

## CMS/CS/EE 144

### Networks: Structure & Economics

#### Administrivia

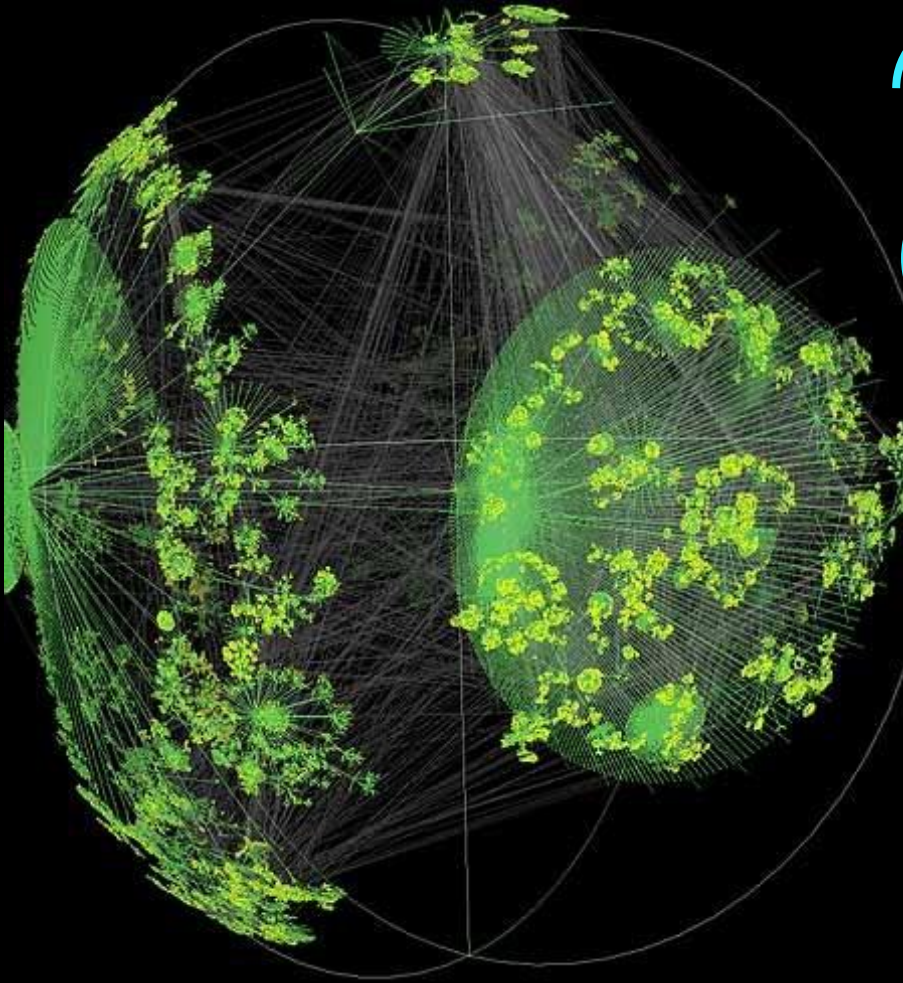
- 1) Register for Piazza if you haven't already
- 2) Buy your textbook!
- 3) HW1 is due Thursday
- 4) Office hours:
  - me: After classes on Thursday
  - TAs: Tue/Wed 7-9pm (107 ANB)
- 5) Don't forget about your blog posts!
- 6) Background poll – fill out if you haven't already

# Course warmup...

The evolution and structure of the web



Our goal: What “structure” does the web graph have?

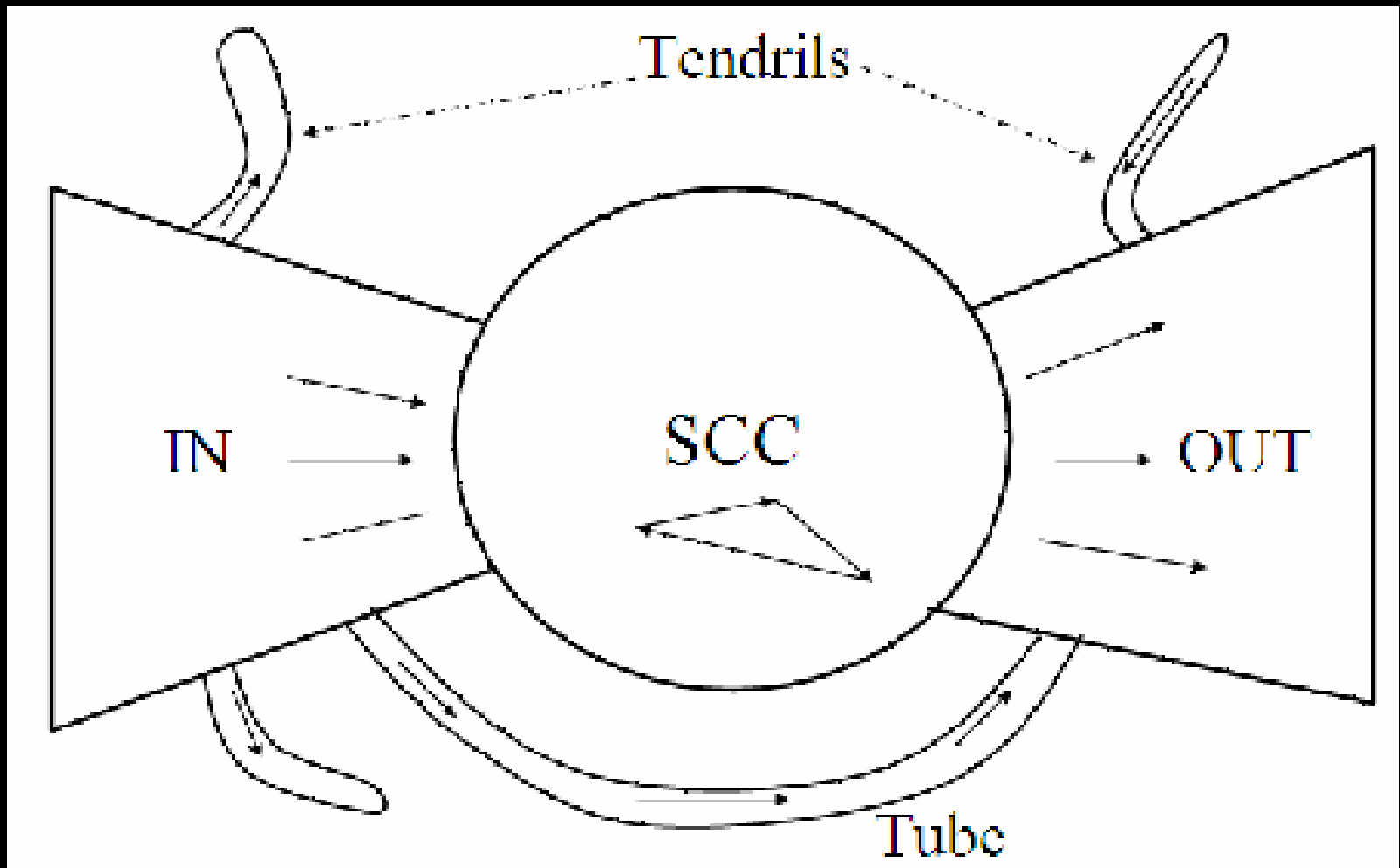


Nodes = pages

Edges = links  
(edges are directed)

Our goal: What “structure” does the web graph have?

- 1) Connectivity?
- 2) Diameter?
- 3) Degree?
- 4) Clustering?



Our goal: What “structure” does the web graph have?

