Asynchronous Federated Optimization

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Abstract

Federated learning enables training on a massive number of edge devices. To improve flexibility and scalability, we propose a new asynchronous federated optimization algorithm. We prove that the proposed approach has nearlinear convergence to a global optimum, for both strongly and non-strongly convex problems, as well as a restricted family of nonconvex problems. Empirical results show that the proposed algorithm converges fast and tolerates staleness.

1 INTRODUCTION

Federated learning (Konevcný et al., 2016; McMahan et al., 2016) enables training a global model on datasets decentrally located on a massive number of resource-weak edge devices. Federated learning is motivated by the massive data generated in our daily life, by edge devices/IoT such as smart phones, wearable devices, sensors, and in smart homes/buildings. Ideally, the larger amounts of training data from diverse users results in improved representation and generalization of machine-learning models. Federated learning is also motivated by the need for privacy preservation. In some scenarios, on-device training without depositing data in the cloud is legally required by regulations such as US HIPAA laws (HealthInsurance.org, 1996) and Europe's GDPR law (EU, 2018).

Typically, a federated learning system is composed of servers and workers, whose architecture is similar to parameter servers (Li et al., 2014a;b; Ho et al., 2013). The workers train the models locally on the private data on edge devices. The servers aggregate the learned models from the workers, and produce a global model on the cloud/datacenter. To protect the users' privacy, the workers do not expose the training data to the servers, and

instead only expose the trained model.

We summarize the key properties of federated learning below:

- Infrequent task scheduling. Edge devices typically have weak computational capacity and limited battery time. Unlike the traditional distributed machine learning, on-device federated learning tasks are allowed to be executed only when the device is idle, charging, and connected to unmetered networks (i.e., WiFi) (Bonawitz et al., 2019). The edge devices will ping the servers when they are ready to execute training tasks. The servers will then schedule training tasks on available edge devices. Furthermore, to avoid congesting the network, the server randomizes the check-in time of the workers. As a result, on each edge device, the training task is executed infrequently.
- Limited communication. The connection between edge devices and the remote servers may be frequently unavailable, slow, or expensive (in terms of communication costs or in the power of battery). Thus, compared to typical distributed optimization, communication in federated learning needs to be much less frequent.
- Non-IID training data. Unlike the traditional distributed machine learning, the data on different devices are not mixed and IID, and thus represent non-identically distributed samples from the population.

We posit that the synchronous flavor of federated optimization is potentially unscalable, inefficient, and inflexible. Previous synchronous training algorithms for federated averaging (McMahan et al., 2016; Bonawitz et al., 2019) can only handle hundreds of devices in parallel, while there are nearly 4 billion mobile phones in total (eMarketer, 2019). Even at smaller scales, like a stadium during a game, there are thousands of devices involved. Too many devices checking in at the same time can congest the network on the server side. Thus, in each global epoch,

the server is limited to selecting only from the subset of available devices to trigger the training tasks. Furthermore, since the task scheduling varies from device to device due to limited computational capacity and battery time, it is difficult to synchronize the selected devices at the end of each epoch. Some devices will no longer be available before synchronization. Instead, the server has to determine a timeout threshold to drop the stragglers. If the number of survived devices is too small, the server may have to drop the entire epoch including all the received updates.

To address these issues that arise in synchronous federated optimization, we propose a novel asynchronous federated optimization algorithm. The key idea is to use a weighted average to update the global model. The mixing weight can also be set adaptively as a function of the staleness. We show that taken together, these changes result in an effective asynchronous federated optimization procedure.

The main contributions of our paper are listed as follows:

- We propose a new asynchronous federated optimization algorithm with provable convergence under non-IID settings.
- We show that the proposed approach has near-linear convergence to a global optimum, for both strongly and non-strongly convex problems, as well as a restricted family of non-convex problems.
- We propose strategies for controlling the error caused by asynchrony. We instroduce a mixing hyperparameter which adaptively controls the trade-off between the convergence rate and variance reduction according to the staleness.
- We show empirically that the proposed algorithm converges fast and outperforms synchronous federated optimization.

