# APFEL v2.6.1: A PDF Evolution Library with QED corrections

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## Abstract

In this document we present the user manual for the APFEL library. Written in FORTRAN 77, all the functionalities can also be accessed via the C/C++ and Python interfaces. For simplicity, we will restrict ourselves to the description of the C/C++ interface, but the usage of the FORTRAN 77 and Python interfaces is very similar and examples of their use are provided in the examples folder of the APFEL source code. First of all, we will discuss how to install APFEL and how to execute the basic example programs. After that, we will list the various customization options that can be accessed by the user for both the PDF evolution and the DIS structure functions modules.

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# 1 Installation

The APFEL library is available from its HepForge website:

http://apfel.hepforge.org/

and from the GitHub webpage:

https://github.com/scarrazza/apfel

It can also be accessed directly from the git repository. The last development version can be downloaded by giving:

git clone https://github.com/scarrazza/apfel.git

For the tagged versions one can use the git tag commands:

```
git tag -1
git checkout tags/tag_name
```

to switch to any of the past releases. We strongly recommend to use the latest stables release

The installation of the APFEL library can be easily done following the standard autotools sequence:

```
./configure
make
make install
```

which automatically installs APFEL in /usr/local/. Note that by default the APFEL library requires an installation of the LHAPDF PDF library<sup>1</sup>. However, an LHAPDF-less installation is also supported by giving:

```
./configure --disable-lhapdf
```

To use a different installation path, one simply needs to use the option:

```
./configure --prefix=/path/to/the/installation/folder
```

In this case, the APFEL installation path should be included to the environmental variable LD\_LIBRARY\_PATH. This can be done adding to the local .bashrc file (or .profile file on Mac) the string:

```
export LD_LIBRARY_PATH=$LD_LIBRARY_PATH:/path/to/the/installation/←
folder/lib
```

Once APFEL has been properly compiled and installed, the configuration script apfel-config should automatically be present. Such script is useful to determine the compiler flags. Type:

```
apfel-config --help
```

in a shell to see all the possible options. Particularly useful is the --list-funcs flag that lists all the functions available in APFEL along with a short explanation. In addition, also the shell script apfel is provided which starts an interactive console session of APFEL providing a prompt tool to use the library without coding.

In the following we will list and illustrate all the functionalities of APFEL and explaining how they can be accessed by the user. The most recent version of APFEL provide also an additional module to compute DIS (and SIA) structure functions in different mass scheme. Such module is dependent of the original PDF evolution module as it inherits from it many of the setting functions that we will describe in the next section. We will start describing

 $<sup>^1{</sup>m The}$  current release of APFEL assumes that LHAPDF version 6 has been previously installed as version 5 is no longer supported.

the functions of the PDF evolution module and we will devote the following section to a thourough description of the DIS module.

# 2 The PDF evolution module

The basic usage of the PDF evolution module of APFEL requires only two steps to have the complete set of evolved PDFs. The first step is the initialization of APFEL through the call of the following function:

```
APFEL::InitializeAPFEL();
```

This will precompute all the needed evolution operators that enter the discretized DGLAP equation. Let us recall that once the general settings of the evolution have been defined (perturbative order, heavy quark masses, reference value of  $\alpha_s$ , and so on), the initialization needs to be performed only once, irrespective of the scales that are used in the PDF evolution. The second step consists in performing the actual PDF evolution between the initial scale Q0 and the final scale Q (in GeV). This can be achieved using the function:

```
APFEL::EvolveAPFEL(Q0,Q);
```

Calling this function APFEL solves the discretized DGLAP equations using the evolution operators precomputed in the initialization step.

Now the user can access the evolved PDFs at the scale Q via the use of the functions:

```
APFEL::xPDF(i,x);
APFEL::xgamma(x);
```

where the real variable x is the desired value of Bjorken-x while the integer variable i in the function xPDF, which runs from -6 to 6, corresponds to the quark flavor index according to the following convention: Note that in APFEL we have explicitly separated

the access to the quark and gluon PDFs (via xPDF) and from that to the photon PDF (via xgamma). Note also that the functions xPDF and xgamma return x times the PDFs (i.e. the momentum fractions).