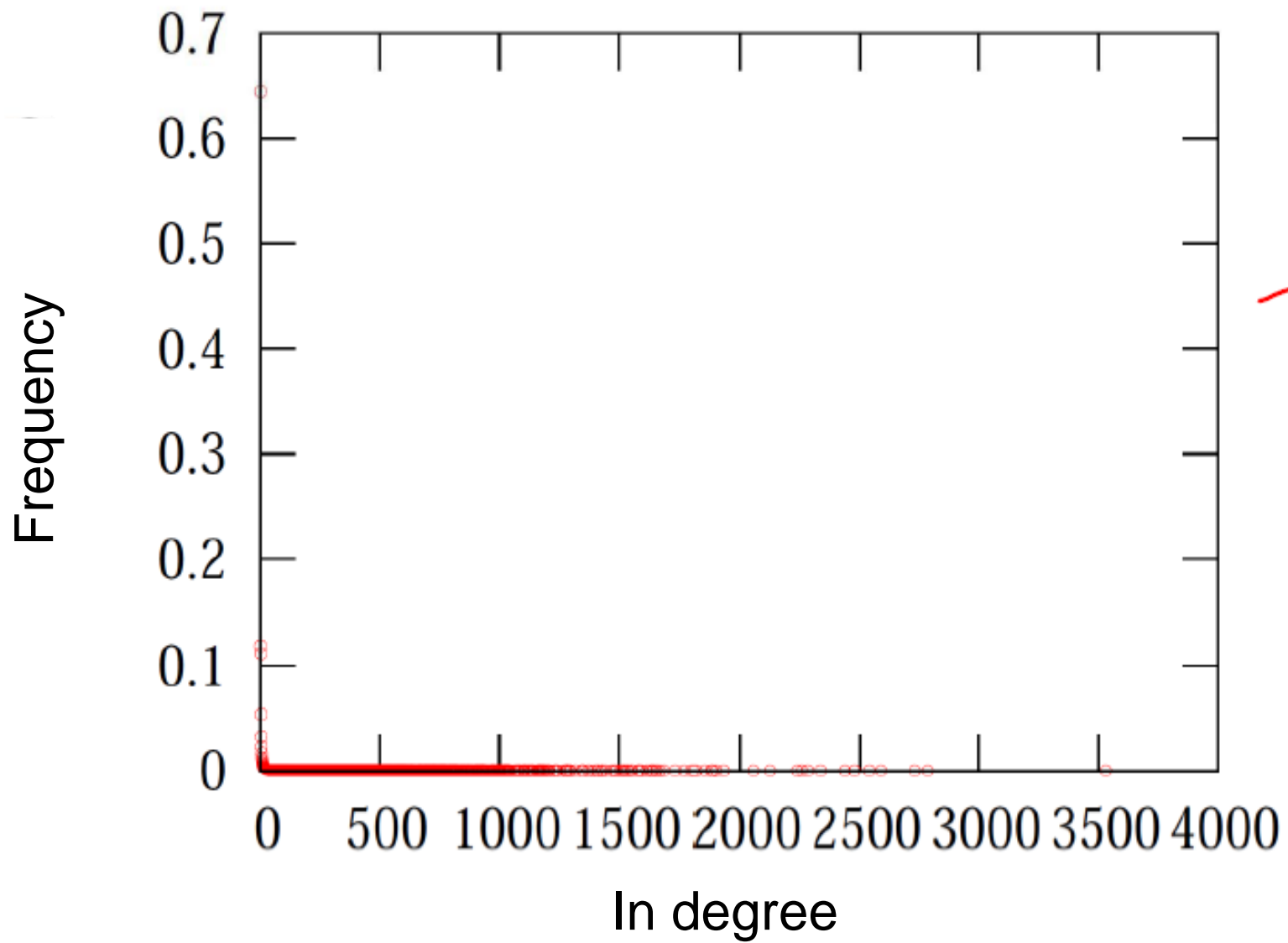
- 1) Connectivity? There is a giant connected component
- 2) Diameter?
- 3) Degree?
- 4) Clustering?

Our goal: What “structure” does the web graph have?

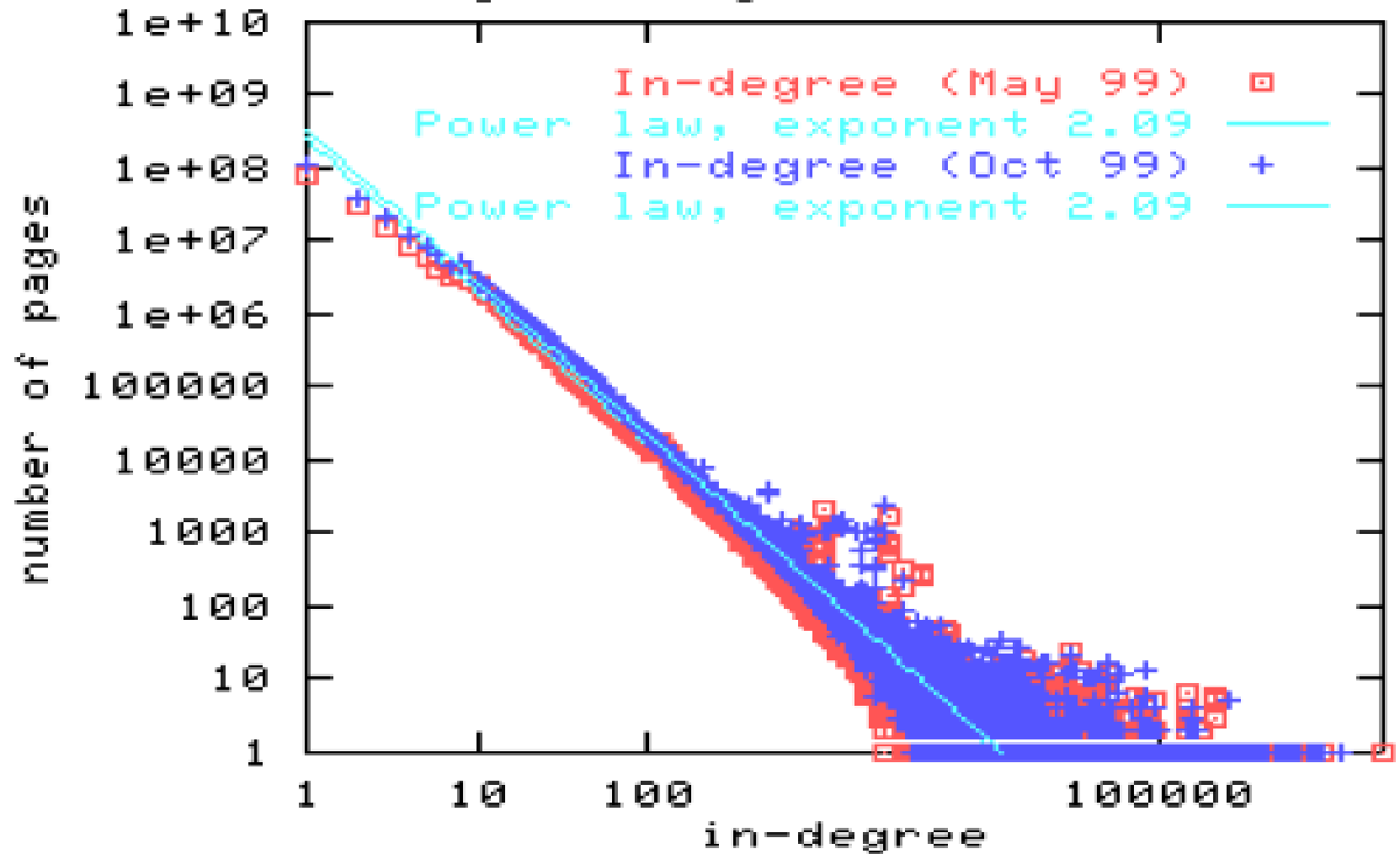
- 1) Connectivity? There is a giant connected component
- 2) Diameter? Small diameter
- 3) Degree?
- 4) Clustering?



