infer

an R package for tidy statistical inference

Andrew Bray

infer.netlify.com

infer makes p-values easier to compute.

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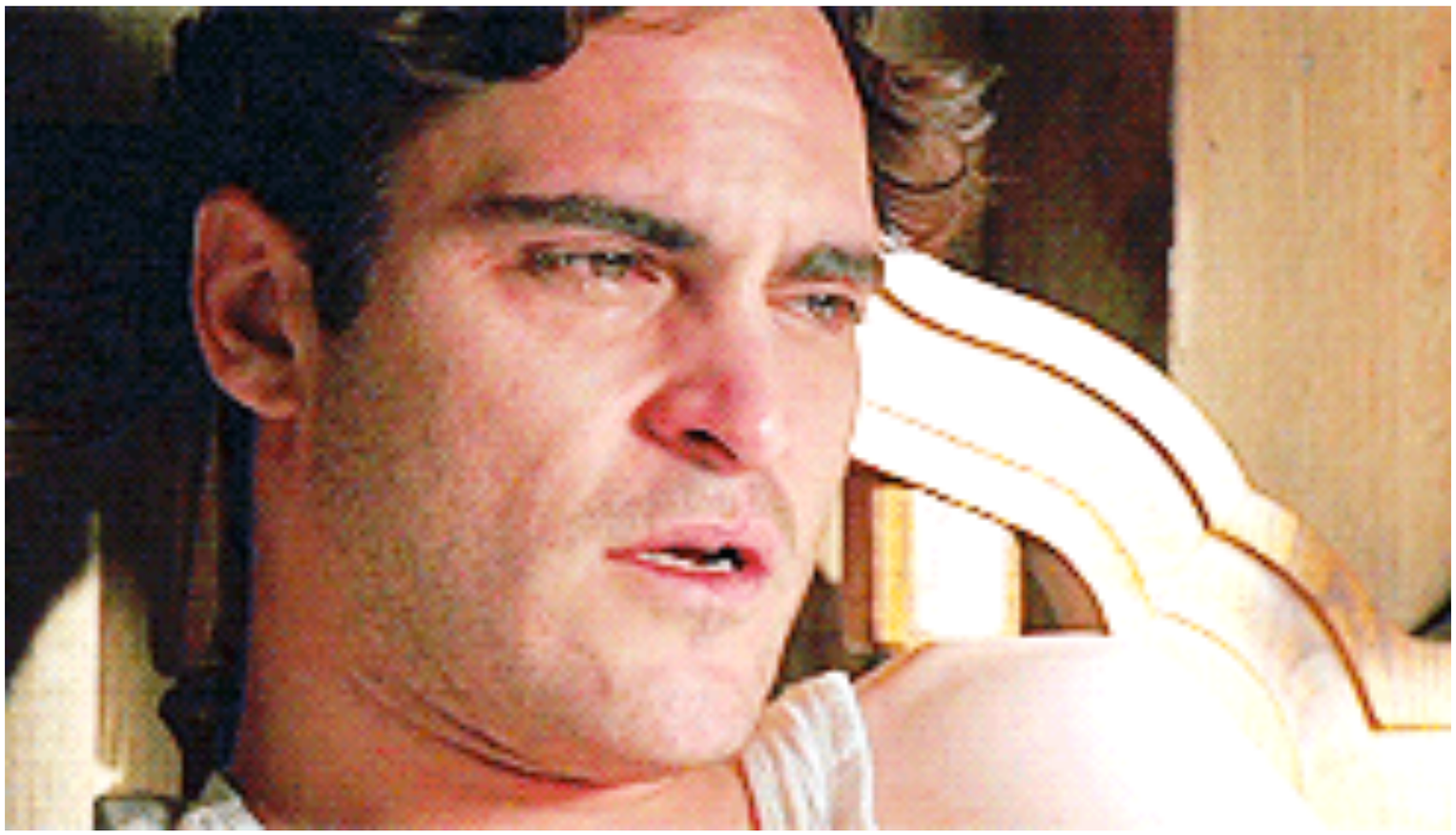

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statistical inference

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tidy and transparent.

statistical inference

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```
chisq.test(gss$party, gss$NASA)
```

```
gss %>%
  specify(NASA ~ party) %>%
  hypothesize(null = "independence") %>%
  generate(reps = 1000, type = "permute") %>%
  calculate(stat = "Chisq")
```

statistical inference

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tidy and transparent.

Case study: Is funding for space exploration a partisan issue?

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```
library(tidyverse)
load(url("http://bit.ly/2E65g15"))
names(gss)
```

```
 [1] "id"       "year"     "age"      "class"    "degree"
 [6] "sex"      "marital"  "race"     "region"   "partyid"
[11] "happy"    "relig"    "cappun"   "finalter" "natspac"
[16] "natarms"  "conclerg" "confed"   "conpress" "conjudge"
[21] "consci"   "conlegis" "zodiac"   "oversamp" "postlife"
[26] "party"    "space"    "NASA"
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```
select(gss, party, NASA)
```

```
# A tibble: 149 x 2
   party NASA
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Case study: Is funding for space exploration a partisan issue?

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ggplot(gss, aes(x = party, fill = NASA)) +
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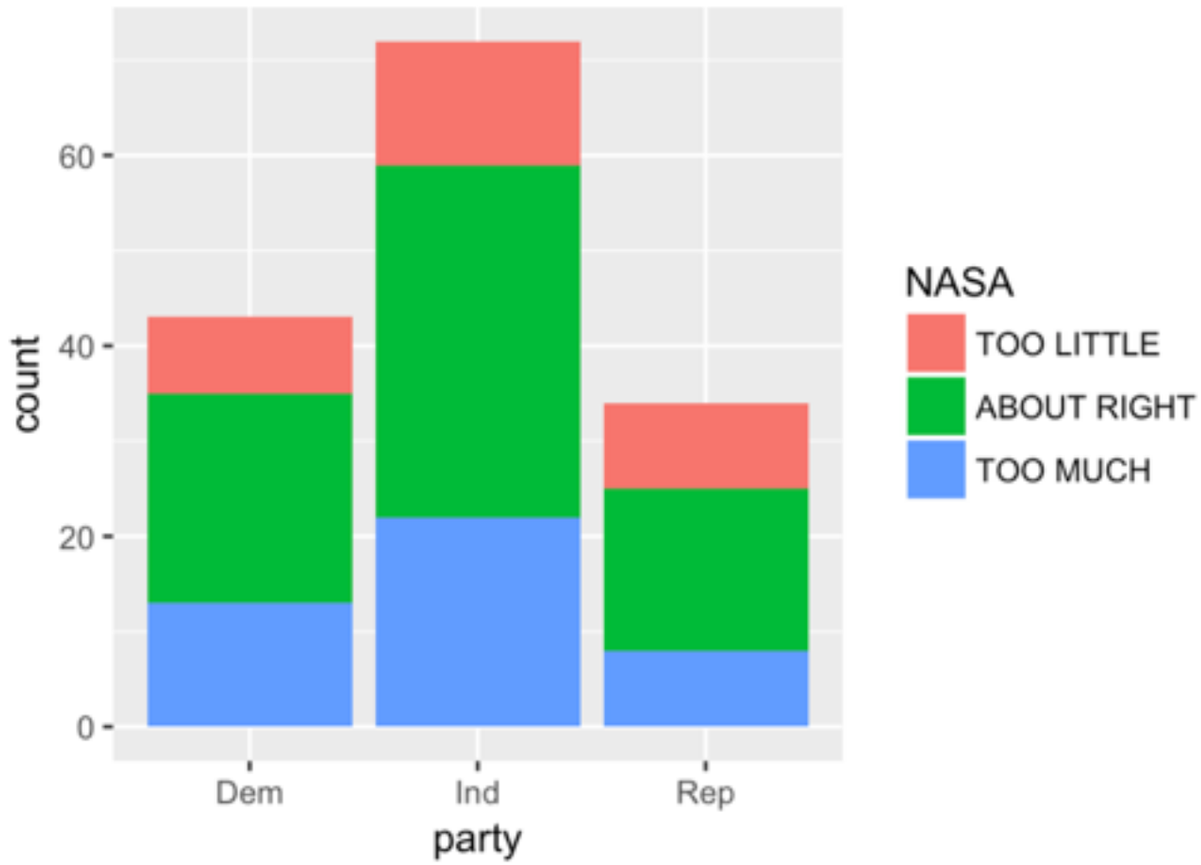
```