The basic information given above is enough to write a simple and yet complete program that performs PDF evolution using APFEL. As an illustration, a C/C++ program that computes and tabulates PDFs to be compared with the Les Houches PDF benchmark evolution tables would be the following:

```
#include <iostream>
#include <iomanip>
#include <cmath>
#include "APFEL.h"
```

```
5 using namespace std;
  int main()
7
  {
8
    // Define grid in x
9
    double xlha[11] = {1e-7, 1e-6, 1e-5, 1e-4, 1e-3, 1e-2,
10
        1e-1, 3e-1, 5e-1, 7e-1, 9e-1};
11
12
13
    // Precomputes evolution operators on the grid
    APFEL::InitializeAPFEL();
14
    // Perform evolution
16
    double Q0 = sqrt(2);
17
    double Q = sqrt(10000);
18
    APFEL::EvolveAPFEL(Q0,Q);
19
20
    cout << scientific << setprecision(5) << endl;</pre>
21
    cout << "
22
                x
          << setw(11) << "
                              u-ubar
23
24
          << setw(11) << "
                              d-dbar
          << setw(11) << " 2(ubr+dbr)
          << setw(11) << "
26
                              c+cbar
          << setw(11) << "
27
                              gluon
          << setw(11) << "
                                         " << endl;
28
                              photon
29
    cout << scientific;</pre>
30
    // Tabulate PDFs for the LHA x values
31
    for (int i = 0; i < 11; i++)</pre>
32
      cout << xlha[i] << "\t"
33
      << APFEL::xPDF(2,xlha[i]) - APFEL::xPDF(-2,xlha[i]) << "\t"
34
      << APFEL::xPDF(1,xlha[i]) - APFEL::xPDF(-1,xlha[i]) << "\t"
35
      << 2*(APFEL::xPDF(-1,xlha[i]) + APFEL::xPDF(-2,xlha[i])) << "\t"
      << APFEL::xPDF(4,xlha[i]) + APFEL::xPDF(-4,xlha[i]) << "\t"</pre>
37
      << APFEL::xPDF(0,xlha[i]) << "\t"
38
      << APFEL::xgamma(xlha[i]) << "\t"
39
40
       << endl;
41
    return 0;
42
43 }
```

It should be noticed that this example code uses the default settings of APFEL for the evolution parameters such as: initial scale PDFs, perturbative order, heavy quark masses, values of the couplings, etc. In the following we will discuss how the user can customize the settings for the PDF evolution in APFEL.

# 2.1 Customization of the PDF evolution

The customization of the PDF evolution with APFEL can be achieved using a number of dedicated functions, to be called before the initialization stage, that is before calling InitializeAPFEL<sup>2</sup>. We will subdivide the available functions into three cathegories:

<sup>&</sup>lt;sup>2</sup>This is not entirely precise because there is a number of customization functions that are effective only at the evolution level and thus can be called also after InitializeAPFEL but before EvolveAPFEL. We will discuss this feature case by case when going through all functions available in APFEL.

- the *setting functions* which provide the real costumization tools. These functions allow the user to change the way how the initialization and the output (see next items) functions behave.
- The *initialization functions* which are resposible to perform the "main" operations, like initializing the evolution factor and evolving PDFs.
- The *output functions* which finally return the result of a given set of setting and initialization functions.

In the following we will list and comment all the functions belonging to each of the cathegories above. Finally, we remind the reader that running the configuration script apfel-config with the --list-funcs flag will list all the functions available in APFEL along with a short explanation.

## 2.1.1 Setting functions

Bofore going through the various setting functions, the user should be aware of the fact that APFEL has a set of default settings that are used if the user does not intervene to change any of them. This is why the example described above needs only a very limited number of steps. However, while each time that APFEL is run a banner with a list of the main settings is displayed, it is usefull to report here the default settings of APFEL. We will first go through all the setting functions and only at the end we will report the default settings so that the meaning of all of them should be clear to the reader who went through this section.

Bofore proceeding with the descitpion of the setting functions of the evolution module, it is useful to notice that in the following we will use the identifiers int, double, bool and string to specify the type of entry expected by each of the fuctions described below.

