

# Exam 1

MATH 5610 FALL 2016

NAME:

GRADE: \_\_\_\_\_

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**Problem 1.** Explain why accumulation of roundoff error is inevitable when arithmetic operations are performed in a floating point system. When is this accumulation of roundoff errors tolerable in numerical calculations.

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**Your Answer/Solution:**

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**Problem 2.** Explain the importance of the machine precision of a computer.

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**Your Answer/Solution:**

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**Problem 3.** What is the basic ingredient for convergence of a functional iteration algorithm in the location of the roots of a nonlinear function? What controls the speed of convergence in such a method?

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**Your Answer/Solution:**

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**Problem 4.** State the disadvantages of computing the inverse of a square matrix in solving a system of linear equations

$$Ax = b$$

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**Your Answer/Solution:**

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**Problem 5.** Give an example/explanation that distinguishes between problem conditioning and algorithm stability.

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**Your Answer/Solution:**

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**Problem 6.** Show that the following difference is a second order approximation of the derivative of a function,  $f$ , at  $x = x_0$ .

$$f'(x_0) \approx \frac{f(x_0 + \frac{h}{2}) - f(x_0 - \frac{h}{2})}{h}$$

Use Taylor series expansions.

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**Your Answer/Solution:**

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