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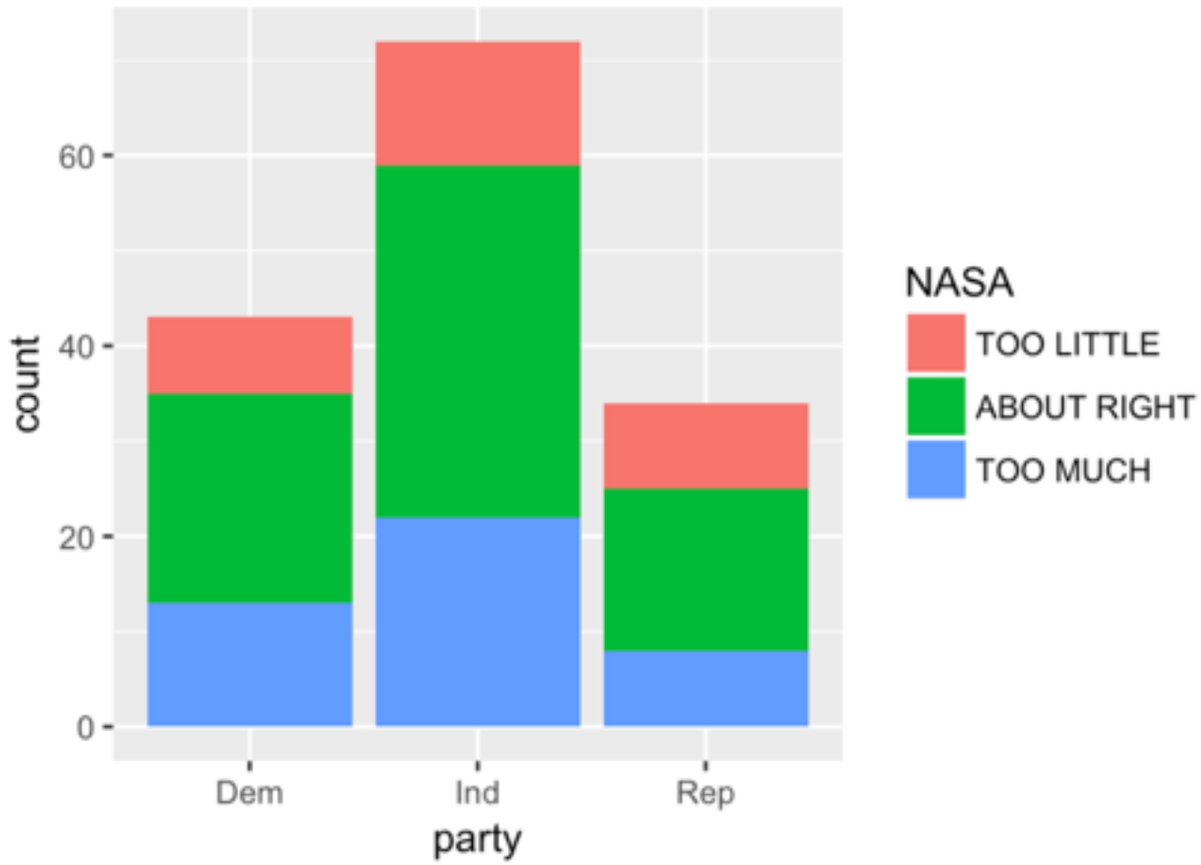

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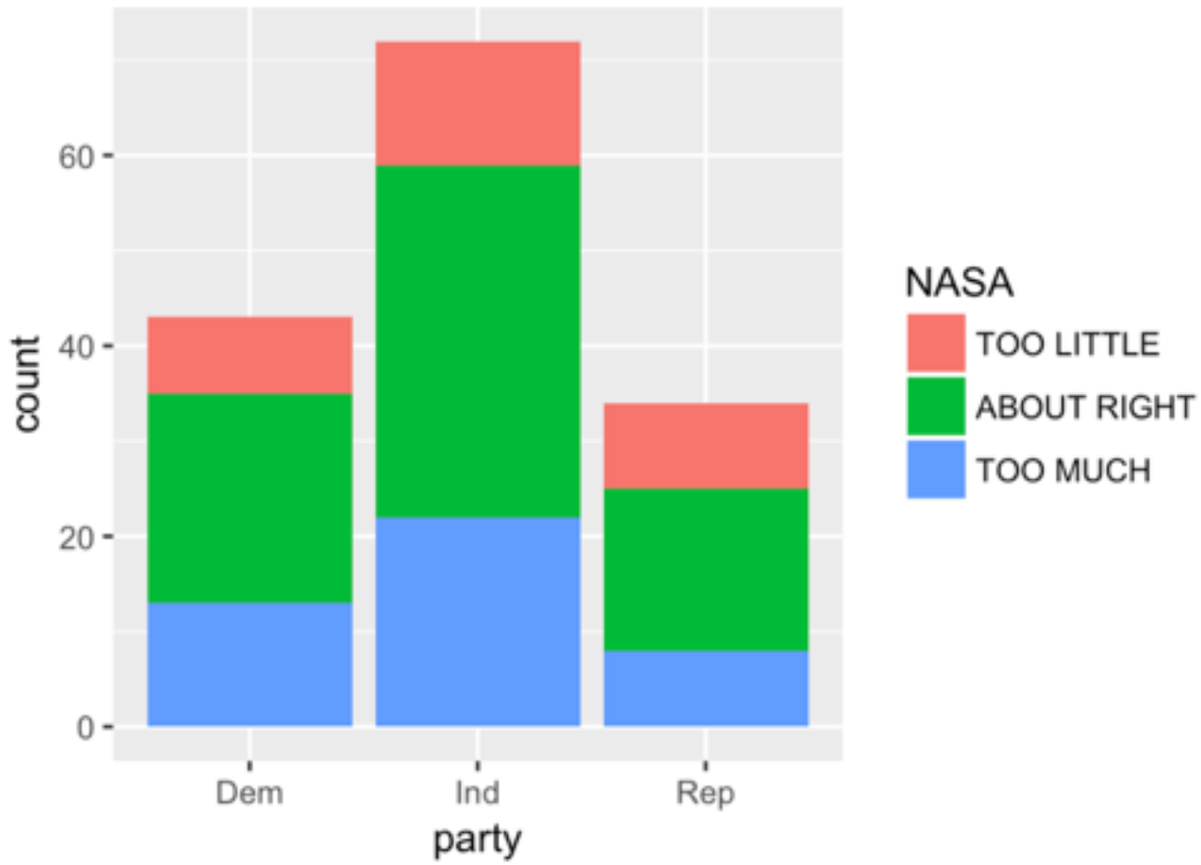
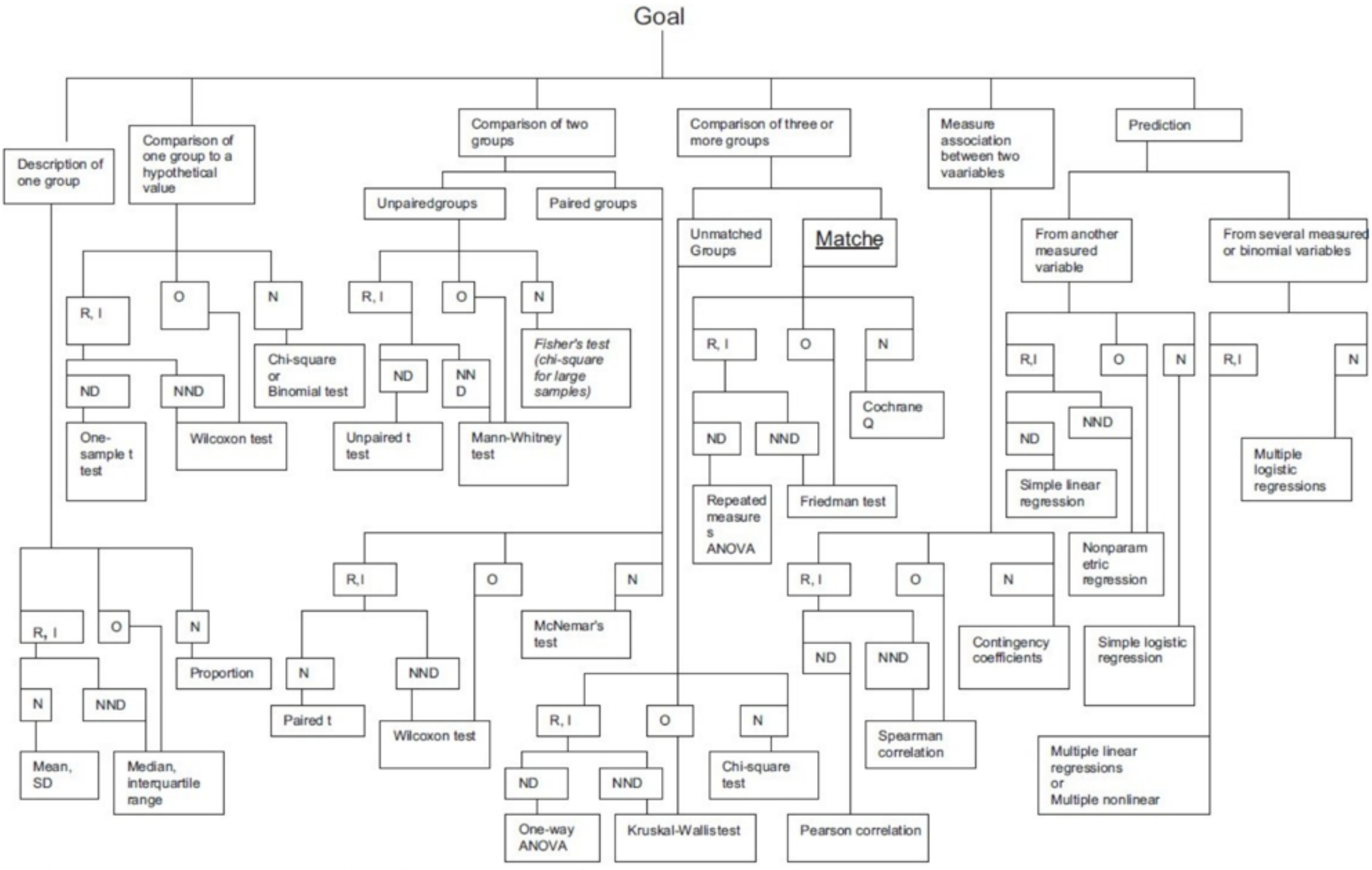


How can we test to see if the structure that we see is *significant*?

Run a hypothesis test!