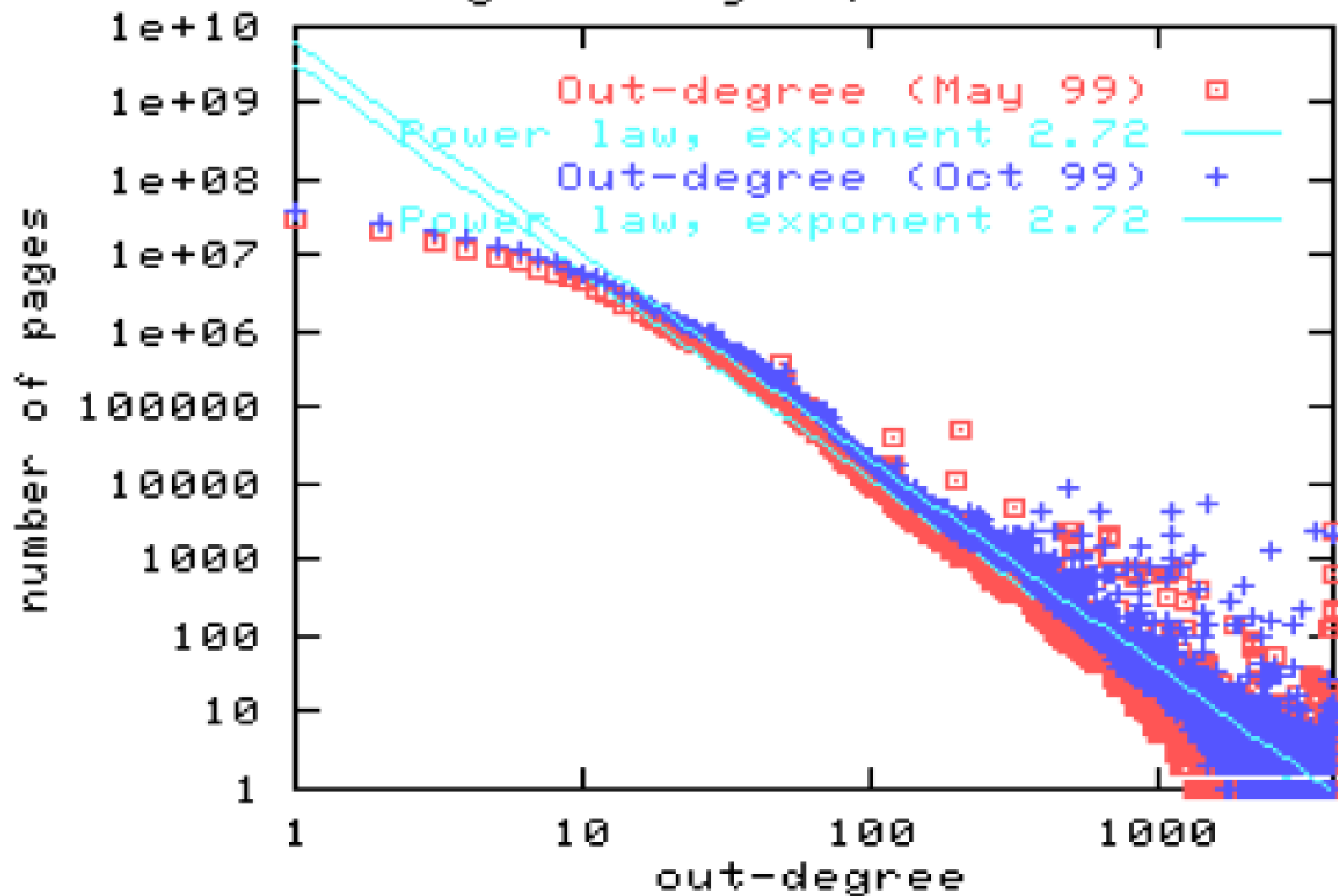




In-degree (May 99, Oct 99) distr.



Out-degree (May 99, Oct 99) distr.



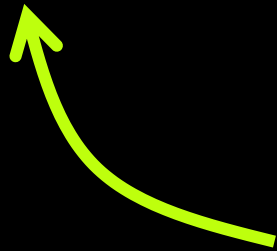
Our goal: What “structure” does the web graph have?

- 1) Connectivity? There is a giant connected component
- 2) Diameter? Small diameter
- 3) Degree? Heavy-tailed degree distribution
- 4) Clustering?



Our goal: What “structure” does the web graph have?

- 1) Connectivity? There is a giant connected component
- 2) Diameter? Small diameter
- 3) Degree? Heavy-tailed degree distribution
- 4) Clustering? Highly clustered



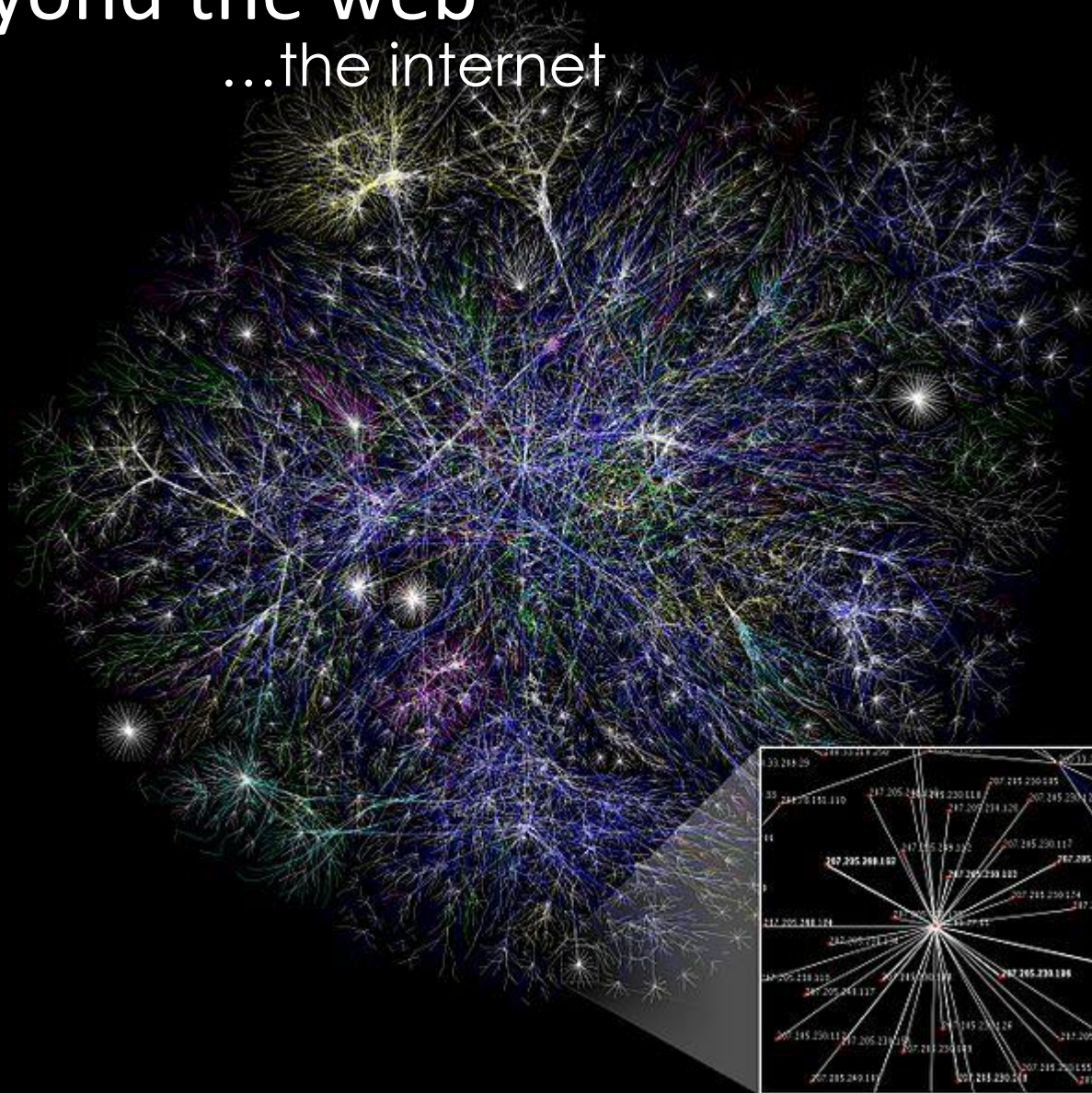
It turns out that these are “universal”