2 RELATED WORK

Edge computing (Garcia Lopez et al., 2015; Hong et al., 2013) is increasingly applied in various scenarios such as smart home, wearable devices, and sensor networks. Meanwhile, machine-learning applications are also moving from cloud to edge (Cao et al., 2015; Mahdavinejad et al., 2018; Zeydan et al., 2016). Typically, edge devices have weaker computation and communication capacity compared to the workstations and datacenters, due to the weak hardware, limited battery time, and metered networks. As a result, simple machine-learning models such as MobileNet (Howard et al., 2017) have been proposed for the learning tasks on weak devices.

Existing federated optimization methods (Konevcnỳ et al., 2015; 2016; McMahan et al., 2016; Bonawitz et al., 2019) focus on synchronous training. In each global epoch, training tasks are triggered on a subset of workers. However, perhaps due to the bad networking conditions and occasional issues, some worker may fail. When this happens, the server has to wait until a sufficient number of workers respond. Otherwise, the server times out, drops the current epoch, and moves on to the next epoch. As far as we know, this paper is the first to discuss asynchronous training in federated learning.

Asynchronous training (Zinkevich et al., 2009; Lian et al., 2017; Zheng et al., 2017) is widely used in traditional distributed SGD. Typically, asynchronous SGD converges faster than synchronous SGD. However, classic asynchronous SGD directly sends gradients to the servers after each local update, which is not feasible for edge devices due to unreliable and slow communication. In this paper, we take the advantage of asynchronous training, and combine it with federated optimization.

Table 1: Notations and Terminologies.

Notation/Term	Description
\overline{n}	Number of devices
T	Number of global epochs
[n]	Set of integers $\{1, \ldots, n\}$
H_{min}	Minimal number of local iterations
$H_{ au}^{i}$	Number of local iterations in the τ^{th} epoch
	on the <i>i</i> th device
x_t	Global model in the t^{th} epoch on server
$x_{\tau,h}^i$	Model initialized from x_{τ} , updated in
,	the h th local iteration, on the i th device
\mathcal{D}^i	Dataset on the <i>i</i> th device
$z_{t,h}^i$	Data (minibatch) sampled from \mathcal{D}^i
γ	Learning rate
α	Mixing hyperparameter
ρ	Regularization weight
t- au	Staleness
s(t- au)	Function of staleness for adaptive α
	All the norms in this paper are l_2 -norms
Device	Where the training data are placed
Worker	One worker on each device,
	process that trains the model

3 PROBLEM FORMULATION

We consider federated learning with n devices. On each device, there is a worker process that trains the model on local data. The overall goal is to train a global model $x \in \mathbb{R}^d$ using data from all the devices.

To do so, we consider the following optimization problem:

$$\min_{x \in \mathbb{R}^d} F(x),$$

where $F(x) = \frac{1}{n} \sum_{i \in [n]} \mathbb{E}_{z^i \sim \mathcal{D}^i} f(x; z^i)$, for $\forall i \in [n]$, z^i is sampled from the local data \mathcal{D}^i on the *i*th device.

Note that different devices have different local datasets, i.e., $\mathcal{D}^i \neq \mathcal{D}^j, \forall i \neq j$. Thus, samples drawn from different devices may have different expectations i.e. in general, $\mathbb{E}_{z^i \sim \mathcal{D}^i} f(x; z^i) \neq \mathbb{E}_{z^j \sim \mathcal{D}^j} f(x; z^j), \forall i \neq j$.

4 METHODOLOGY

A single execution of federated optimization has T global epochs. In the t^{th} epoch, the server receives a locally trained model x_{new} from an arbitrary worker, and updates the global model by weighted averaging:

$$x_t = (1 - \alpha)x_{t-1} + \alpha x_{new},$$

where $\alpha \in (0,1)$ is the mixing hyperparameter.

On an arbitrary device i, after receiving a global model x_t (potentially stale) from the server, we locally solve the following regularized optimization problem using SGD for arbitrary number of iterations:

$$\min_{x \in \mathbb{R}^d} \mathbb{E}_{z^i \sim \mathcal{D}^i} f(x; z^i) + \frac{\rho}{2} ||x - x_t||^2.$$

The server and workers conduct updates asynchronously. The server immediately updates the global model whenever it receives a local model. The communication between the server and workers is non-blocking.