Goal
Description of one group
Comparison of one group to a hypothetical value
Comparison of two groups
Comparison of three or more groups
Measure association between two vaariables
Prediction
R, I
O
N
ND
NND
One-sample t test
Wilcoxon test
Chi-square or Binomial test
Unpairedgroups
Paired groups
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NND
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Fisher's test (chi-square for large samples)
Unmatched Groups
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O
N
ND
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Repeated measures ANOVA
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Cochrane Q
From another measured variable
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Multiple logistic regressions
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Mean, SD
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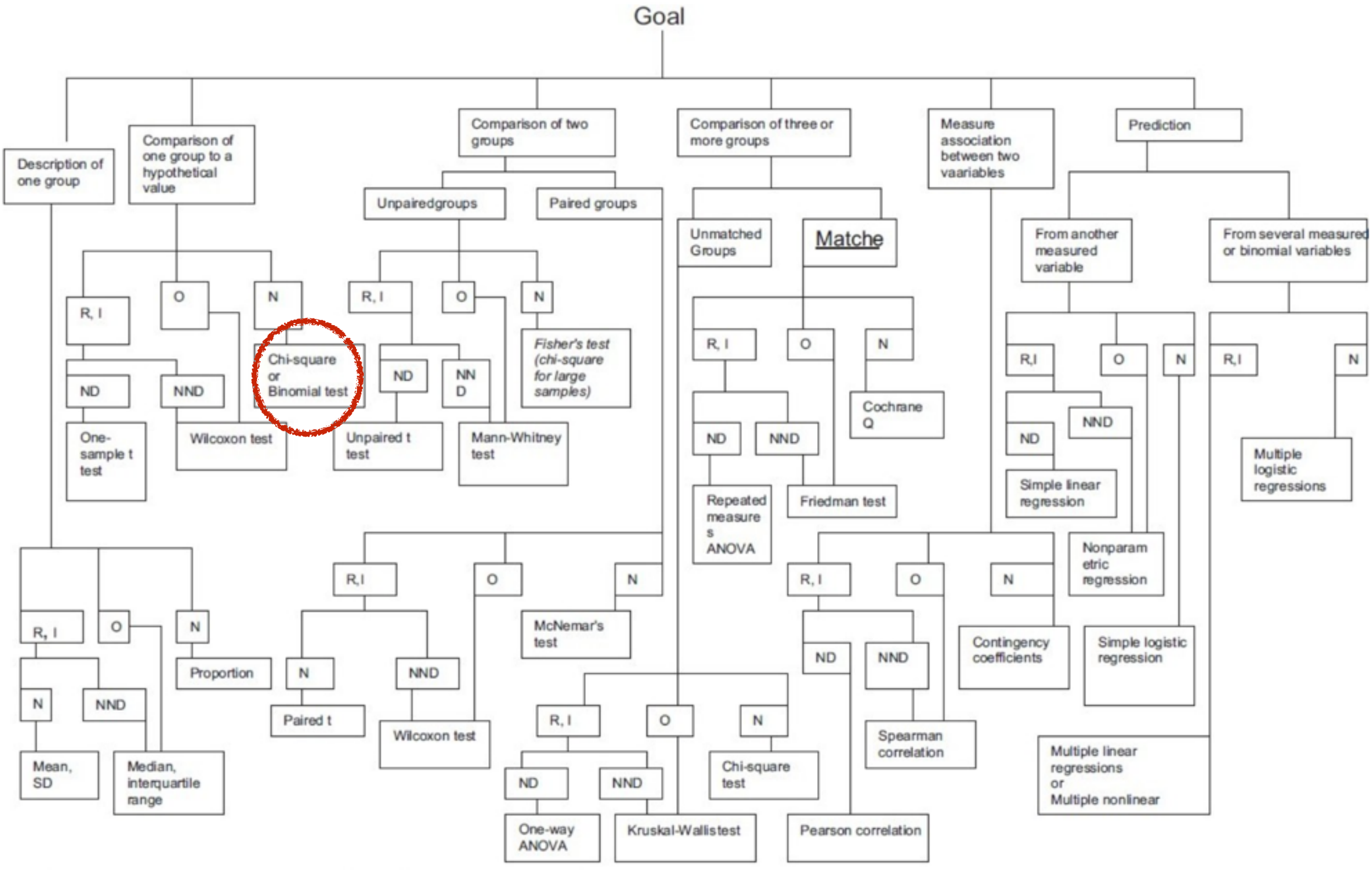
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Optimistic effort I

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```
chisq.test(data = gss, x = party, y = NASA)
```

```
Error in chisq.test(data = gss, x = party, y = NASA) :
  unused argument (data = gss)
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```
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. . . optimistic effort II

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chisq.test(NASA ~ party, data = gss)
```

```
Error in chisq.test(data = gss, x = party, y = NASA) :
  unused argument (data = gss)
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Optimistic effort I

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chisq.test(data = gss, x = party, y = NASA)
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. . . optimistic effort II

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chisq.test(NASA ~ party, data = gss)
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…after looking at the help file

```
chisq.test(gss$party, gss$NASA)
```

```
        Pearson's Chi-squared test

data:  gss$party and gss$NASA
X-squared = 1.3261, df = 4, p-value = 0.8569
```

chisq.test

From stats v3.4.3
by R-core R-core@R-project.org

Pearson's Chi-Squared Test For Count Data

`chisq.test` performs chi-squared contingency table tests and goodness-of-fit tests.

Keywords distribution, htest

Usage

```
chisq.test(x, y = NULL, correct = TRUE,
           p = rep(1/length(x), length(x)), rescale.p = FALSE,
           simulate.p.value = FALSE, B = 2000)
```

Arguments

x	a numeric vector or matrix. `x` and `y` can also both be factors.
y	a numeric vector; ignored if `x` is a matrix. If `x` is a factor, `y` should be a factor of the same length.

t.test

From stats v3.4.3
by R-core R-core@R-project.org

Student's T-Test

Performs one and two sample t-tests on vectors of data.

Keywords htest

Usage

```
t.test(x, …)

# S3 method for default
t.test(x, y = NULL,
       alternative = c("two.sided", "less", "greater"),
       mu = 0, paired = FALSE, var.equal = FALSE,
       conf.level = 0.95, …)

# S3 method for formula
t.test(formula, data, subset, na.action, …)
```

Arguments

x	a (non-empty) numeric vector of data values.
y	an optional (non-empty) numeric vector of data values.

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Two paradigms

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Mathematical Approximation

- Chi-squared
- Student t
- Normal

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Computational

- Permutation
- Bootstrap

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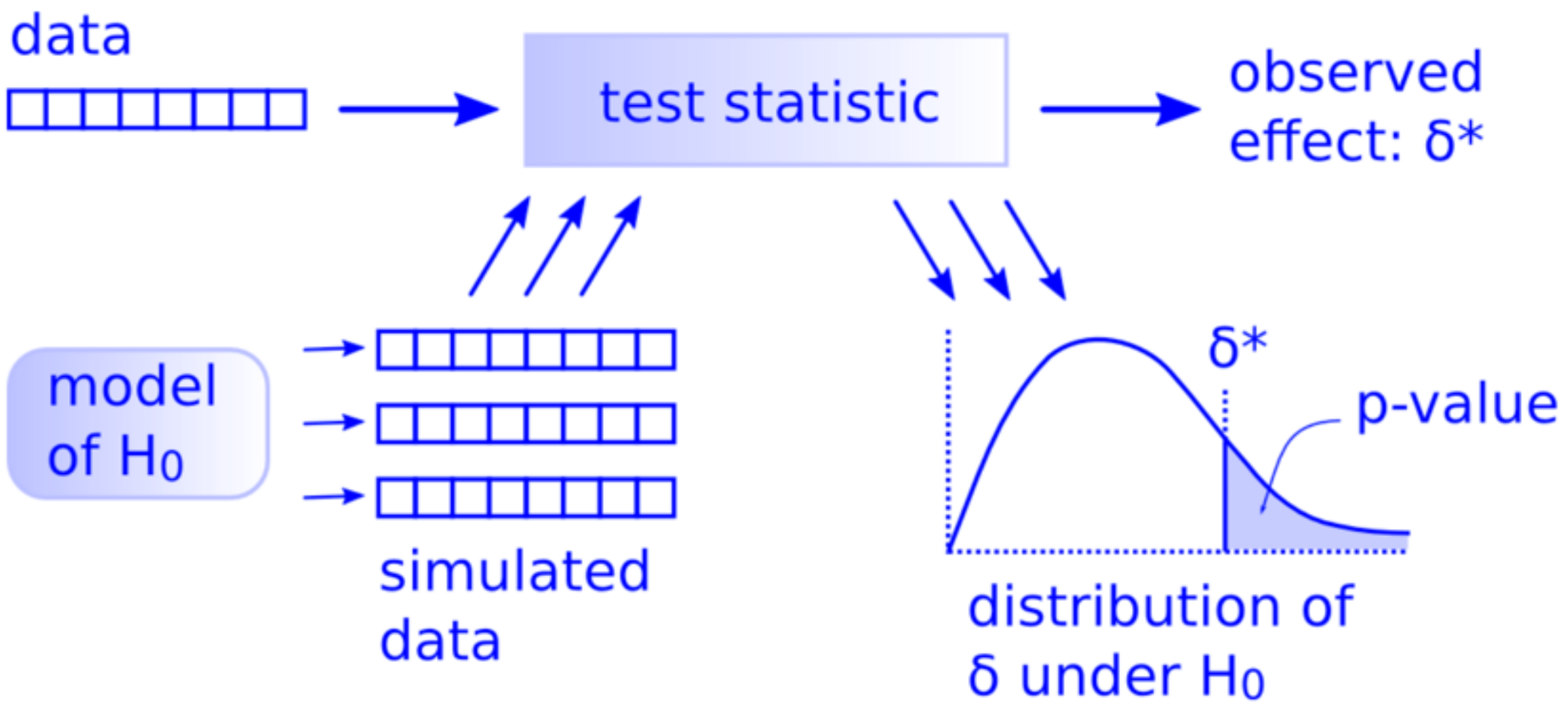
There is only one test

- Allen Downey



Simulation through Permutation

If we live in world where these variables are totally unrelated, the ties between variables are arbitrary, so they might just as well have been shuffled.