# Beyond the web

...there are lots of other networks people study

# Beyond the web

...the internet





# Beyond the web

...online social networks

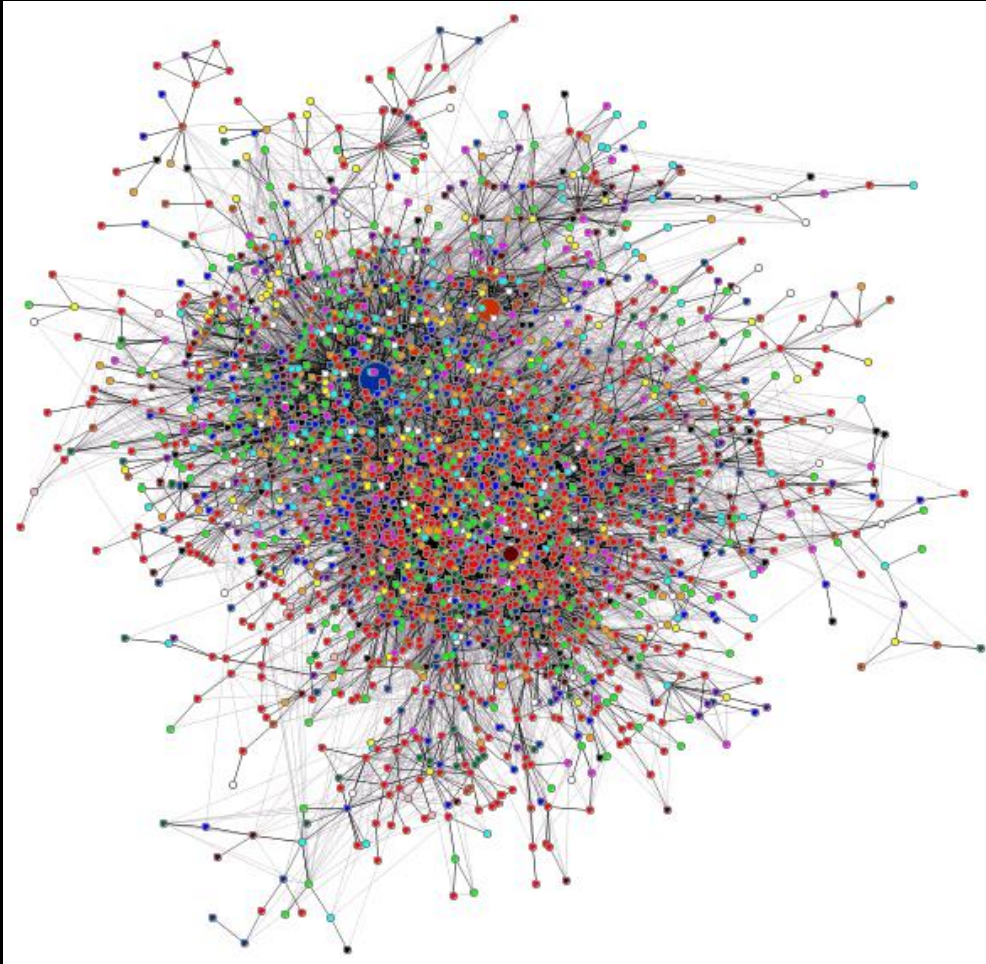
(Facebook, Myspace, blogs, flickr, IMs, etc)



# Beyond the web

...online social networks

(Facebook, Myspace, blogs, flickr, IMs, etc)



Blogosphere links

# Beyond the web

...online social networks

(Facebook, Myspace, blogs, flickr, IMs, etc)

twitter

A map of North America, including the United States, Canada, and Mexico, is shown against a black background. The map is overlaid with a complex network of glowing lines and nodes. The lines are primarily blue and orange, with some white nodes at the intersections. The network is denser in the eastern United States and the Great Lakes region, with more sparse connections in the western United States and Mexico. The overall effect is a visualization of a large-scale social network.