The detailed algorithm is shown in Algorithm 1. The model parameter $x_{\tau,h}^i$ is updated in hth local iteration after receiving x_{τ} , on the ith device. $z_{\tau,h}^i$ is the data randomly drawn in hth local iteration after receiving x_{τ} , on the ith device. H_{τ}^i is the number of local iterations after receiving x_{τ} , on the ith device. γ is the learning rate and T is the total number of global epochs.

Remark 1. On the server side, there are two threads running asynchronously in parallel: scheduler and updater. The scheduler periodically triggers training tasks on some selected workers. The updater receives locally trained models from workers and updates the global model. There could be multiple updater threads with read-write lock on the global model, which improves the throughput. The scheduler randomizes the timing of training tasks to avoid overloading the updater thread, and controls the staleness $(t-\tau)$ in the updater thread). Since we do not focus on the system design in this paper, we will not discuss the details of the scheduling strategies.

Intuitively, larger staleness results in greater error when updating the global model. For the local models with large staleness $(t-\tau)$, we can decrease α to mitigate the error caused by staleness. As shown in Algorithm 1, optionally,

we can use a function $s(t - \tau)$ to decide the value of α . We list some choices for $s(t - \tau)$, parameterized by a, b:

- Linear: $s_a(t-\tau) = \frac{1}{a(t-\tau)+1}, a > 0.$
- Polynomial: $s_a(t-\tau) = (t-\tau+1)^{-a}, a > 0.$
- Exponential: $s_a(t-\tau) = \exp(-a(t-\tau)), a > 0.$

• Hinge:
$$s_{a,b}(t-\tau)=\begin{cases} 1 & \text{if } t-\tau \leq b \\ \frac{1}{a(t-\tau-b)+1} & \text{otherwise} \end{cases},$$
 $a>0, b\geq 0.$

Algorithm 1 Asynchronous Federated Optimization (FedAsync)

Server Process:

Input: $\alpha \in (0,1)$ Initialize $x_0, \alpha_t \leftarrow \alpha, \forall t \in [T]$

Scheduler Thread:

Scheduler periodically triggers some training tasks on some workers, and sends them the latest global model with time stamp

Updater Thread:

for all epoch $t \in [T]$ do

Receive the pair (x_{new}, τ) from any worker Optional: $\alpha_t \leftarrow \alpha \times s(t-\tau)$, $s(\cdot)$ is a function of the staleness

$$x_t = (1 - \alpha_t)x_{t-1} + \alpha_t x_{new}$$

end for

Worker Processes:

for all $i \in [n]$ in parallel do

If triggered by the scheduler:

Receive the pair of the global model and its time stamp (x_t, t) from the server

$$\tau \leftarrow t, x_{\tau,0}^i \leftarrow x_t$$

For μ -weakly convex F:

Define $g_{x_t}(x;z) = f(x;z) + \frac{\rho}{2} ||x - x_t||^2$, where $> \mu$

for all local iteration $h \in [H^i_{\tau}]$ do

Randomly sample $z_{\tau,h}^i \sim \mathcal{D}^i$

$$x_{\tau,h}^i \leftarrow \left\{ \begin{array}{l} \text{Option I, for strongly convex } F \colon \\ x_{\tau,h-1}^i - \gamma \nabla f(x_{\tau,h-1}^i; z_{\tau,h}^i) \\ \text{Option II, for weakly convex } F \colon \\ x_{\tau,h-1}^i - \gamma \nabla g_{x_t}(x_{\tau,h-1}^i; z_{\tau,h}^i) \end{array} \right.$$

end for

Push $(x_{\tau,H_{\tau}^{i}}^{i},\tau)$ to the server

end for

5 CONVERGENCE ANALYSIS

In this section, we prove the convergence of Algorithm 1 with non-IID data.

5.1 ASSUMPTIONS

First, we introduce some definitions and assumptions for our convergence analysis.

Definition 1. (Smoothness) A differentiable function f is L-smooth if for $\forall x, y$,

$$f(y) - f(x) \le \langle \nabla f(x), y - x \rangle + \frac{L}{2} ||y - x||^2,$$

where L > 0.