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select(gss, party, NASA)
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 4 Ind   TOO LITTLE
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 7 Ind   ABOUT RIGHT
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 9 Dem   TOO LITTLE
10 Ind   TOO LITTLE
# ... with 139 more rows
```

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```
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  mutate(perm = sample(NASA)) %>%
  select(party, perm)
```

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Test statistic

Chi-squared statistic: a measure of the difference between your data and what you would expect if the null hypothesis were true.

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```
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1.32606
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```
chisq.test(gss$party, gss$perm1)$stat
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chisq.test(gss$party, gss$perm2)$stat
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X-squared
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X-squared
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```
X-squared
  5.306025
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chisq.test(gss$party, gss$perm2)$stat
```

```
X-squared
  1.121982
```

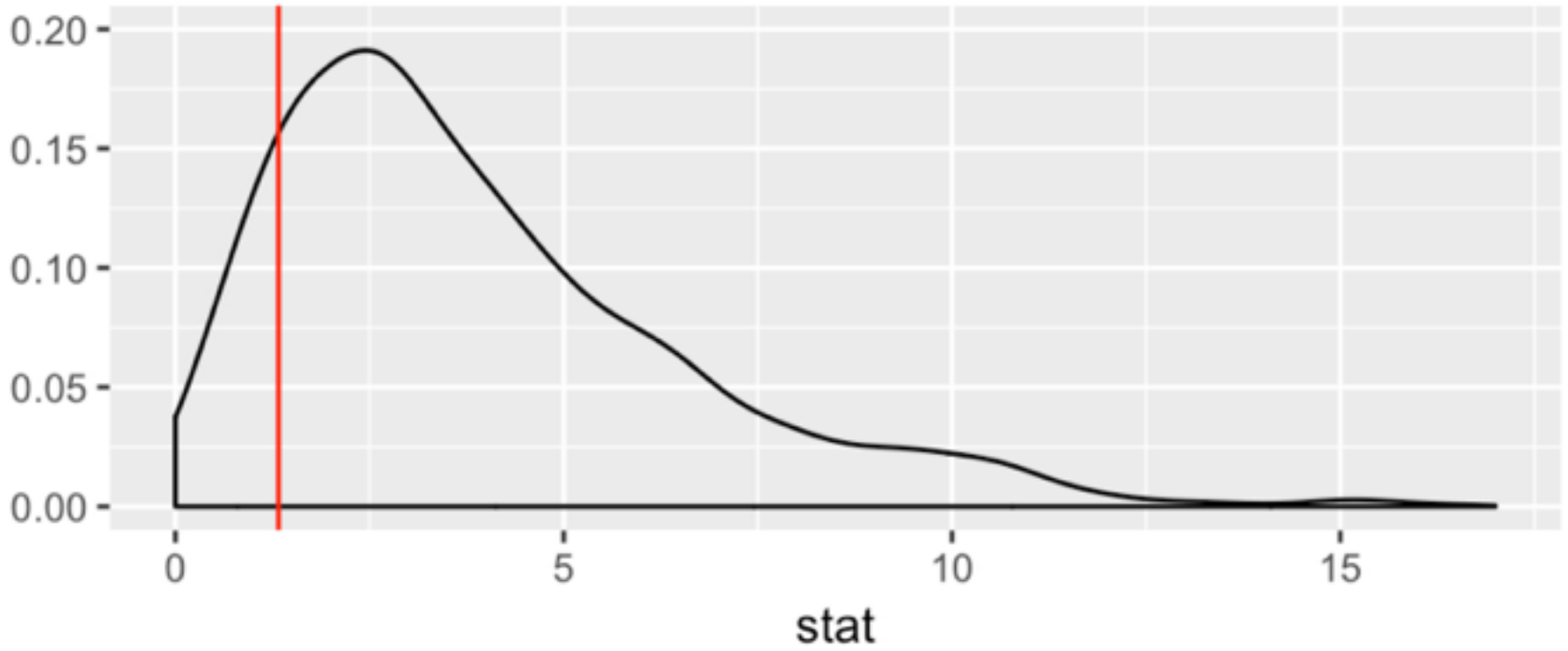
```
chisq.test(gss$party, gss$perm3)$stat
```