# Beyond the web

...traditional social networks

e.g. friends

hierarchy in business

family trees

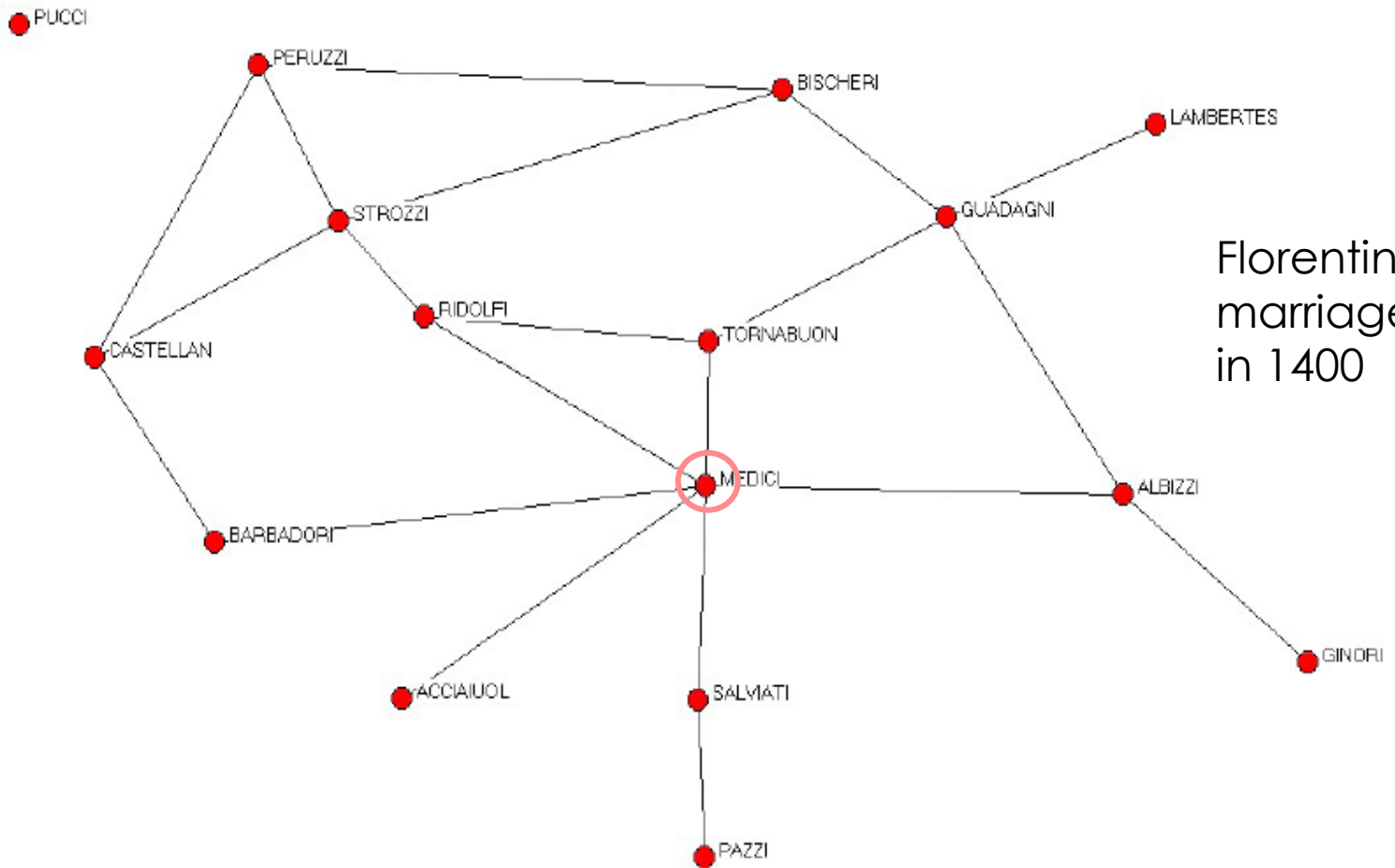
marriages

sexual relations

...many others

# Beyond the web

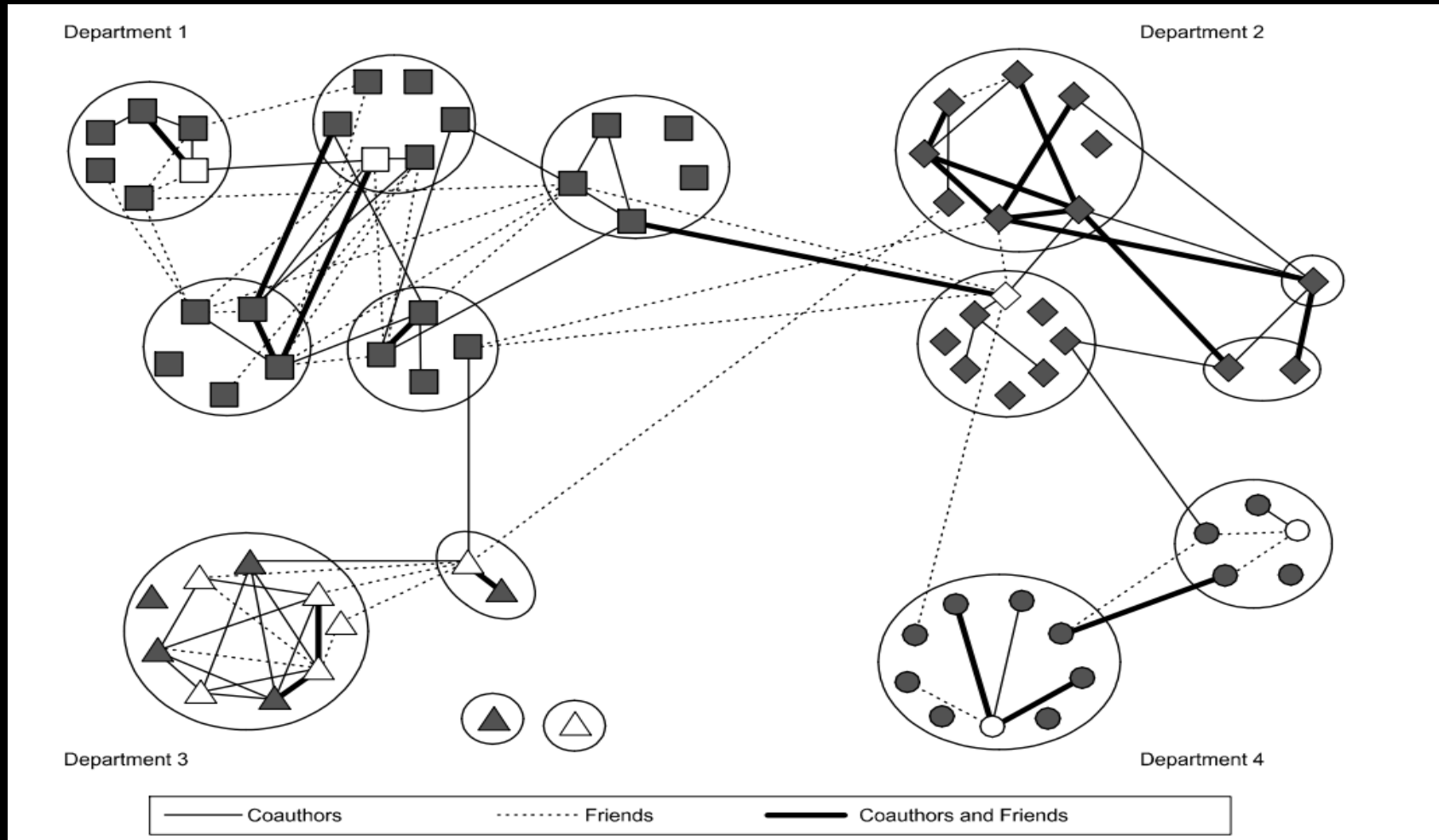
...traditional social networks





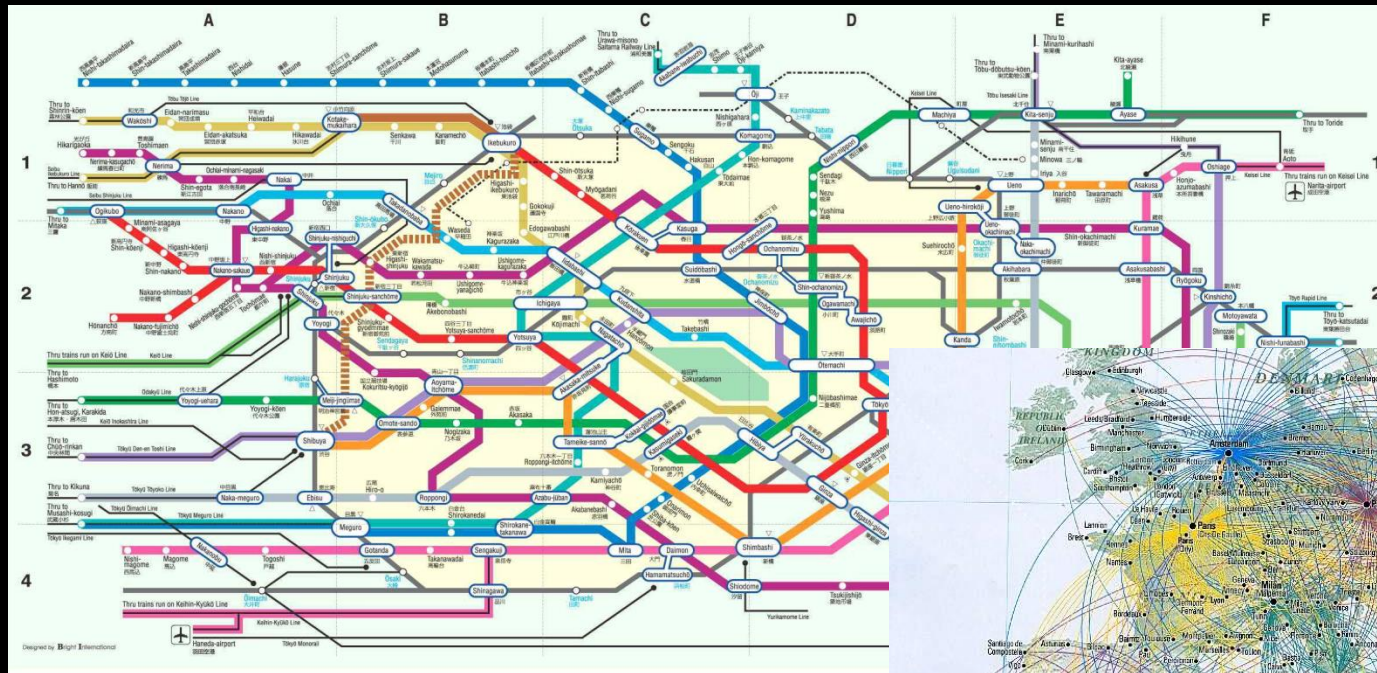
# Beyond the web

...traditional social networks



(from Leeat Yariv)