## APFEL::SetPerturbativeOrder(int pto);

This function sets the perturbative order of the PDF evolution to "pto". The integer "pto" can take the values 0, 1 of 2 according to whether the PDF evolution is performed at  $\mathcal{O}(\alpha_s)$ ,  $\mathcal{O}(\alpha_s^2)$ , or  $\mathcal{O}(\alpha_s^3)$ , that is LO, NLO and NNLO, respectively. This function also sets the perturbative order of the evolution of the couplings  $\alpha_s$  and  $\alpha$  and possibly of the heavy quark masses. The default for pto" is 2.

## APFEL::SetTheory(string theory);

This function sets the theory to be used in the evolution. The alternatives for theory are:

- "QCD": the PDF evolution is done solving the pure QCD DGLAP equations,
- "QED": the PDF evolution is done solving the pure QED DGLAP equations,
- "QUnid": the PDF evolution is done solving the coupled QCD+QED DGLAP equations as explained above.

There are more options available that access more "exotic" (and obsolete) solutions of the coupled QCD+QED DGLAP equations. They are:

- "QCEDP" for QCD+QED in parallel,
- "QCEDS" for QCD+QED in series,
- "QECDP" for QED+QCD in parallel,
- "QECDS" for QED+QCD in series,
- "QavDP" for the averaged solution in parallel,
- "QavDS" for the averaged solution in series,

and they refer to different combinations of the separate QCD and QED evolutions. The reader can refer to the original APFEL publication for a detailed explanation. However, the use of these solution is discouraged unless the user is well aware of their meaning. The default is "QCD".

#### APFEL::SetVFNS();

This function sets the Variable-Flavour Number Scheme (VFNS) for the PDF,  $\alpha_s$ , and  $\alpha^3$  evolution. In practice this means that, if any heavy quark threshold is encountered during the evolution, the solutions of the DGLAP equation below and above the threshold itself will be properly matched. This option is used as a default.

```
APFEL::SetFFNS(int nfl);
```

This function, as opposed to SetVFNS, sets the Fixed-Flavour Number Scheme (FFNS) with "nf1" active flavours for the PDF,  $\alpha_s$  and  $\alpha$  (and  $\overline{\rm MS}$ ) evolution. This function forces the evolution to be done with "nf1" active flavours in any evolution range. The allowed values are nf1 = 3, 4, 5 and 6.

```
APFEL::SetAlphaQCDRef(double alpharef, double Qref);
```

This function sets the reference values of the strong coupling  $\alpha_s$  at the scale "Qref" in GeV to "alpharef". The default is "alpharef" = 0.35 at "Qref" =  $\sqrt{2}$  GeV.

```
APFEL::SetAlphaQEDRef(double alpharef, double Qref);
```

This function sets the reference values of the QED coupling  $\alpha$  at the scale "Qref" in GeV to "alpharef". The default is "alpharef" =  $7.496252 \cdot 10^{-3}$  at "Qref" = 1.777 GeV.

```
APFEL::SetLambdaQCDRef(double lambdaref, int nref);
```

 $<sup>{}^{3}</sup>$ In case the  $\overline{\rm MS}$  definition for the heavy quark masses is used (see below) and the running of the masses has been enabled, this function sets the VFNS also for the running of the heavy quark masses.

This function sets the value of  $\Lambda_{\rm QCD}$  in GeV with "nref" flavours to "lambdaref". This value is used only if the "lambda" solution of the  $\beta$ -function equation (see below) is used to compute the running of  $\alpha_s$ . The default is "lambdaref" = 0.220 GeV with "nref" = 5

```
APFEL::SetPoleMasses(double mc, double mb, double mt);
```

This function sets the values of the heavy quark thresholds in GeV and sets the pole-mass scheme as a renormalization scheme for the heavy quark masses. This function is used as a default with "mc" =  $\sqrt{2}$  GeV, "mb" = 4.5 GeV, "mt" = 175 GeV.

```
APFEL::SetMSbarMasses(double mc, double mb, double mt);
sets the values of the heavy quark thresholds
in GeV in the MSbar scheme.
```

