1 0.228
## 2
            2 1.83
## 3
            3 0.672
## 4
            4 0.237
##
   5
            5 0.501
##
  6
       6 1.67
## 7
            7 1.53
##
            8 1.03
##
   9
            9 0.228
           10 2.03
##
  10
```

Sampling dist for F via Randomization, cont.

Sampling dist for F via Approximation

If:

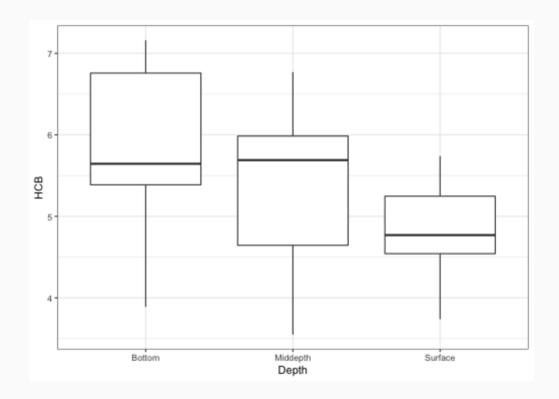
- 1. Independent observations.
- 2. Approximate normal distributions within groups.
- 3. Constant variance between groups.

Then the sampling distribution for the F statistic under the H_0 is well approximated by an F distribution with $df_1 = k - 1$ and $df_2 = N - k$. The p-value is represented by the upper tail.

Sampling dist for F via Approximation, cont.

```
qplot(x = F_stats, geom = "density") +
  stat_function(fun = df, args = c(df1 = 2, df2 =
```

Wolf River Conclusions



- With a p-value of ≈ 0.07 , it is questionable whether HCB concentration functions the same at all three depths.
- *Replicating the study* could add some certainty.
- In a subsequent study, we may wish to only test middepth versus bottom.