System F Language Specification

Syntax

Expressions

\overline{e}	:=	1	literals
Е	.—	t	
		v	expression identifier
		(e)	parenthesized
		$e[\tau]$	type concretization
		e_1 e_2	application
		$e_1 op e_2$	binary operation
		(e_1,\ldots,e_n)	n -tuples, $n \geq 2$
		$\lambda v : \tau \cdot e$	lambda abstraction ¹
		$\Lambda t. e$	type $abstraction^2$
		$\mathtt{let}\ p = e_1\ \mathtt{in}\ e_2$	let binding
		$\mathtt{if}\ e_1\ \mathtt{then}\ e_2\ \mathtt{else}\ e_3$	if expression
\overline{l}	:=	null	unit literal: Unit
		true false	boolean literals: Bool
		~2 ~1 0 1 2	64-bit signed ints: Int
\overline{p}	:=	_: τ	discarded pattern
		v: au	single argument
		(p_1, \ldots, p_n)	n -tuple destructor, $n \ge 2$

Types

au	:= t	type identifier
	(au)	parenthesized
	$ au_1$ -> $ au_2$	arrow types
	$\forall t. \tau$	universal types
	$\tau_1 * \ldots * \tau_n$	tuple types, $n \ge 2$
	$\verb Int Bool Unit $	built-in types

Declarations

	δ := let p) = e	declaration
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One can also denote a curried multi-argument function with the syntax λ ($v_1:t_1$) ... ($v_n:t_n$). e, which desugars to n nested lambda expressions. Note that in this case, parentheses are needed around each annotated argument.

²Similarly, Λ t_1 ... t_n . e is n nested type abstractions.

Alternative syntax

We can write \setminus or lambda instead of λ . We can write any in place of Λ . We can write forall in place of \forall .

Semantics:

Call-by-value big step semantics. When a bound variable is bound again, the new binding takes over. There is no one-type tuples Lexical scope.