```
X-squared
  2.824082
```

Distribution of statistic

Distribution of statistic

via permutation



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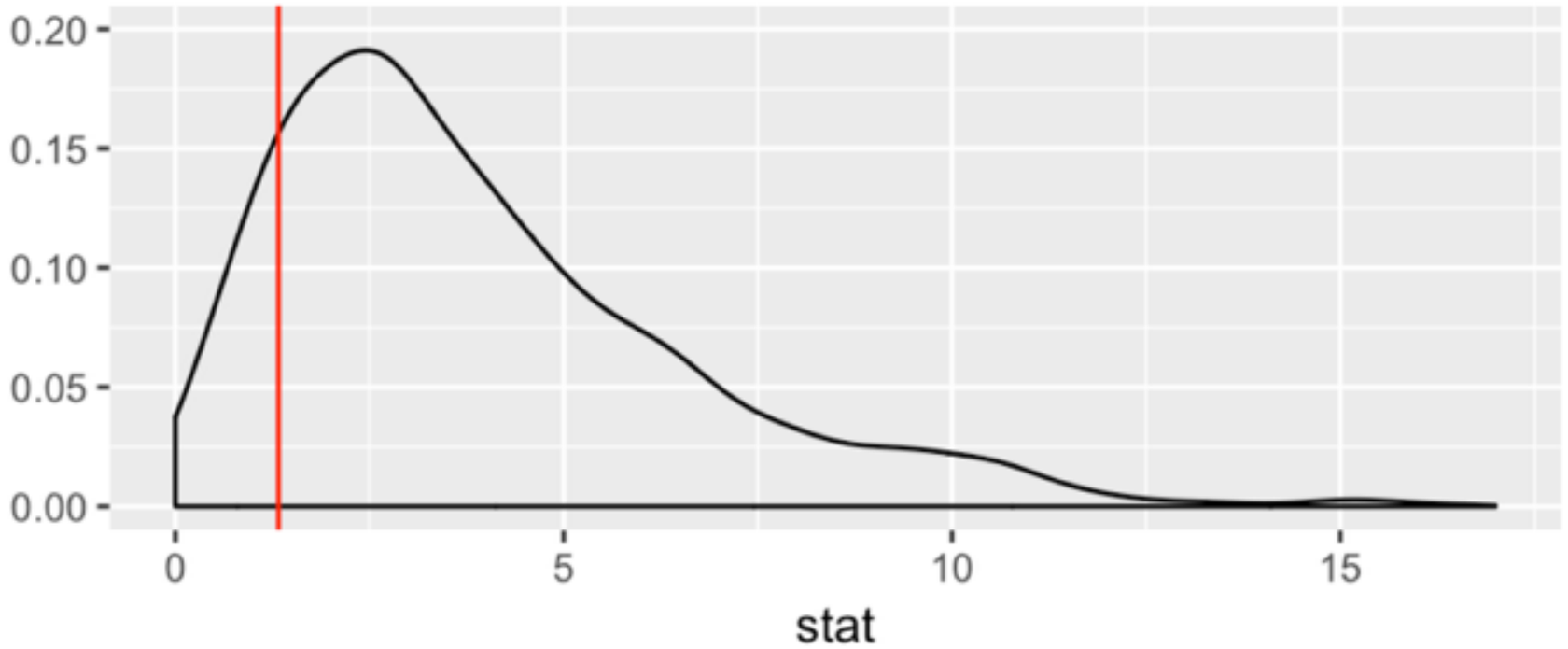

Question: Is funding for space exploration a partisan issue?

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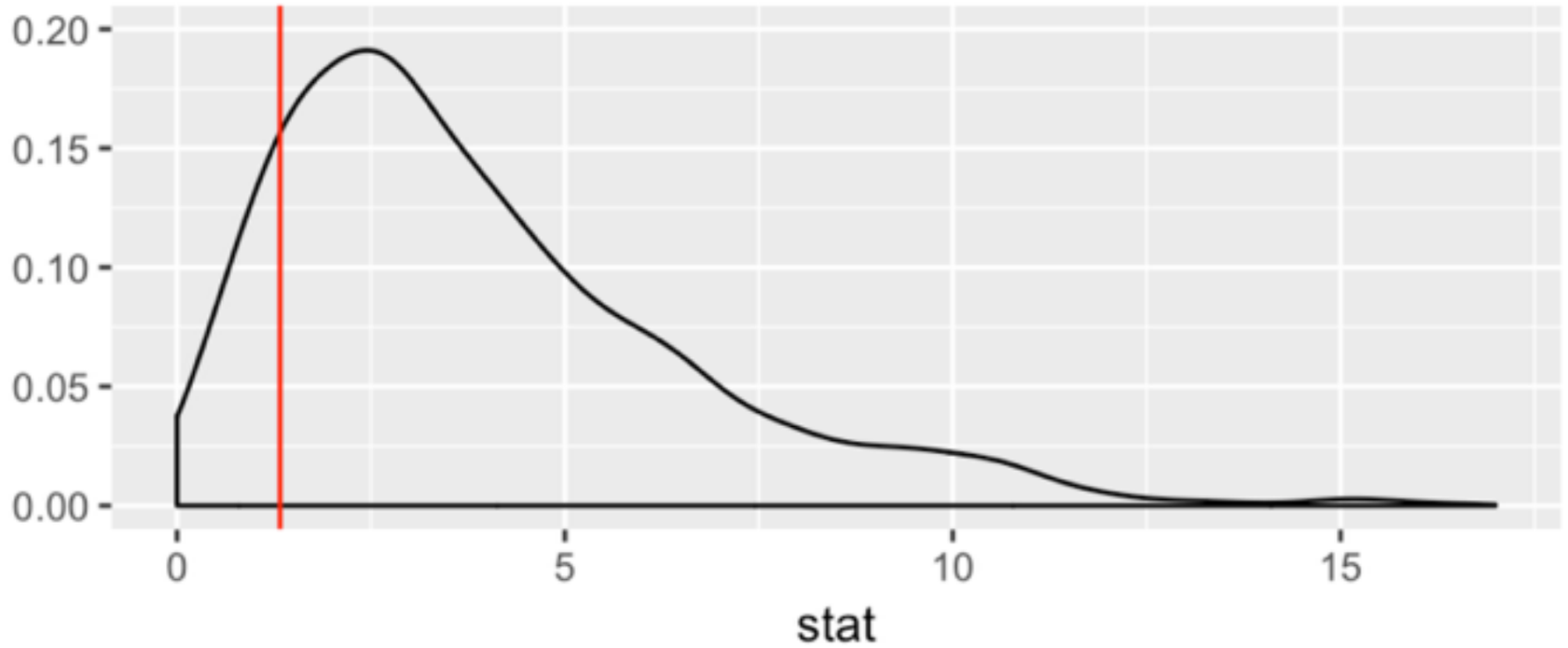

Question: Is funding for space exploration a partisan issue?

Answer: The GSS data is consistent with the model that there is no association between party and space funding.

Distribution of statistic

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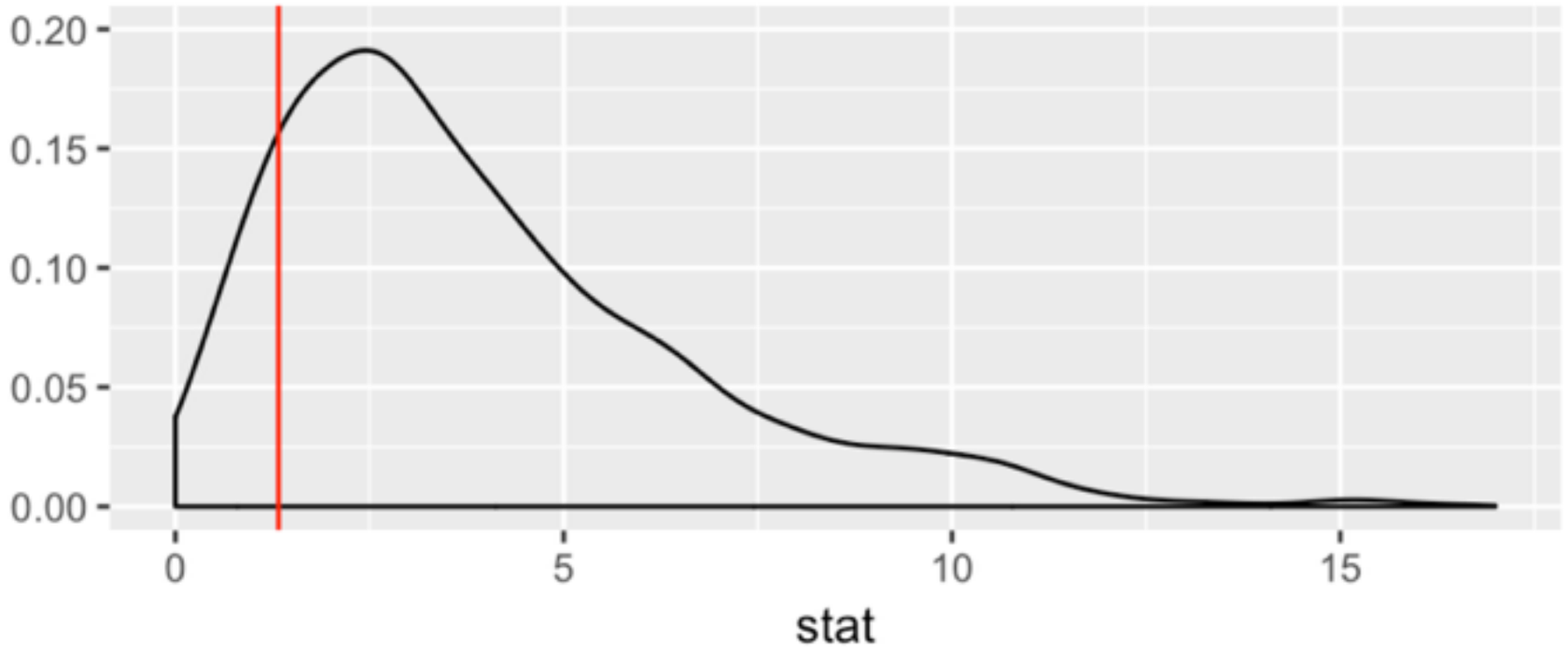

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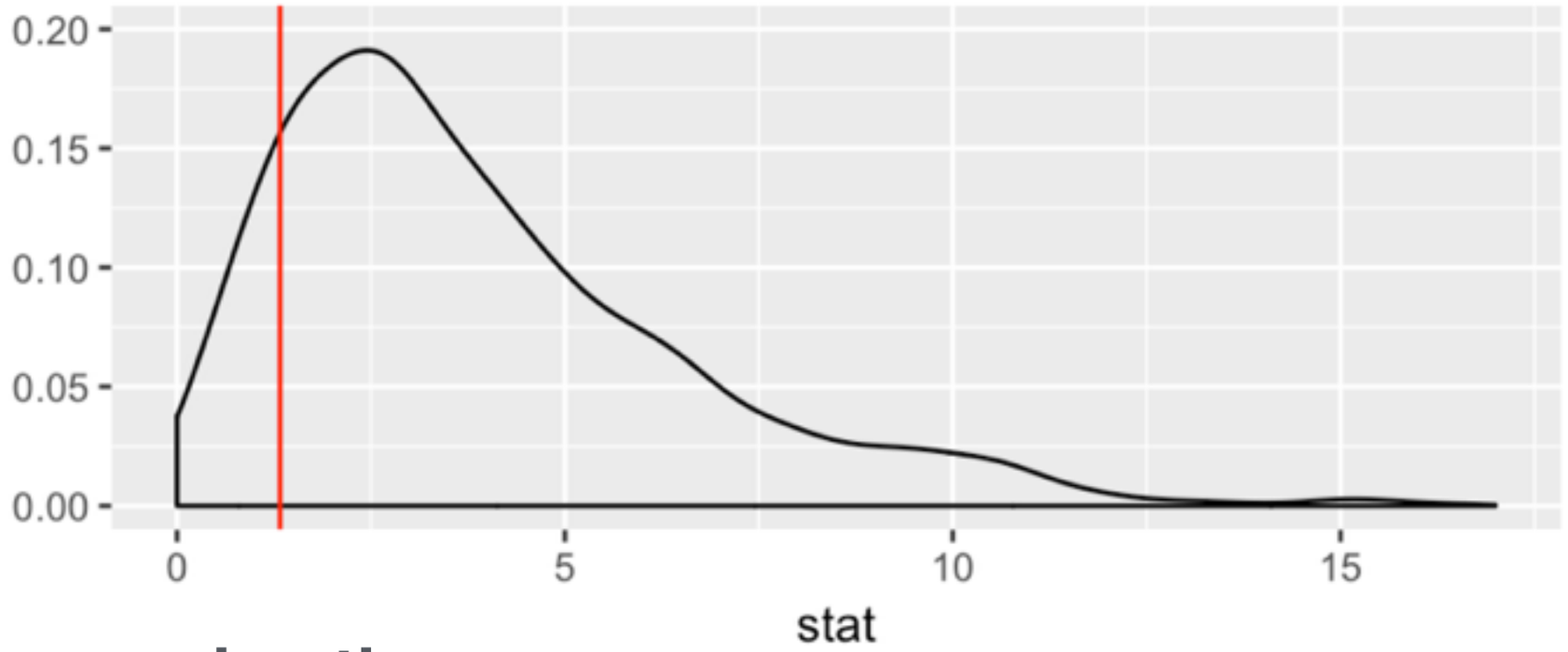
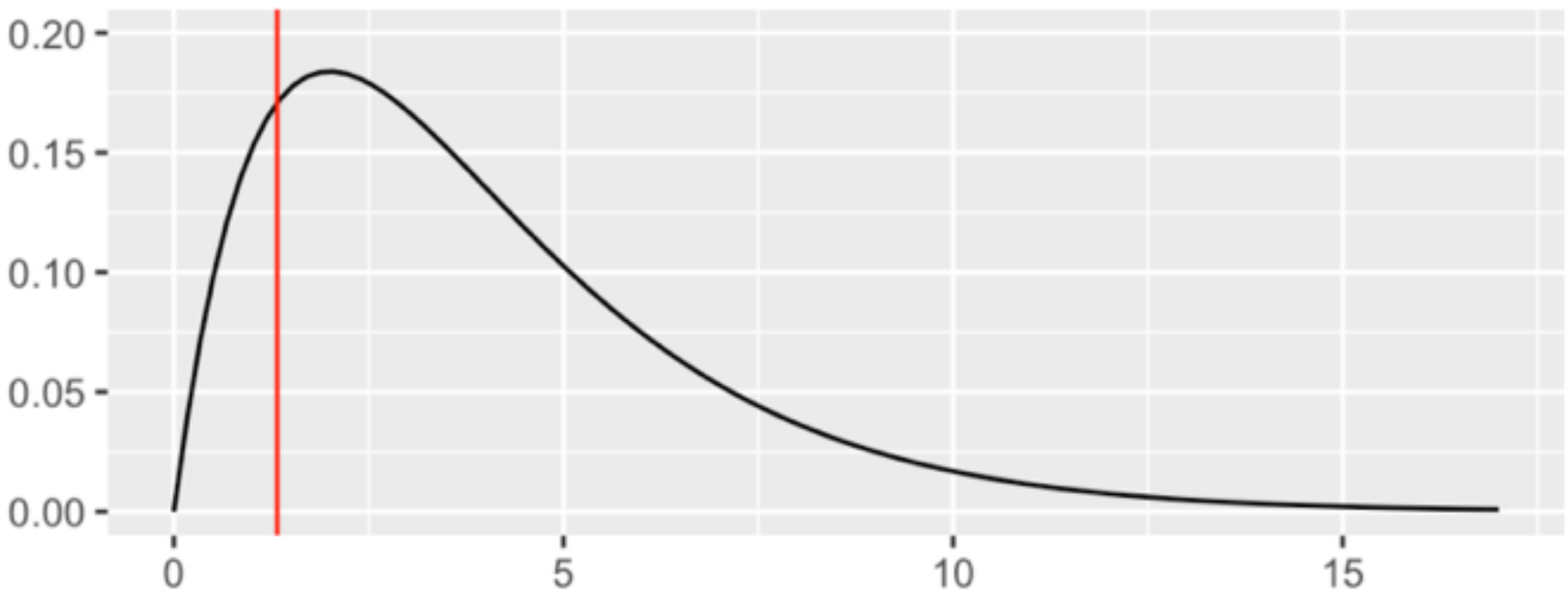


via approximation



