

## 1. Q1

### a. Part 1

- $p(F) = 0.6$
- $p(S) = 0.7$
- $p(T) = 0.8$

$$\begin{aligned} 1 - p(!F) * p(!S) * p(!T) &= \\ 1 - 0.4 * 0.3 * 0.2 &= \\ \mathbf{0.976 \text{ or } 97.6 \%} \end{aligned}$$

### b. Part 2

$$\begin{aligned} p(N \geq 2) &= p(N \geq 1) - p(N = 1) \\ p(N = 1) &= p(f)(!s)(!t) + p(!f)p(s)p(!t) + p(f)(!s)(!t) \\ &= \mathbf{0.788 \text{ or } 78.8\%} \end{aligned}$$

## 2. Q2

$$\begin{aligned} P(S \geq 800) &= 0.2 \\ N &= \text{num of robots} \\ P(N \geq 1) &= 1 - p(N = 0) \\ 1 - p(S \geq 800) &= 0.8 \\ \mathbf{S^5 = 0.8^5 = 0.723 \text{ or } 72.3\%} \end{aligned}$$

## 3. Q4

$$\begin{aligned} p(A|C) &= p(A) \text{ and } p(C|A) = p(C) \\ p(B|C) &= p(B) \text{ and } p(C|B) = p(C) \\ p(A|B) &= 0 \text{ and } p(B|A) = 0 \\ p(A \text{ or } C) &= \frac{2}{3} \\ p(B \text{ or } C) &= \frac{3}{4} \\ p(A \text{ or } B \text{ or } C) &= \frac{11}{12} \end{aligned}$$

$$\begin{aligned} p(A) + p(B) + p(C) - p(A \& B) - p(C \& B) - p(A \& C) + p(A \& B \& C) &= \frac{11}{12} \\ p(A) + p(C) - p(A \& C) &= \frac{2}{3} \\ p(C) + p(B) - p(C \& B) &= \frac{3}{4} \end{aligned}$$

Independent and Disjoint:

$$\begin{aligned} p(A) + p(C) - p(A)*p(C) &= \frac{2}{3} \\ p(C) + p(B) - p(C)*p(B) &= \frac{3}{4} \\ p(A) + p(B) + p(C) - p(C)*p(B) - p(A)*p(C) &= \frac{11}{12} \end{aligned}$$

$$11/12 = p(A) + \frac{3}{4} - p(A) * p(C)$$

$$p(A) - p(A) * p(C) = 1/6$$

$$p(C) + 1/6 = 2/3$$

$$p(C) = \frac{1}{2}$$

## 4. Q4

F -> p(picking up fake coin)

$$p(!F) = 0.8$$

$$p(F) = 0.2$$

$$p(H|!F) = 0.5$$

$$p(H|F) = 1$$

$$p(H) = p(H|F) * p(F) + p(H|!F) * p(!F) = 1 * 0.2 + 0.5 * 0.8$$

$$p(H) = 0.6$$

$$p(F|H) = p(H|F) * p(F) / p(H) = 1 * 0.2 / 0.6 \quad p(F|H) = \mathbf{0.333 \text{ or } 33.3\%}$$