This function, as opposed to SetPoleMasses, sets the values of the heavy quark masses in GeV and sets the  $\overline{\rm MS}$  scheme as a renormalization scheme for the heavy quark masses. The reference scales at which the masses are defined can be specified using the SetMassScaleReference function (see below).

```
APFEL::SetMassScaleReference(double Qc, double Qb, double Qt);
```

This function sets the reference scales in GeV at which heavy quark masses are given. This function is effective only if the  $\overline{\rm MS}$  definition for the heavy quark masses is used and has no effect if the pole masses are used. If this function is not called, APFEL will assume that the mass reference scales are equal to the masses themselves. In other words, in the absence of a call to this function when using the  $\overline{\rm MS}$  definition for the heavy quark masses, the SetMSbarMasses function will define  $m_c(m_c)$ ,  $m_b(m_b)$  and  $m_t(m_t)$ . If instead this function is called and the reference scales are found to be different from the masses themselves, the values of  $m_c(m_c)$ ,  $m_b(m_b)$  and  $m_t(m_t)$  are also evaluated by applying the RG evolution as they are needed as thresholds for the VFNS evolution when using the  $\overline{\rm MS}$  definition for the heavy quark masses.

```
APFEL::EnableMassRunning(bool);
```

This function enables or disables the running of the  $\overline{\rm MS}$  masses. This is effective only if the SetMSbarMasses is also called and in practice switches on and off the solution RG equation of the heavy quark masses. The default is true.

```
APFEL::SetTauMass(double mtau);
```

This function sets the values of the  $\tau$  lepton in GeV to mtau. This function is effective only if the evolution of the lepton PDFs is enabled (see below). The default is "mtau" = 1.777 GeV.

```
APFEL::SetMaxFlavourAlpha(int nf);
```

This function sets the maximum number of active flavours in the evolution of the couplings  $\alpha_s$  and  $\alpha$  (and the masses) to  $\mathbf{nf}$ . In practice, this function forces the code not to match the solution of the  $\beta$ -function and  $\gamma$ -function equations at a given threshold if that threshold is above the maximum number allowed  $\mathbf{nf}$ . The default is " $\mathbf{nf}$ " = 6.

```
APFEL::SetMaxFlavourPDFs(int nf);
```

This function sets the maximum number of active flavours in the evolution of PDFs to nf. In practice, this function forces the code not to match the solution of the DGLAP equation at a given threshold if that threshold is above the maximum number allowed nf. The default is "nf" = 6.

```
APFEL::SetRenFacRatio(double ratio);
```

This function sets the ratio between factorization scale  $\mu_F$  (entering PDFs) and renormalization scale  $\mu_R$  (entering the couplings and possibly the heavy quark masses) to "ratio". If "ratio" is different from one, APFEL will assume that  $\mu_R = \mu_F$ / "ratio" and, as explained above, this gives rise to additional terms in the higher order splitting functions. The default is "ratio" = 1.

```
APFEL::SetTimeLikeEvolution(bool);
```

This function enables or disables the time-like evolution. This evolution, as opposed to the space-like evolution used for PDFs, is used to evolve fragmentation functions (FFs). The default is false.

```
APFEL::SetSmallxResummation(bool, string la);
```

This function enables or disables the small-x resummation in the evolution and set the logarithmic accuracy of the resummation to "la". The possible options for la" are "LL" and "NLL". The small-x resummation of the evolution relies on an external code called HELL that returns the difference between the fixed-order and the resummed splitting functions as explained above. By default, the small-x resummation is disabled.

```
APFEL::SetAlphaEvolution(string evol);
```

This function sets the solution of the  $\beta$ -function equations for the running couplings to "evol". The variable "evol" can take the following strings:

- "exact": the β-function equations are solved numerically in an exact way using the Runge-Kutta method. The boundary condition is given by the reference values of the coupling at the reference scales.
- "expanded": the  $\beta$ -function equations are solved analytically by expanding the inverse of the  $\beta$ -function when computing the solution of the RG equation. See above for more details. The boundary condition is given by the reference values of the coupling at the reference scales.

• "lambda": the  $\beta$ -function equations are solved in an analytical way in terms of the Landau pole  $\Lambda_{\rm QCD}$ . See above for more details.