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- dataframe in, dataframe out

infer makes statistical inference tidy and transparent.

- dataframe in, dataframe out
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The `infer` verbs

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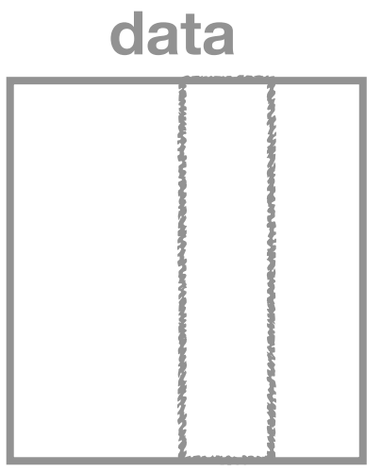

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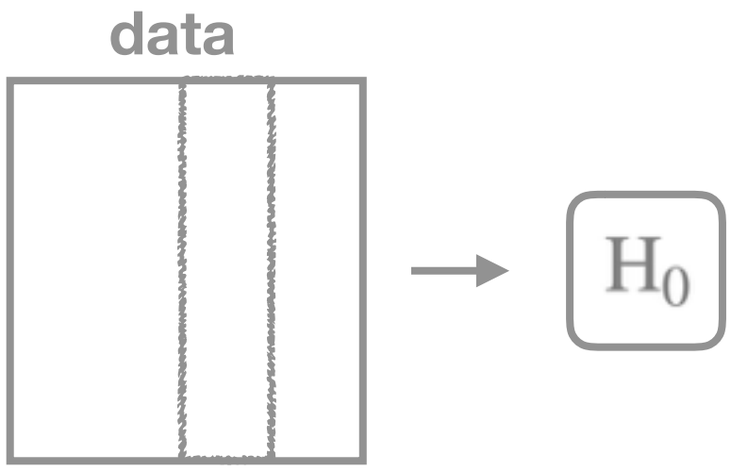

`specify()`

`hypothesize()`

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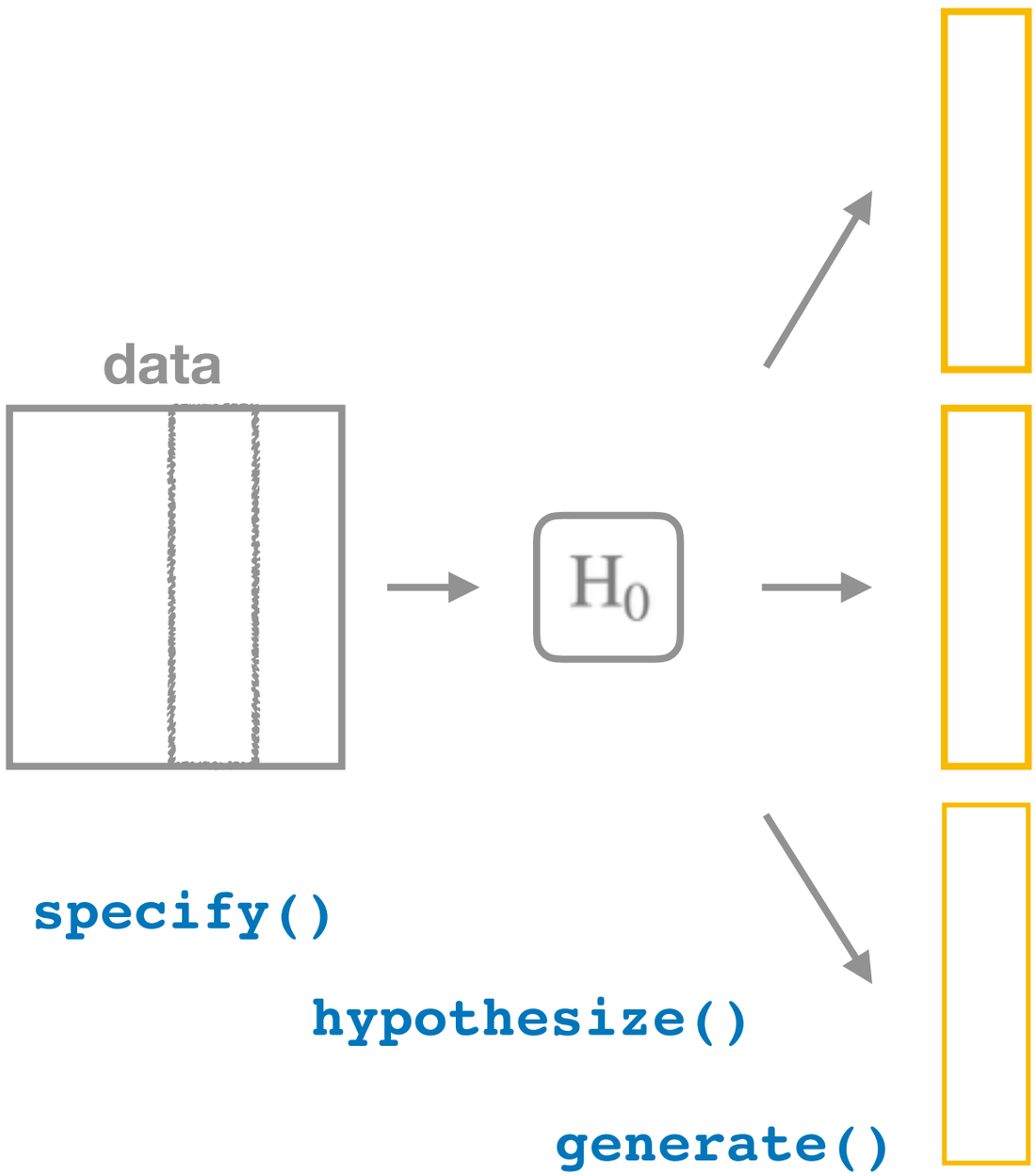

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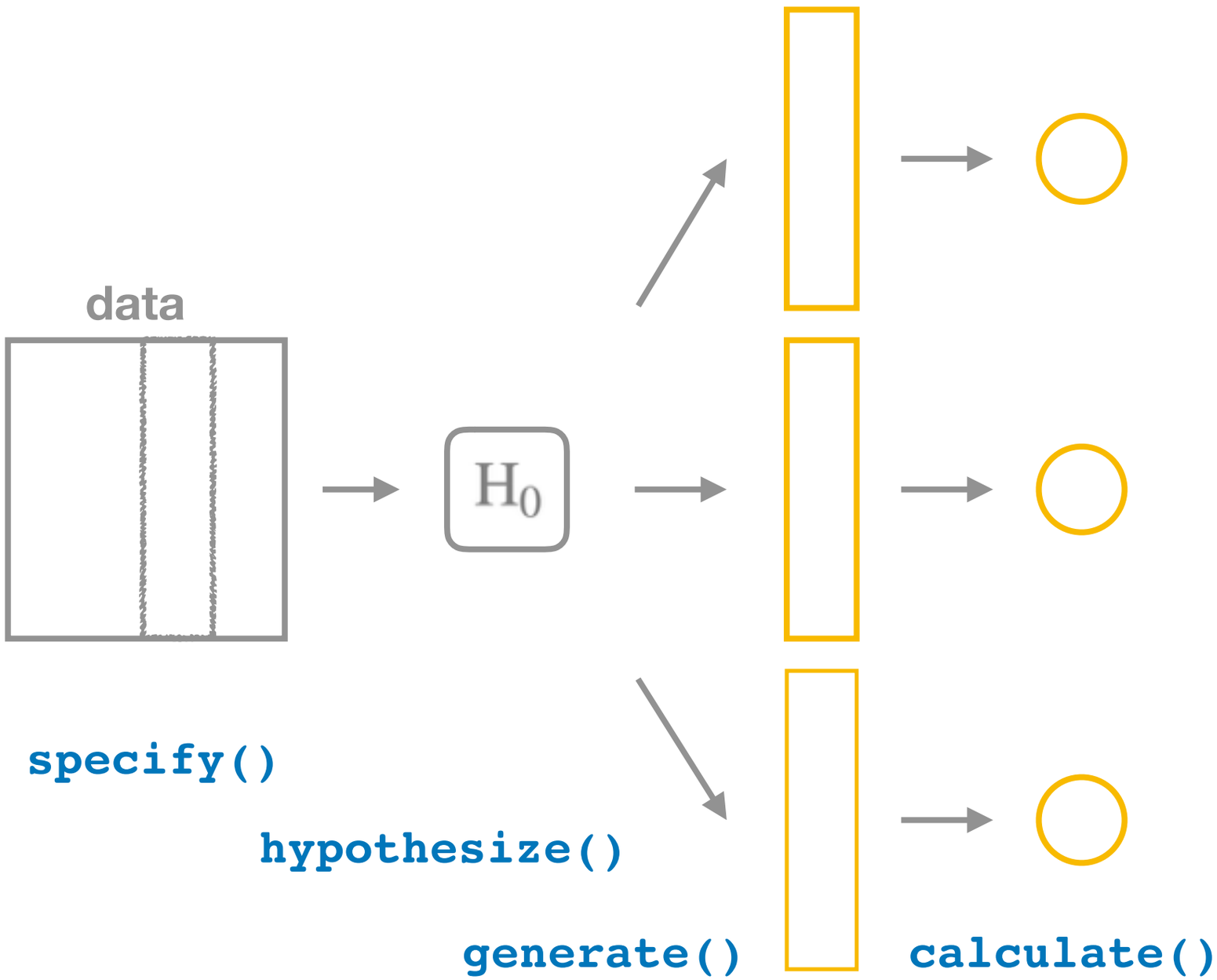

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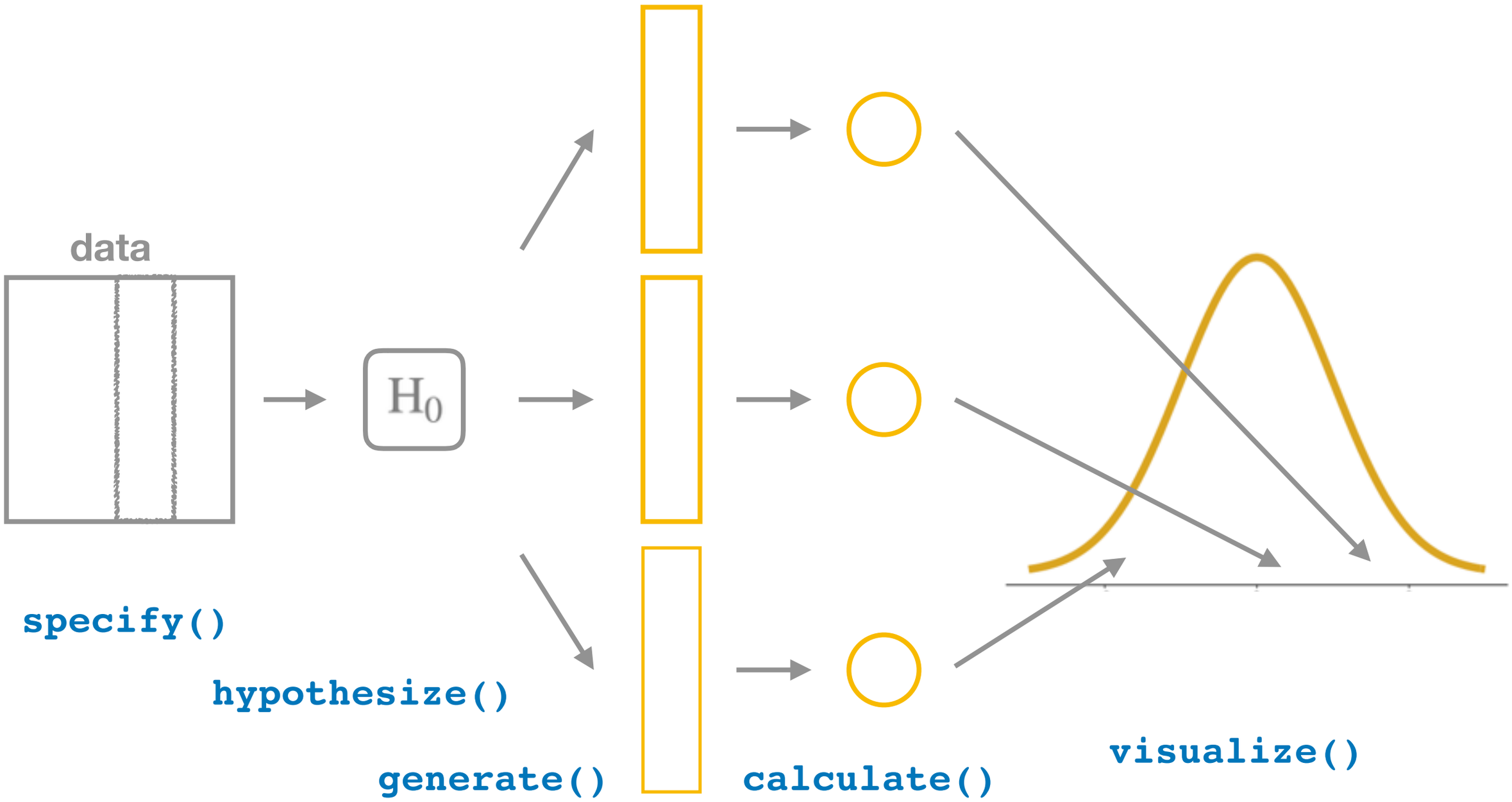

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```