Definition 2. (Strong convexity) A differentiable function f is μ -strongly convex if for $\forall x, y$,

$$\langle \nabla f(x), y - x \rangle + \frac{\mu}{2} ||y - x||^2 \le f(y) - f(x),$$

where $\mu \geq 0$. Note that if $\mu = 0$, f is convex.

Definition 3. (Weak convexity) A differentiable function f is μ -weakly convex if the function g with $g(x) = f(x) + \frac{\mu}{2} ||x||^2$ is convex, where $\mu \geq 0$.

Remark 2. Note that when f is μ -weakly convex, then f is convex if $\mu = 0$, and potentially non-convex if $\mu > 0$.

Assumption 1. (Existence of global optimum) We assume that there exists a set $\mathcal{X}_* \subset \mathbb{R}^d$, where any element $x_* \in \mathcal{X}_*$ is a global optimum of F(x), $x_* = \inf_x F(x)$, and $\nabla F(x_*) = 0$.

5.2 CONVERGENCE GUARANTEES

Based on the assumptions above, we have the following convergence guarantees. Detailed proofs can be found in the appendix.

Theorem 1. Assume that the global loss function F is L-smooth and μ -strongly convex, and each worker executes at least H_{min} local updates before pushing models to the server. Furthermore, we assume that for $\forall x \in \mathbb{R}^d, i \in [n]$, and $\forall z \sim \mathcal{D}^i$, we have $\mathbb{E}\|\nabla f(x;z) - \nabla F(x)\|^2 \leq V_1$, and $\mathbb{E}\left[\|\nabla f(x;z)\|^2\right] \leq V_2$. Taking $\gamma < \frac{1}{L}$, after T global updates/epochs on the server, Algorithm 1 with Option I converges to a global optimum $x_* \in \mathcal{X}_*$:

$$\mathbb{E}[F(x_T) - F(x_*)] \\ \leq (\beta)^T [F(x_0) - F(x_*)] + (1 - (\beta)^T) \mathcal{O}(V_1 + V_2),$$

where
$$\beta = 1 - \alpha + \alpha (1 - \gamma \mu)^{H_{min}}$$
.

Remark 3. The mixing hyperparameter $\alpha \in (0,1)$ controls the trade-off between the convergence rate and additional error caused by variance. When $\alpha \to 1$, the

convergence rate approaches $(1 - \gamma \mu)^{TH_{min}}$, with the additional error $\mathcal{O}(V_1 + V_2)$:

$$\mathbb{E}\left[F(x_T) - F(x_*)\right] \\ \leq (1 - \gamma \mu)^{TH_{min}} \left[F(x_0) - F(x_*)\right] + \mathcal{O}\left(V_1 + V_2\right).$$

When $\alpha \to 0$, $\beta \to 1$. As a result, the variance $(1-\beta^T)\mathcal{O}(V_1+V_2)$ is reduced to 0. In practice, to balance the convergence rate and the variance reduction, we use diminishing α : $\alpha_t \propto \frac{1}{\sqrt{t}}, \forall t \in [T]$, such that the the algorithm converges fast at the beginning, and reduces the variance at the end.

Theorem 2. Assume that the global loss function F is L-smooth and μ -weakly convex (potentially non-convex), and each worker executes at least H_{min} local updates before pushing models to the server. Furthermore, we assume that for $\forall x \in \mathbb{R}^d, i \in [n]$, and $\forall z \sim \mathcal{D}^i$, we have $\mathbb{E}\|\nabla f(x;z) - \nabla F(x)\|^2 \leq V_1$, and $\mathbb{E}\left[\|\nabla g_{x'}(x;z)\|^2\right] \leq V_2$, $\forall x'$. Taking $\rho > \mu$ and $\gamma < \min(\frac{1}{L}, \frac{2}{\rho - \mu})$, after T global updates/epochs on the server, Algorithm 1 with Option II converges to a global optimum $x_* \in \mathcal{X}_*$:

$$\begin{split} & \mathbb{E}\left[F(x_T) - F(x_*)\right] \\ & \leq (\beta)^T \left[F(x_0) - F(x_*)\right] + \left(1 - (\beta)^T\right) \mathcal{O}(V_1 + V_2), \\ & \text{where } \beta = 1 - \alpha + \alpha \left[1 - \frac{\gamma(\rho - \mu)}{2}\right]^{H_{min}}. \end{split}$$