# Beyond the web ...transportation networks



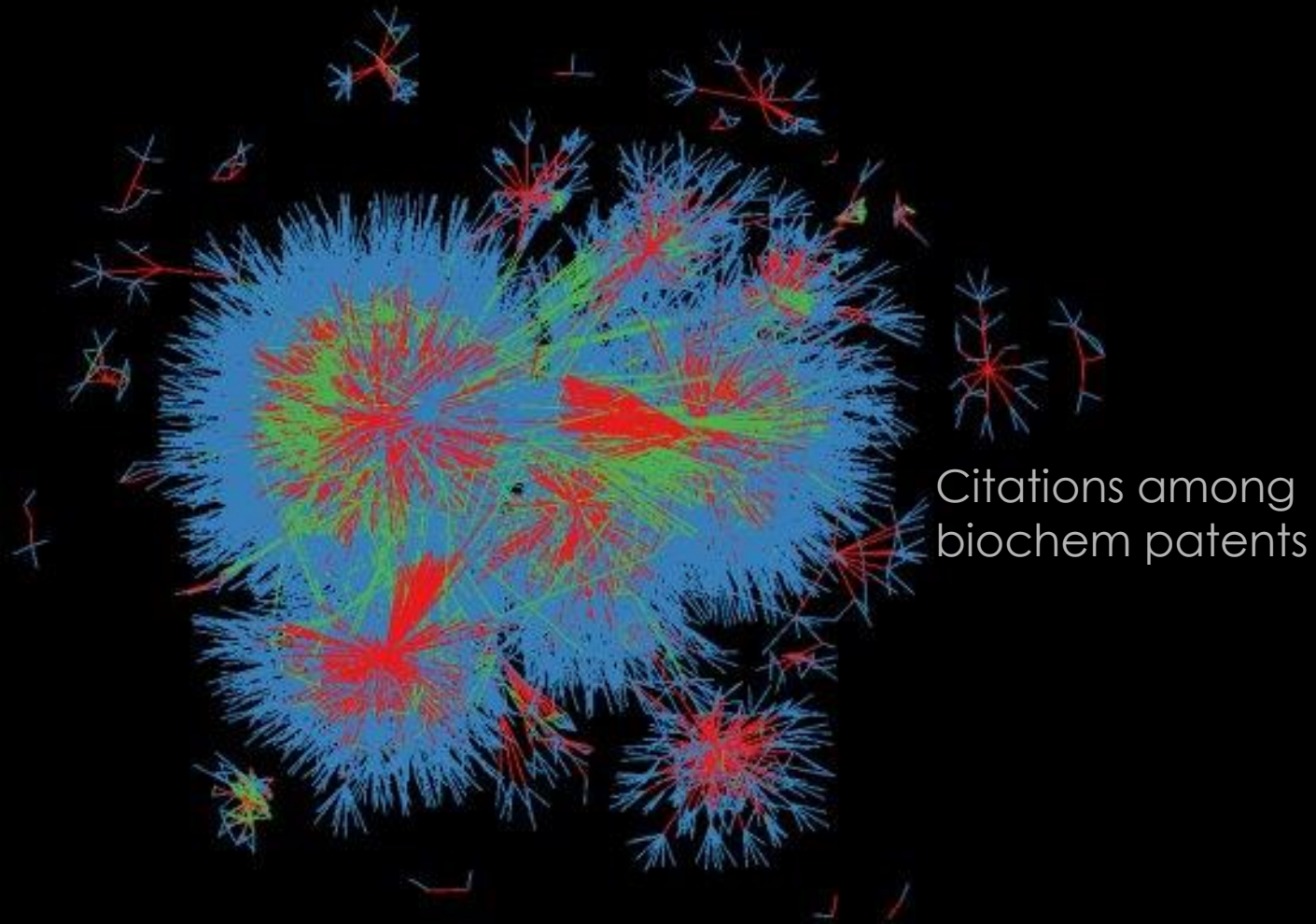
Tokyo metro

European airlines



# Beyond the web

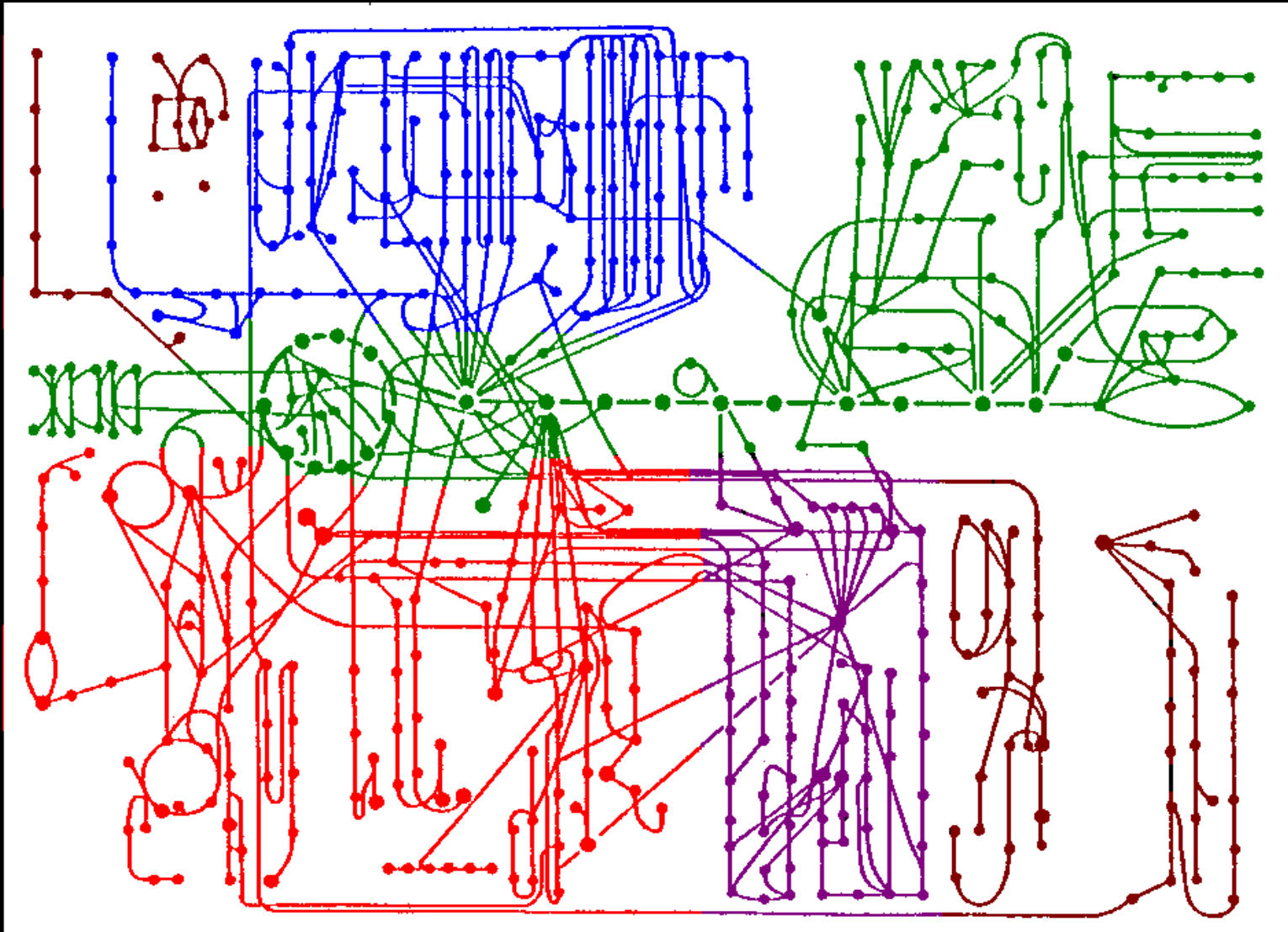
...coauthor & citation networks





# Beyond the web

...biological networks



Biochemical  
pathways of  
malaria

# Beyond the web

## ...biological networks

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**Railways and slime moulds**

## A life of slime

Network-engineering problems can be solved by surprisingly simple creatures

Jan 21st 2010

From *The Economist* print edition

FROM adhesives that mimic the feet of geckos to swimsuits modelled on shark skin, biologically inspired design has taken off in recent times. Copying nature's ideas allows people to harness the power of evolution to come up with clever products. Now a group of researchers has taken this idea a step further by using an entire living organism—a slime mould—to solve a complex problem. In this case, the challenge was to design an efficient rail network for the city of Tokyo and its outlying towns.

Slime moulds are unusual critters—neither animal, nor plant nor fungus. If they resemble anything, it is a colonial amoeba. *Physarum polycephalum*, the species in question, consists of a membrane-bound bag of



**Show me the way to Shinjuku**

SPL

All these (and many others) tend to have the same “universal” properties as the web

- 1) A “giant” connected component
- 2) Small diameter
- 3) Heavy-tailed degree distribution
- 4) High clustering coefficient

## We'll look at 6 examples

Social network → Slashdot network in 2009

Citation network → US Patents

Web Graph → Google 2002

Internet Graph → 2005

Product co-purchasing → Amazon 2003

Road networks → California 2008

(all data from <http://snap.stanford.edu/data/index.html>)

- 1) A “giant” connected component
- 2) Small diameter
- 3) Heavy-tailed degree distribution
- 4) High clustering coefficient

Social network → ??

Citation network → ??

Web Graph → ??

Internet Graph → ??

Product co-purchasing → ??

Road networks → ??

- 1) A “giant” connected component
- 2) Small diameter
- 3) Heavy-tailed degree distribution
- 4) High clustering coefficient

Social network → 86% nodes in SCC, 100% in WCC

Citation network → 0% in SCC, 99% in WCC

Web Graph → 50% in SCC, 98% in WCC

Internet Graph → 99% in SCC, 99% in WCC

Product co-purchasing → 98% in SCC, 100% in WCC

Road networks → 99% in WCC

- 1) A “giant” connected component
- 2) Small diameter
- 3) Heavy-tailed degree distribution
- 4) High clustering coefficient

Social network → ??

Citation network → ??

Web Graph → ??

Internet Graph → ??

Product co-purchasing → ??

Road networks → ??