```
# A tibble: 1,000 x 2
   replicate   stat
   <fct>      <dbl>
 1 1          0.163
 2 2          7.49
 3 3          0.817
 4 4          7.25
 5 5         12.0
 6 6          3.59
 7 7          3.11
 8 8          3.40
 9 9          0.870
10 10         4.21
# ... with 990 more rows
```

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  specify(NASA ~ party) %>%
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  calculate(stat = "Chisq") %>%
  visualize()
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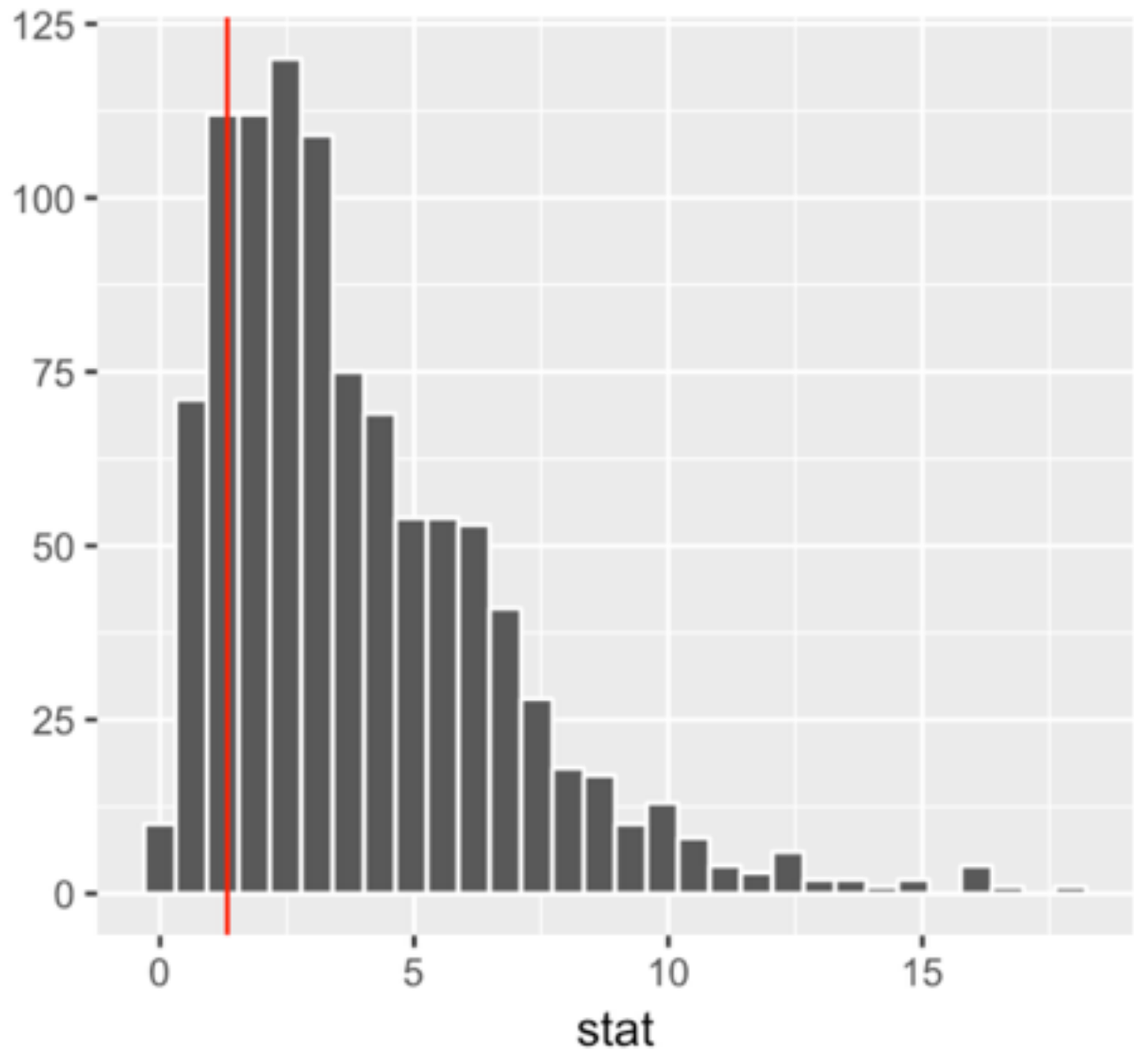

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  calculate(stat = "Chisq") %>%
  summarize(p_val = mean(stat > obs_stat))
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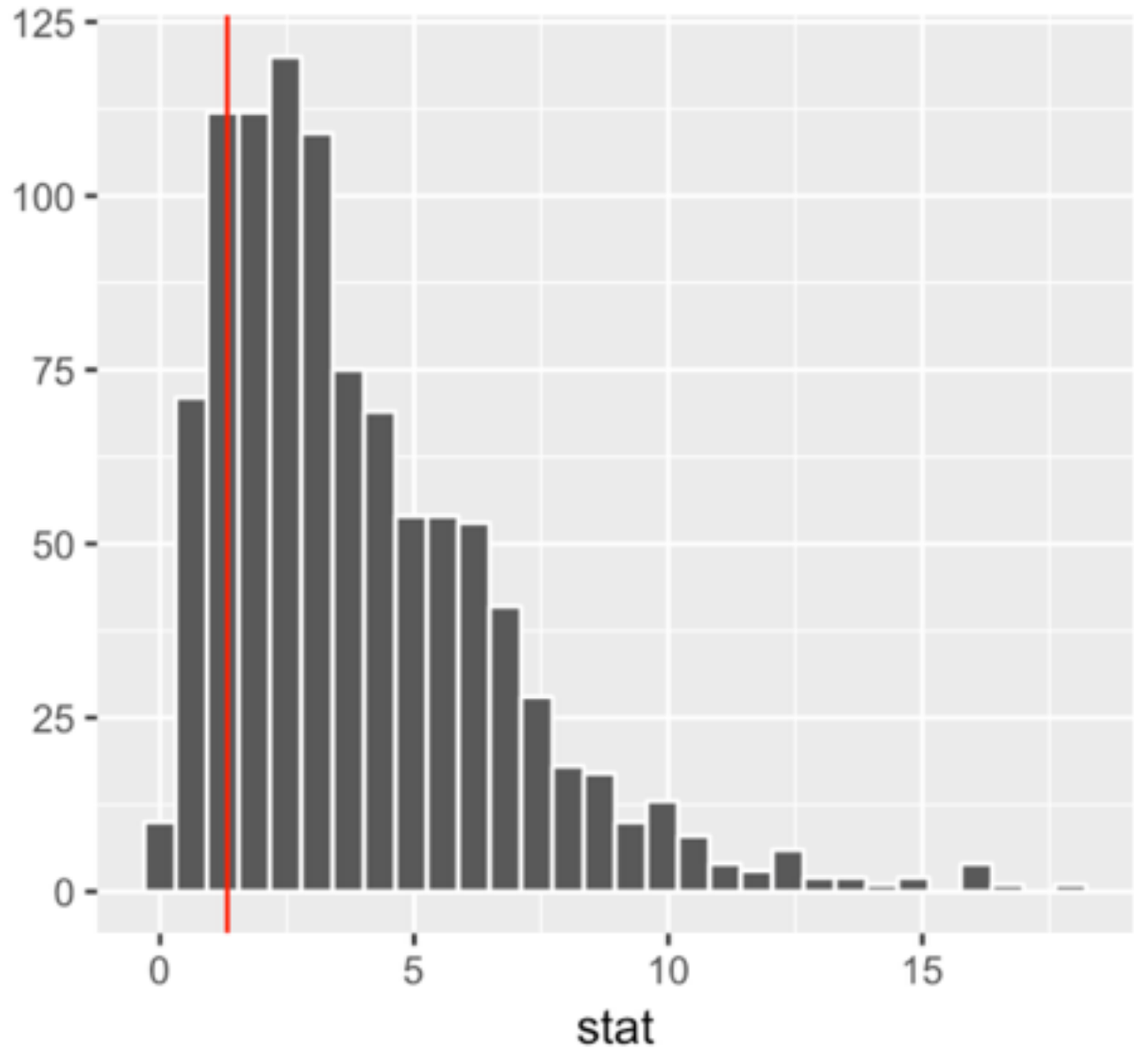

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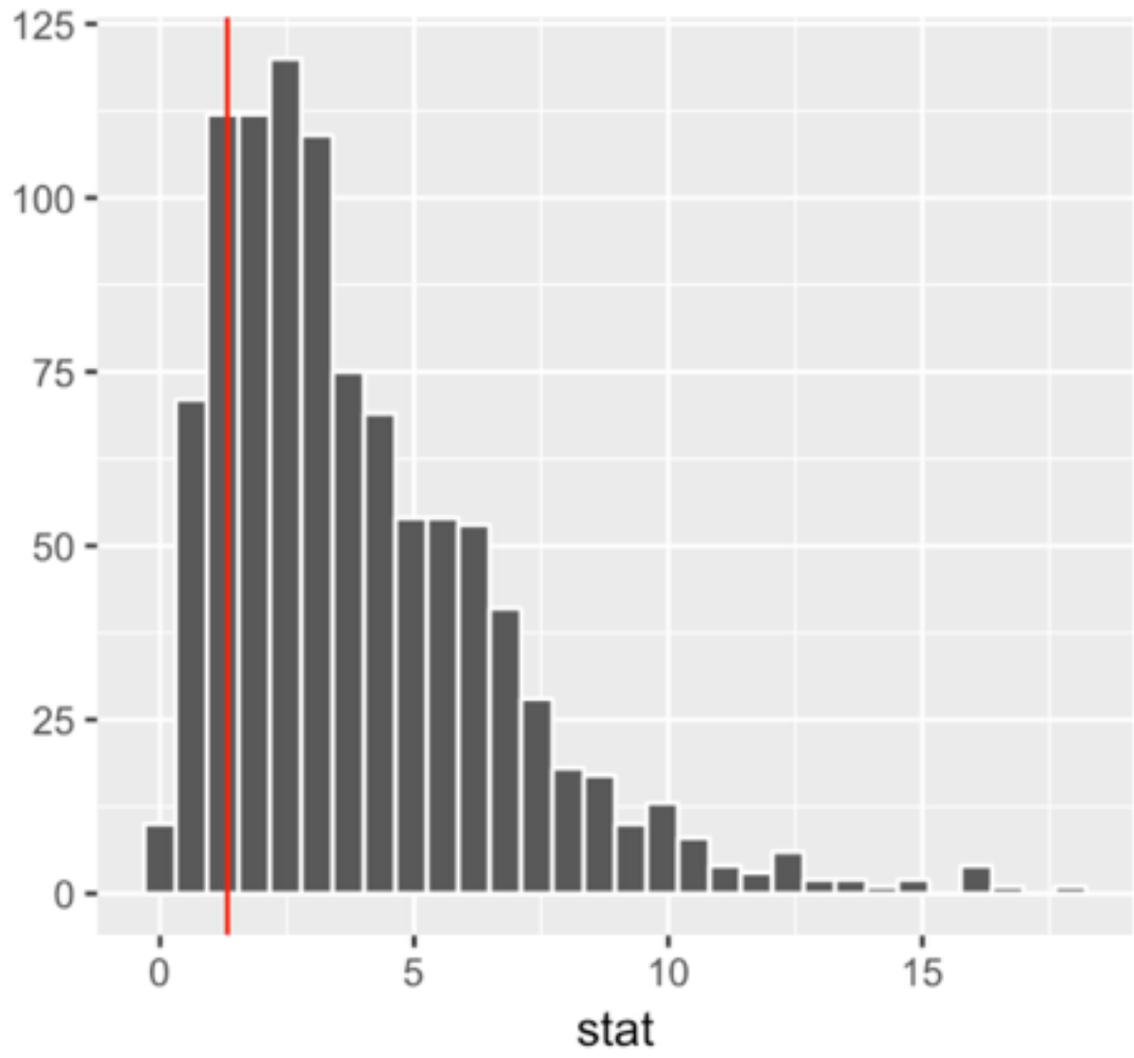
```

```
# A tibble: 1 x 1
  p_val
  <dbl>
1 0.864
```