Algorithm 2 Federated Averaging (FedAvg)

```
Input: k \in [n]
Initialize x_0
for all epoch t \in [T] do

Randomly select a group of k workers, denoted as S_t \subseteq [n]
for all i \in S_t in parallel do

Receive the latest global model x_{t-1} from the server x_{t,0}^i \leftarrow x_{t-1}
for all local iteration h \in [H_t^i] do

Randomly sample z_{t,h}^i
x_{t,h}^i \leftarrow x_{t,h-1}^i - \gamma \nabla f(x_{t,h-1}^i; z_{t,h}^i)
end for

Push x_{t,H_t^i}^i to the server
end for

Update the global model: x_t = \frac{1}{k} \sum_{i \in S_t} x_{t,H_t^i}^i
end for
```

6 EXPERIMENTS

In this section, we empirically evaluate the proposed algorithm.

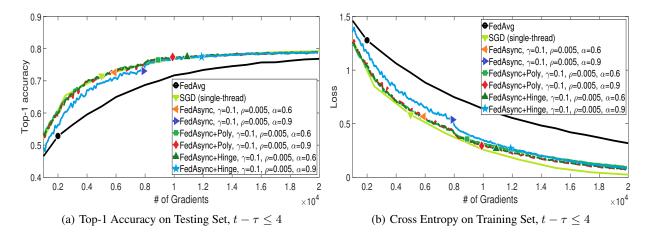


Figure 1: Metrics vs. # of gradients. The maximum staleness is 4. Learning rate γ decays by 0.5 at the 800th global epoch. For FedAsync+Poly, we take a=0.5. For FedAsync+Hinge, we take a=10,b=4. Note that when the maximum staleness is 4, FedAsync and FedAsync+Hinge with b=4 are the same.

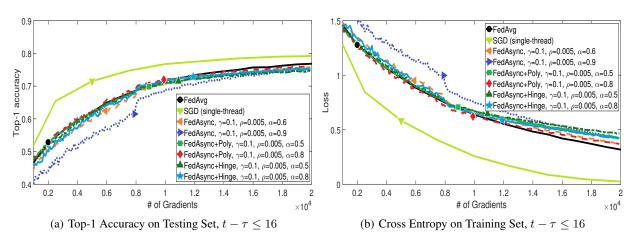


Figure 2: Metrics vs. # of gradients. The maximum staleness is 16. Learning rate γ decays by 0.5 at the 800th global epoch. For FedAsync+Poly, we take a=0.5. For FedAsync+Hinge, we take a=10,b=4.

Algorithm 3 SGD (Single Thread)	
Initialize x_0	
for all iteration $t \in [T]$ do	
Randomly sample z_t	
$x_t \leftarrow x_{t-1} - \gamma \nabla f(x_{t-1}; z_t)$	
end for	

6.1 DATASETS

We conduct experiments on the benchmark CIFAR-10 image classification dataset (Krizhevsky & Hinton, 2009), which is composed of 50k images for training and 10k images for testing. We resize each image and crop it to the shape of (24, 24, 3). We use convolutional neural network (CNN) with 4 convolutional layers followed by 1

fully connected layer. We chose a simple network architecture so that it can be easily handled by mobile devices. The detailed network architecture can be found in the appendix. In each experiment, the training set is partitioned onto n=100 devices. Each of the n=100 partitions has 500 images. For any worker, the minibatch size for SGD is 50.

6.2 EVALUATION SPECIFICS

The experiments are conducted on CPU devices. We implement the federated optimization algorithms using the MXNET (Chen et al., 2015) framework.

The baseline algorithm is *FedAvg* introduced by McMahan et al. (2016), which is synchronous federated optimization. The detailed *FedAvg* is shown in Algorithm 2.