It should be noticed that a different choice of "evol" only affects the running of  $\alpha_s$  beyond LO while the running of  $\alpha$ , being computed always at LO, is left unchanged. The default is "evol" = "exact".

## APFEL::SetPDFEvolution(string evolp);

This function sets the solution of the DGLAP equations for the evolution of PDFs to "evolp". The variable "evolp" can take the following strings:

- "exactmu": the DGLAP equation differential in the factorization scale  $\mu_F$  is solved numerically in an exact way using the Runge-Kutta method.
- "exactalpha": the DGLAP equation differential in the coupling  $\alpha_s$  is solved numerically in an exact way using the Runge-Kutta method. This solution is completely equivalent to exactmu.
- "expandalpha": the DGLAP equation differential in the coupling  $\alpha_s$  is solved analytically by expanding the ratio between splitting functions and  $\beta$ -function. See above for more details.
- "truncated": this solution mimics the N-space truncated solution and its implementation requires the numerical derivatives of the expandalpha solution. A detailed explanantion of the implementation of this particular solution is given above.

In all cases the boundary conditions are given by the input initial scale PDFs. The default is "evol" = "exact".

```
APFEL::SetEpsilonTruncation(double eps);
```

If the truncated evolution for PDFs has been chosen by calling the SetPDFEvolution function, the SetEpsilonTruncation function sets the truncation parameter  $\epsilon$  used to compute the numerical dericatives to eps.

## APFEL::SetPDFSet(string name);

This function sets the PDF set to be evolved to "name". The string variable "name" can be the name of an LHAPDF set and in this case it must finish with the string ".LHgrid". This is needed to distinguish the LHAPDF sets from the other possible options available. The other possible options for "name" are:

- "private":
- "apfel":
- "ToyLH":
- "external":

```
• "external1":
```

- "repexternal":
- "leptexternal":
- "kretzer":
- "MELA":
- "pretabulated":
- "pretabulated1":