- 1) A “giant” connected component
- 2) Small diameter
- 3) Heavy-tailed degree distribution
- 4) High clustering coefficient

Social network → 12, 90%tile effective diameter is 4.7

Citation network → 22, 90%tile effective diameter is 9.4

Web Graph → 22, 90%tile effective diameter is 8.1

Internet Graph → 25, 90%tile effective diameter is 5.9

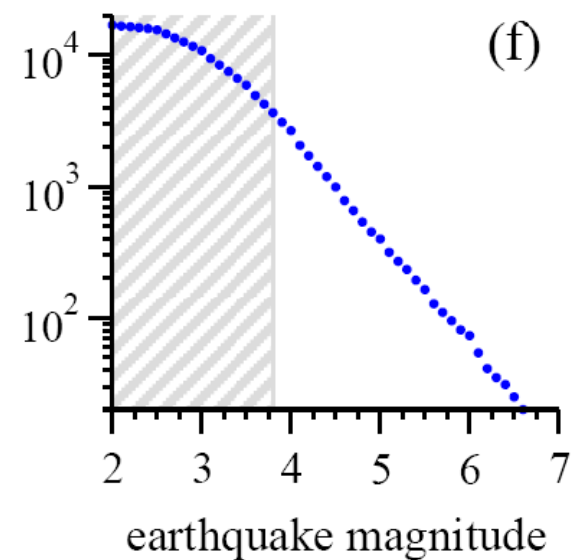
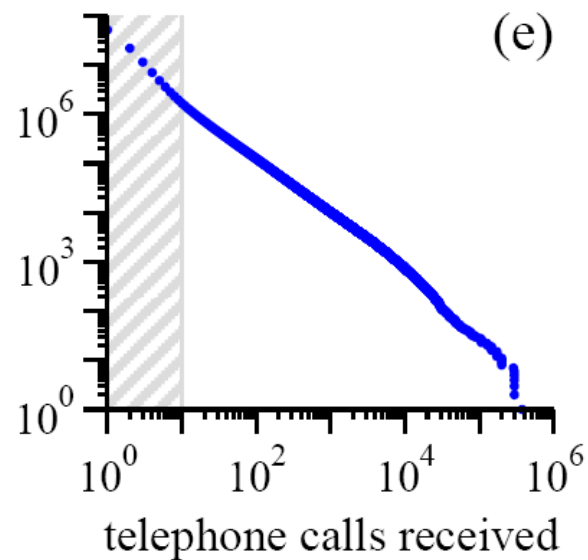
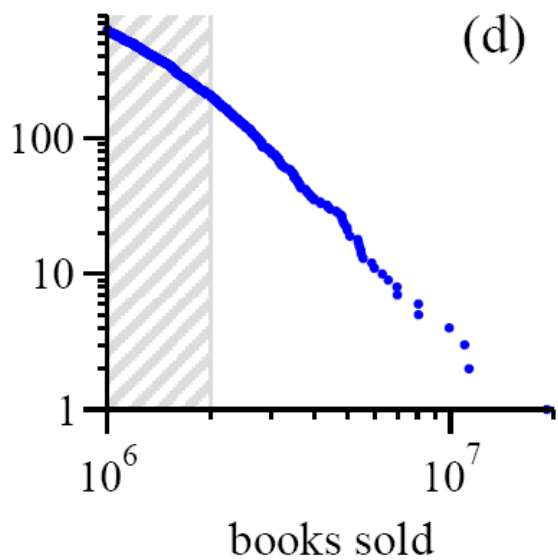
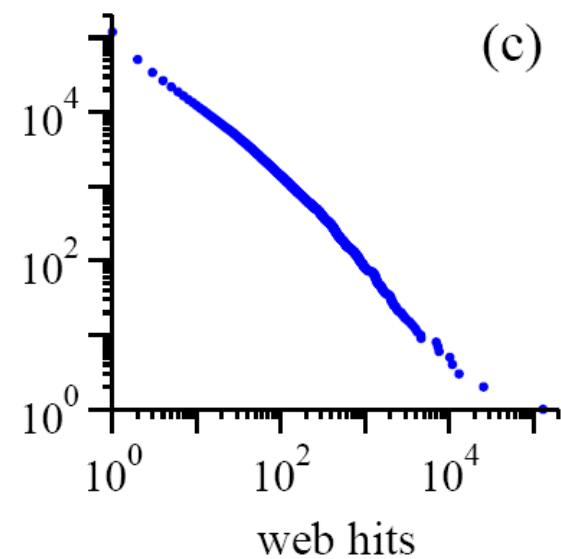
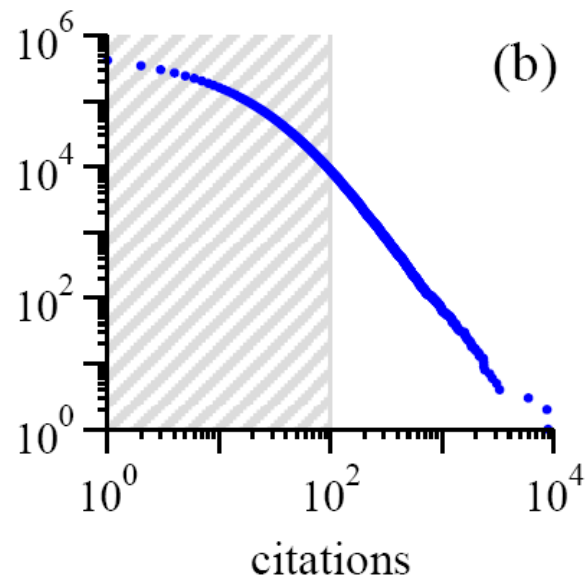
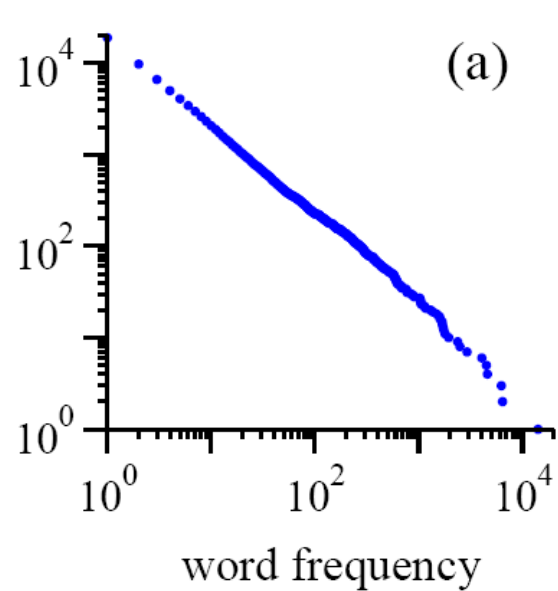
Product co-purchasing → 21, 90%tile effective diam is 7.6