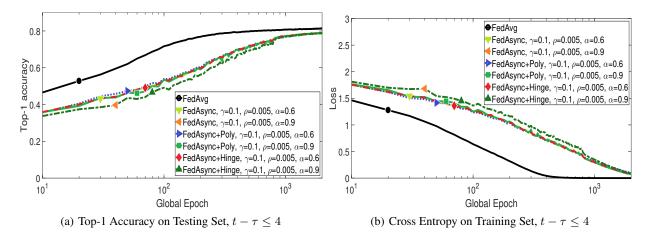


Figure 3: Metrics vs. # of global epochs. The maximum staleness is 4. Learning rate γ decays by 0.5 at the 800th global epoch. For FedAsync+Poly, we take a=0.5. For FedAsync+Hinge, we take a=10,b=4. Note that when the maximum staleness is 4, FedAsync+Hinge with b=4 are the same.

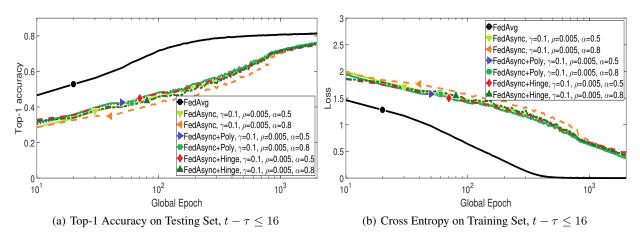


Figure 4: Metrics vs. # of global epochs. The maximum staleness is 16. Learning rate γ decays by 0.5 at the 800th global epoch. For FedAsync+Poly, we take a=0.5. For FedAsync+Hinge, we take a=10,b=4.

For FedAvg, in each epoch, k=10 devices are randomly selected to launch local updates. We also use single-thread SGD as the baseline. The detailed SGD is shown in Algorithm 3. For the two baseline algorithms, we use grid search to tune the learning rates and report the best results according to the top-1 accuracy on the testing set.

We repeat each experiment 10 times and take the average. We use top-1 accuracy on the testing set, and cross entropy loss function on the training set as the evaluation metrics.

For convenience, we name Algorithm 1 as FedAsync. We also test the performance of FedAsync with adaptive mixing hyperparameters $\alpha_t = \alpha \times s(t-\tau)$, as mentioned in Section 4. We employ the following two strategies:

• Polynomial:
$$s_a(t-\tau) = (t-\tau+1)^{-a}, a > 0.$$

• Hinge:
$$s_{a,b}(t-\tau) = \begin{cases} 1 & \text{if } t-\tau \leq b \\ \frac{1}{a(t-\tau-b)+1} & \text{otherwise} \end{cases}$$
, $a>0, b>0$.

For convenience, we refer to FedAsync with polynomial adaptive α as FedAsync+Poly, and FedAsync with hinge adaptive α as FedAsync+Hinge.

In general, it is non-trivial to compare asynchronous training and synchronous training in a fair way. We conduct three comparisons: metrics vs. number of global epochs, metrics vs. number of gradients, and metrics vs. number of communications:

• The number of global epochs counts how many times the global model is updated. The total number of global epochs is T=2000 in both Algorithm 1 and

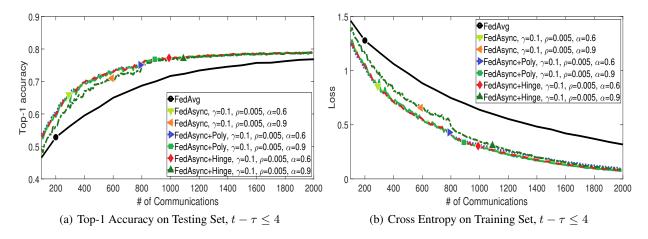


Figure 5: Metrics vs. # of communications. The maximum staleness is 4. Learning rate γ decays by 0.5 at the 800th global epoch. For FedAsync+Poly, we take a=0.5. For FedAsync+Hinge, we take a=10,b=4. Note that when the maximum staleness is 4, FedAsync and FedAsync+Hinge with b=4 are the same.