Reusable parts

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gss %>%
  specify(NASA ~ party) %>%
  hypothesize(null = "independence") %>%
  generate(reps = 1000, type = "permute") %>%
  calculate(stat = "Chisq")
```

Permutation Chi-squared

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Approximation Chi-squared*

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Permutation p1 - p2

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*fiddle

"diff in props"

Permutation p1 - p2

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Permutation p1 - p2

Confidence interval for p1 - p2

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*fiddle

Permutation p1 - p2

```
gss %>%
  specify(NASA ~ party, success = "TOO MUCH") %>%
  hypothesize(null = "independence") %>%
  generate(reps = 1000, type = "permute") %>%
  calculate(stat = "diff in props")
```

"diff in props"

"bootstrap"

Confidence interval for p1 - p2

What’s to come

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- Generalize input to `calculate()`
  - For example, `calculate(trimmed_mean)`
  - Support for more advanced regression models
- Spruce up `visualize()`
- Add list-columns to `generate()`
- Wrapper functions: `t_test, chisq_test,` etc.

statistical inference

infer makes ~~p-values easier to compute.~~ tidy and transparent.

```
chisq.test(gss$party, gss$NASA)
```

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- Thanks to Chester Ismay, Ben Baumer, Mine Cetinkaya-Rundel, Jo Hardin, and the other contributors.
- website: infer.netlify.com
- slides: http://bit.ly/2DYoBOz