Road networks → 850, 90%tile effective diameter is 500

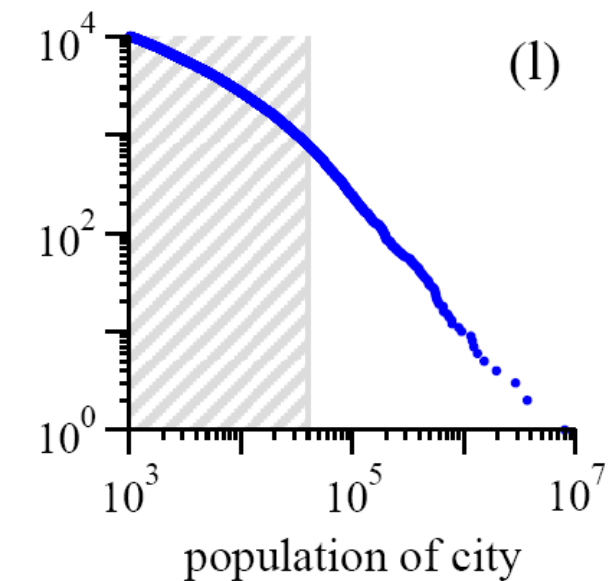
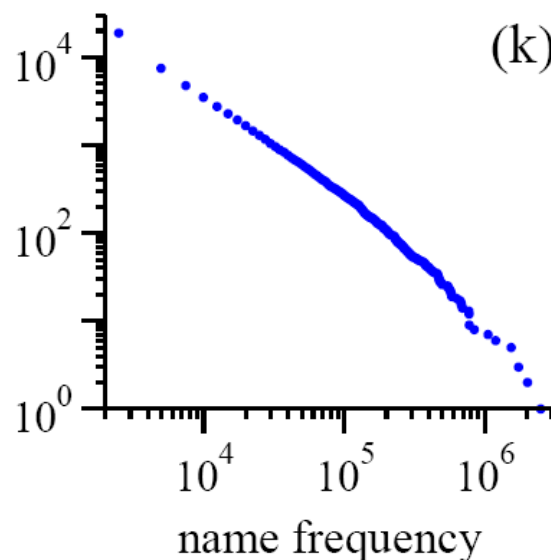
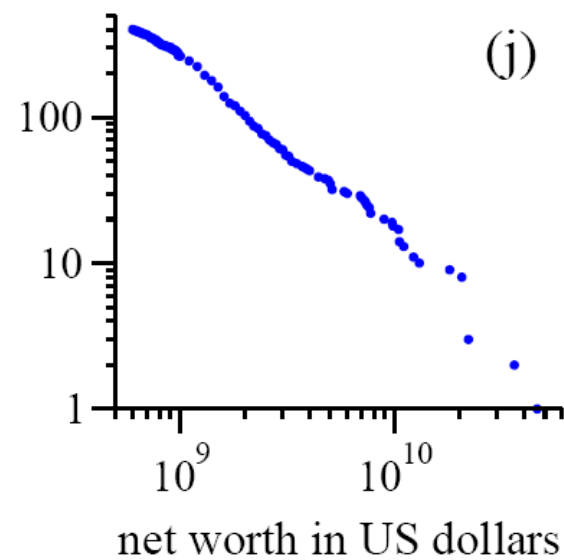
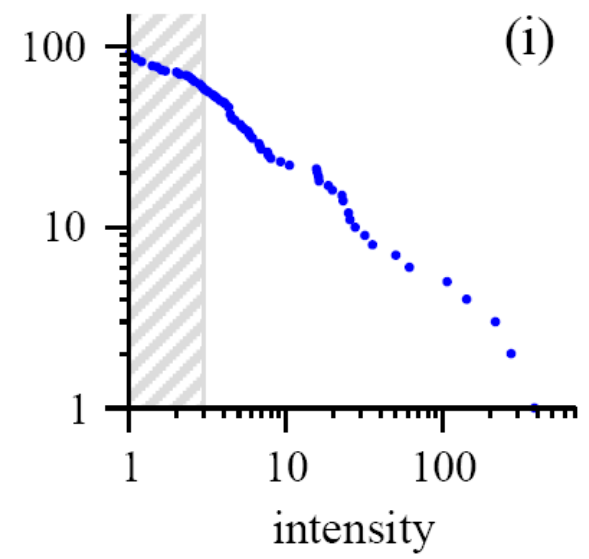
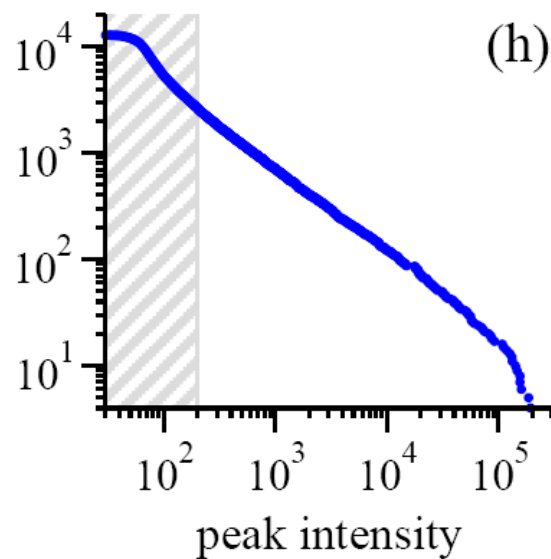
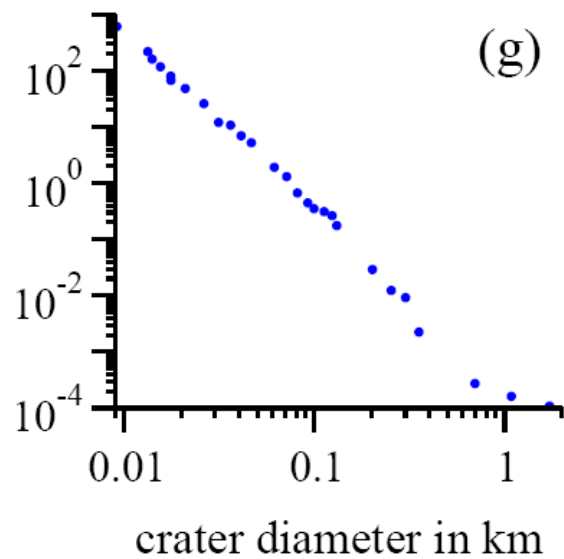


- 1) A “giant” connected component
- 2) Small diameter
- 3) Heavy-tailed degree distribution
- 4) High clustering coefficient

Here I'll start by showing you some other data sets...



(These are the ccdfs.)



(These are the ccdfs.)

The reason I showed you others is that the existence of heavy-tailed degree distributions is a bit **controversial**

...heavy-tails are “universal”, but naïve statistics can lead you astray

## On Power-Law Relationships of the Internet Topology


*Michalis Faloutsos*  
U.C. Riverside  
Dept. of Comp. Science  
michalis@cs.ucr.edu

*Petros Faloutsos*  
U. of Toronto  
Dept. of Comp. Science  
pfal@cs.toronto.edu

*Christos Faloutsos \**  
Carnegie Mellon Univ.  
Dept. of Comp. Science  
christos@cs.cmu.edu

1999 Sigcomm paper – 4500+ citations!

2005, STOC

 **BUT...**

## On the Bias of Traceroute Sampling or, Power-law Degree Distributions in Regular Graphs

Dimitris Achlioptas  
Microsoft Research  
Microsoft Corporation  
Redmond, WA 98052  
optas@microsoft.com

David Kempe  
Department of Computer Science  
University of Southern California  
Los Angeles, CA 90089  
dkempe@usc.edu

Aaron Clauset  
Department of Computer Science  
University of New Mexico  
Albuquerque, NM 87131  
aaron@cs.unm.edu

Cristopher Moore  
Department of Computer Science  
University of New Mexico  
Albuquerque, NM 87131  
moore@cs.unm.edu

IEEE/ACM TRANSACTIONS ON NETWORKS

1205

## Understanding Internet Topology: Principles, Models, and Validation

David Alderson, *Member, IEEE*, Lun Li, *Student Member, IEEE*, Walter Willinger, *Fellow, IEEE*, and  
John C. Doyle, *Member, IEEE*

2005, ToN

There are similar stories in power nets, social nets, ...

- 1) A “giant” connected component
- 2) Small diameter
- 3) Heavy-tailed degree distribution
- 4) High clustering coefficient

(without correlations clustering coefs would all be  $< 0.001$ )

Social network → ??

Citation network → ??

Web Graph → ??

Internet Graph → ??

Product co-purchasing → ??

Road networks → ??

- 1) A “giant” connected component
- 2) Small diameter
- 3) Heavy-tailed degree distribution
- 4) High clustering coefficient

(without correlations clustering coefs would all be  $< 0.001$ )

Social network → Avg clustering coef 0.06

Citation network → Avg clustering coef 0.09

Web Graph → Avg clustering coef 0.60

Internet Graph → Avg clustering coef 0.30

Product co-purchasing → Avg clustering coef 0.42

Road networks → Avg clustering coef 0.05

- 1) A “giant” connected component
- 2) Small diameter
- 3) Heavy-tailed degree distribution
- 4) High clustering coefficient

Hopefully you're convinced that these are “universal”!

... the interesting thing to find these days are  
places where one or more doesn't hold!



DISCLAIMER: We're moving on, but there are many other interesting properties of networks that we could discuss!

- weak ties vs. strong ties
- expansion
- densification
- shrinking diameter
- power law eigenvalues
- ...

- Identifying “universal” properties is still an active research area.
- Any of these would make good projects

Two possible next steps for us:

Scientific question

What causes the emergence of these properties?

Engineering question

How can we exploit these properties for system design?

→ Since this is Caltech we'll be scientists first,  
and then engineers...

**BUT**

...to keep you motivated:

You should start to think of ways to exploit  
the properties we've discussed...