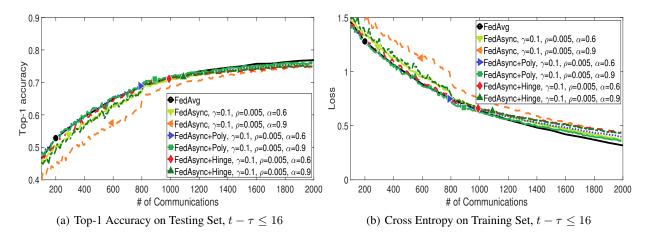


Figure 6: Metrics vs. # of communications. The maximum staleness is 16. Learning rate γ decays by 0.5 at the 800th global epoch. For FedAsync+Poly, we take a=0.5. For FedAsync+Hinge, we take a=10,b=4.

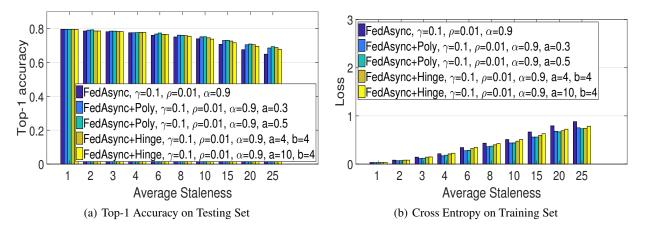


Figure 7: Metrics at the end of training (at the 2000th epoch), with different staleness. Learning rate γ decays by 0.5 at the 800th global epoch.

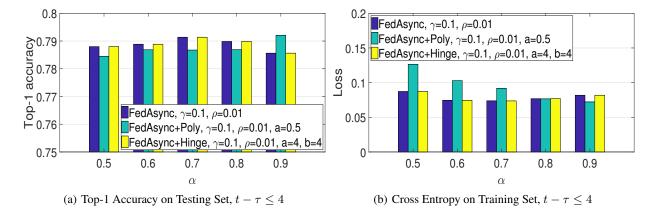


Figure 8: Metrics at the end of training (at the 2000th epoch), with different α . The maximum staleness is 4. Learning rate γ decays by 0.5 at the 800th global epoch. For FedAsync+Poly, we take a=0.5. For FedAsync+Hinge, we take a=4,b=4. Note that when the maximum staleness is 4, FedAsync and FedAsync+Hinge with b=4 are the same.

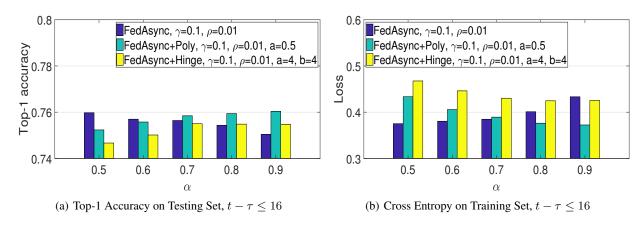


Figure 9: Metrics at the end of training (at the 2000th epoch), with different α . The maximum staleness is 16. Learning rate γ decays by 0.5 at the 800th global epoch. For FedAsync+Poly, we take a=0.5. For FedAsync+Hinge, we take a=4,b=4.

Algorithm 2. Single-thread SGD does not have global epochs, so we ignore it in the experiments of metrics vs. # of global epochs.

- The number of gradients is the number of gradients applied to the global model. Note that for both Algorithm 1 and Algorithm 2, an epoch of local iterations is a full pass of the local dataset. Thus, for FedAsync, in each global epoch, 10 gradients is applied to the global model. For FedAvg, since $k=10,\ 10\times 10=100$ gradients is applied to the global model in each global epoch.
- The number of communications measures the communication overhead on the server side. We count how many times the models are exchanged (sent/received) on the server. On average, in each global epoch, FedAvg has 10× the communications of FedAsync. Single-

thread SGD has no communication, so we ignore it.

In all the experiments, we simulate the asynchrony by randomly sampling the staleness $(t-\tau)$ from a uniform distribution.

6.3 EMPIRICAL RESULTS

We test the algorithms with different initial learning rates γ , regularization weights ρ , mixing hyperparameter α , and staleness. The learning rates decays by 0.5 at the 800th global epoch.

