Self-Tuned Rejection Sampling within Gibbs and a Case Study in Small Area Estimation

Guide to Replication Materials

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1 Introduction

This document describes replication materials for the article "Self-Tuned Rejection Sampling within Gibbs and a Case Study in Small Area Estimation". It includes an R package, code for two simulations, and a data analysis. The following folders are included in the materials.

- 01-sim-cond: simulation generating from a single conditional of the SAE model under consideration.
- 02-sim-post: simulation generating from the posterior of the SAE model under consideration.
- 03-sae: data analysis with the SAIPE dataset.
- data: the SAIPE dataset and codes /inputs to assemble it.
- vws: An R package that supports construction of VWS samplers.
- saevws: an R package for the Gibbs sampler and supporting functions. It can be configured with basic vertical weighted strips (VWS), self-tuned VWS, and independent Metropolis-Hastings (IMH) for the $\sigma_1^2, \ldots, \sigma_m^2$ steps.

A working installation of R (R Core Team 2025) is required with the following packages (and their dependencies). These packages are available on CRAN at the time of this writing.

- devtools (Wickham et al. 2022),
- fntl (Raim 2024)
- jsonlite (Ooms 2014)
- knitr (Xie 2014)
- mcmcse (Flegal et al. 2021)
- Rcpp (Eddelbuettel and Balamuta 2018),
- sae (Molina and Marhuenda 2015)
- statmod (Smyth 2005)
- tidyverse (Wickham et al. 2019),
- xtable (Dahl et al. 2019)

Additionally, the included vws package must be installed.

```
R> devtools::install_local("/path/to/vws")
```

Section 2 gives an overview of the saevws package, including installation and basic usage. Section 3 lists the scripts used for the conditional simulation, posterior simulation, and data analysis. Section 4 gives a comprehensive list of packages and versions used in the computational studies, for reproducibility.

2 saevws R Package

The saevws package can be installed using an R command like the following.

```
R> devtools::install_local("/path/to/saevws")
```

The package exports several functions for use in R:

- gibbs invokes the Gibbs sampler.
- get_gibbs_control constructs a control object with additional arguments for the Gibbs sampler.
- get_vws_control constructs a control object with additional arguments for VWS within the Gibbs sampler.
- get_init constructs an object with initial values for the Gibbs sampler.
- get_fixed constructs an object to indicate that certain elements of the MCMC chain are to remain fixed in the Gibbs sampler. This is primarily used for testing the code.
- traceplots is a utility to make trace plots from a matrix with draws.

These functions' interfaces are shown below; see the associated manual pages for details about arguments, outputs, etc..

```
gibbs =
function (y, s2, X, Z, df, init = get_init(m = length(y), d1 = ncol(X),
   d2 = ncol(Z)), control = get_gibbs_control(), fixed = get_fixed())
get_gibbs_control =
function (R = 1000, burn = 0, thin = 1, report = R + 1, save_latent = integer(0),
   vws = get_vws_control())
get vws control =
function (tol1 = 0.01, tol2 = exp(-100), max_rejects = 1e+06, method = c("vws-tune",
    "vws-basic", "imh"), N = 50)
get_init =
function (m, d1, d2, beta = NULL, gamma = NULL, phi2 = NULL, tau2 = NULL,
    sigma2 = NULL, theta = NULL)
get_fixed =
function (beta = FALSE, gamma = FALSE, phi2 = FALSE, tau2 = FALSE, sigma2 = FALSE,
   theta = FALSE)
traceplots =
function (x, xlab = "")
```

3 Scripts

The following codes in O1-sim-cond produce the conditional simulation study in Section 5.1 of the article.

- metro.R: Simulations with IMH.
- vws.R: Simulations with VWS.
- samplers.cpp: C++ functions for samplers consisting of one IMH step and one VWS step.

The following codes in O2-sim-post produce the posterior simulation study in Section 5.2 of the article.

• gen.R: Generate folder structure for the study. Each level of the study is placed into a separate folder.

- sim.R: Run one level of the study.
- analyze .R: Analyze the results from the completed study and produce summaries.

The O3-sae folder contains a single script saipe. R that produces the data analysis in Section 6 of the article.

The data folder contains scripts and inputs to create the example SAIPE dataset.

- saipe.csv: the prepared dataset.
- cntysnap.csv: Supplemental Nutrition Assistance Program (SNAP) data for 2022, to be used as a covariate with 2023 SAIPE data.
- co-est2023-alldata.csv: 2023 population estimates from the U.S. Census Bureau's Population Estimates Program. The data may be obtained from the Census Bureau website.
- build-data.R: Code to construct the dataset saipe.csv.

4 Session Information

Results in the paper were produced in an R environment with the following packages and versions.

```
library(devtools)
library(tidyverse)
library(Rcpp)
library(mitr)
library(mcmcse)
library(jsonlite)
library(xtable)
library(xtable)
library(vws)
library(statmod)
```

```
R version 4.4.0 Patched (2024-05-13 r86547 ucrt)
Platform: x86_64-w64-mingw32/x64
Running under: Windows 11 x64 (build 26100)
Matrix products: default
locale:
[1] LC_COLLATE=English_United States.utf8
[2] LC_CTYPE=English_United States.utf8
[3] LC_MONETARY=English_United States.utf8
[4] LC_NUMERIC=C
[5] LC_TIME=English_United States.utf8
time zone: America/New_York
tzcode source: internal
attached base packages:
              graphics grDevices utils
                                            datasets methods
[1] stats
                                                                 base
other attached packages:
[1] saevws_0.1.0
loaded via a namespace (and not attached):
```

[1]	vctrs_0.6.5	cli_3.6.5	knitr_1.50	rlang_1.1.6
[5]	xfun_0.53	generics_0.1.4	S7_0.2.0	jsonlite_2.0.0
[9]	glue_1.8.0	htmltools_0.5.8.1	brio_1.1.5	scales_1.4.0
[13]	rmarkdown_2.29	grid_4.4.0	vws_0.2.0	tibble_3.3.0
[17]	evaluate_1.0.5	fastmap_1.2.0	yaml_2.3.10	lifecycle_1.0.4
[21]	compiler_4.4.0	dplyr_1.1.4	RColorBrewer_1.1-3	testthat_3.2.3
[25]	fftwtools_0.9-11	Rcpp_1.1.0	pkgconfig_2.0.3	rstudioapi_0.17.1
[29]	farver_2.1.2	digest_0.6.37	R6_2.6.1	tidyselect_1.2.1
[33]	pillar_1.11.0	magrittr_2.0.3	mcmcse_1.5-0	ellipse_0.5.0
[37]	tools_4.4.0	gtable_0.3.6	ggplot2_4.0.0	

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