In Figure 1 and 2, we show how *FedAsync* converges when the number of gradients grows. We can see that when the overall staleness is small, *FedAsync* converges as fast as *SGD*, and faster than *FedAvg*. When the staleness is larger, *FedAsync* converges slower. In the worst case,

FedAsync has similar convergence rate as FedAvg. When α is too large, the convergence can be unstable. Using adaptive α , the convergence can be robust to large α . Note that when the maximum staleness is 4, FedAsync and FedAsync+Hinge with b=4 are the same.

In Figure 3 and 4, we show how FedAsync converges when the number of global epochs grows. Obviously, FedAvg makes more progress in each epoch. However, in each epoch, FedAvg has to wait until all the k=10 workers respond, while FedAsync only needs one worker's response to move on to the next epoch.

In Figure 5 and 6, we show how *FedAsync* converges when the communication overhead grows. With the same amount of communication overhead, *FedAsync* converges faster than *FedAvg* when staleness is small. When staleness is large, *FedAsync* has similar performance as *FedAvg*.

In Figure 7, we show how staleness affects the convergence of *FedAsync*. Overall, larger staleness makes the convergence slower, but the influence is not catastrophic. Furthermore, using adaptive mixing hyperparameters, the instability caused by large staleness can be mitigated.

In Figure 8 and 9, we show how α affects the convergence of FedAsync. In general, FedAsync is robust to different α . Note that the difference is so tiny that we have to zoom in. When the staleness is small, adaptive mixing hyperparameter is less necessary. When the staleness is large, smaller α is better for FedAsync, while larger α is better for FedAsync+Hinge. That is because adaptive α is automatically adjusted to be smaller when the staleness is large, so that we should not manually decrease α .

6.4 DISCUSSION

In general, the convergence rate of FedAsync is between single-thread SGD and FedAvg. Larger α and smaller staleness makes FedAsync closer to single-thread SGD. Smaller α and larger staleness makes FedAsync closer to FedAvg.

FedAsync is generally insensitive to hyperparameters. When the staleness is large, we can tune α to improve the convergence. Without adaptive α , smaller α is better for larger staleness. For adaptive α , the best choice is FedAsync+Poly with $s_a(t-\tau)=(t-\tau+1)^{-a}$, a=0.5.

Larger staleness makes the convergence slower and unstable. There are three ways to control the influence of staleness:

• On the serve side, the updater thread can drop the updates with large staleness $(t - \tau)$. This can also be

viewed as a special case of adaptive mixing hyperparameter α . In particular, when the staleness is too large, we can simply take $\alpha=0$.

- More generally, using adaptive mixing hyperparameters improves the convergence, as shown in Figure 7. Different strategies has different improvement. So far we find that FedAsync+Poly with $s_a(t-\tau)=(t-\tau+1)^{-a}, a=0.5$ has the best performance.
- On the server side, the scheduler thread can control the assignment of training tasks to the workers. If the ondevice training is triggered less frequently, the overall staleness will be smaller.

Systematically, *FedAsync* has the following advantages compared to *FedAvg*:

- Efficiency: The server can receive the updates from the workers at any time. Unlike FedAvg, stragglers' updates will not be dropped. When the staleness is small, FedAsync converges much faster than FedAvg. In the worst case, when the staleness is large, FedAsync still has similar performance as FedAvg.
- Flexibility: If some workers are no longer eligible for the training tasks (the devices are no longer idle, charging, or connected to unmetered networks), they can temporarily save the workspace, and continue the training or push the trained model to the server later. This also gives more flexibility to the scheduler on the server. Unlike FedAvg, FedAsync can schedule training tasks even if the workers are currently ineligible, since the server does not wait until the workers respond. The currently ineligible workers can start the training tasks later.
- Scalability: Compared to FedAvg, FedAsync can handle more workers running in parallel since all the updates on the server and the workers are non-blocking. The server only needs to randomize the responding time of the workers to avoid congesting the network.

7 CONCLUSION

We proposed a novel asynchronous federated optimization algorithm on non-IID training data. The algorithm has near-linear convergence to a global optimum, for both strongly and non-strongly convex problems, as well as a restricted family of non-convex problems. For future work, we plan to investigate the design of strategies to adaptively tune the mixing hyperparameters.

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