The default is "name" = "ToyLH".

```
APFEL::SetReplica(int nr);
1
      sets the replica/member of the LHAPDF set to be
      evolved (default "nr" = 0).
   APFEL::SetQLimits(double Qmin, double Qmax);
2
      sets the range where it is possible to perform
      the evolution (default "Qmin" = 0.5 GeV, "Qmax"
3
      = 1000 GeV).
  APFEL::SetNumberOfGrids(int n);
      sets the number of subgrids "n" (default 3)
   APFEL::SetGridParameters(int i, int n, int deg, double x);
1
      sets the parameter of the i-th subgrid. "n" =
      number intevals, "deg" = interpolation order,
3
      "x" lower bound of the grid (the upper bound is
      always 1).
   APFEL::SetExternalGrid(int i, int np, int deg, double *x);
1
      sets the external grid in the position \hbox{\tt "i"} with
2
3
      "np" intervals, interpolation degree "deg". "x"
      \hbox{\tt must be a one-dimentional array with upper bound} \\
      in 1 (there cannot be more than 1 external grid).
  APFEL::SetFastEvolution(bool);
      sets the fast PDF evolution (default true).
  APFEL::GetVersion();
    returns the APFEL version in use.
```

```
APFEL::EnableWelcomeMessage(bool);
      enables the printing of the welcome message with
2
      the APFEL banner and the report of the evolution
3
      parameters (default true).
   APFEL::EnableEvolutionOperator(bool);
      enables the computation of the external evolution
      parameters (default false).
   APFEL::EnableLeptonEvolution(bool);
      enables the evolution of the lepton PDFs when the
2
      fast QUniD is used (default false).
  APFEL::LockGrids(bool);
    locks the subgrids (default false).
   APFEL::CleanUp();
2
      resets all the evolution parameters to the
      default settings.
   {\tt APFEL::SetLHgridParameters(int\ nx,\ int\ nxm,\ double\ xmin,\ double\ xm,\ } \leftarrow
       double xmax, int nq2, double q2min, double q2max);
      sets the parameters of the grid over which PDFs
      will be tabulated in the LHAPDF format.
   APFEL::ListFunctions();
      lists all the functions available in APFEL.
1 Initialization functions:
   APFEL::InitializeAPFEL();
      initializes the APFEL library. If no settings has
3
      been specified, it uses the default ones.
4
   APFEL::EvolveAPFEL(double Q0, double Q);
5
      evolves PDFs on the grid to the scale "Q" [GeV]
      starting from the scale "QO" [GeV].
   APFEL::DeriveAPFEL(double Q);
      computes the logarithmic derivative with respect
9
      of "Q" of PDFs at the scale "Q" [GeV].
1 Output functions:
  APFEL::xPDF(int i, double x) and xgamma(double x);
      return "x" times the i-th and the photon PDF
```

```
in "x" at the final scale "Q" [GeV] defined in
        "EvolveAPFEL".
    APFEL::xPDFall(double x, double *xf);
6
       returns at once "x" times all the PDF in the
7
        array xf[-6:6] computed in "x" at the final scale
8
       "Q" [GeV] defined in "EvolveAPFEL".
9
10
    APFEL::xPDFj(int i, double x) and xgammaj(double x);
       return "x" times the i-th and the photon PDF
11
        in "x" at the final scale "Q" [GeV] defined in
12
        "EvolveAPFEL" interpolated on the joint grid.
13
    APFEL::dxPDF(int i, double x) and dxgamma(double x);
       return "x" times the derivative in ln(Q^2) of
15
        the i-th \underline{and} the photon PDF in \underline{"x"} at the scale
16
       "Q" [GeV] defined in "DeriveAPFEL".
17
    APFEL::NPDF(int i, int N) and Ngamma(int N);
18
       return the N-th moment of the i-th and the
19
       photon PDF the final scale "Q" [GeV] defined in
20
        "EvolveAPFEL".
21
    APFEL::LUMI(int i, int j, double S);
22
23
       returns the partonic luminosity of the i-th and
       j-th partons for the CoM energy S [GeV^2] for the
       final invariant mass Mx = Q [GeV] defined in
26
        "EvolveAPFEL"
    APFEL::AlphaQCD(double Q);
27
       returns the QCD strong coupling alpha_s at the
28
       scale "Q" [GeV].
29
    APFEL::AlphaQED(double Q);
30
       returns the QED coupling alpha at the scale
31
        "Q" [GeV].
32
    APFEL::HeavyQuarkMass(int i,double Q);
33
       returns the mass of the i-th heavy quark
34
        (i = 4,5,6) scale "Q" [GeV] (the masses run only
       when using the MSbar scheme).
36
37
    APFEL::nIntervals();
38
       returns the number of intervals of the joint
39
       grid.
    APFEL::xGrid(int alpha);
40
       returns the value of "x" on the alpha-th node of
41
        the joint grid.
42
    APFEL::GetPerturbativeOrder();
43
       returns the perturbative order set for the
44
45
    APFEL::ExternalEvolutionOperator(string fname, int i, int j, double x, \hookleftarrow
46
        int beta);
        returns the PDF evolution operator.
47
    APFEL::LHAPDFgrid(int Nrep, double Qin, string fname);
48
       produces a PDF interpolation grid in the LHAPDF
49
       format.
50
    APFEL::LHAPDFgridDerivative(int Nrep, string fname);
51
       produces an interpolation grid in the LHAPDF
52
       format for the derived PDFs.
53
```

```
---- Functions of the DIS module ----
2
3 Initialization functions:
```

```
4
    APFEL::InitializeAPFEL_DIS();
        initializes the DIS module. If no settings has
6
       been specified, it uses the default ones.
7
    APFEL::ComputeStructureFunctionsAPFEL(double Q0, double Q);
8
       computes the DIS structure functions on the grid
9
       at the scale \ensuremath{^{\text{\tiny T}} Q}\ensuremath{^{\text{\tiny T}}} [GeV] applying also the PDF
10
       evolution from the initial scale "QO" [GeV].
11
12
13
   Setting functions:
14
    APFEL::SetMassScheme(string ms);
15
16
       sets the mass scheme to be used to compute the
        structure functions ("ms" = "ZM-VFNS", "FFNS",
17
        "FONLL-A", "FONLL-B", "FONLL-C", default "ms" =
18
        "ZM-VFNS").
19
    APFEL::SetPolarizationDIS(double pol);
20
       sets the beam polarization (default "pol" = 0).
21
    APFEL::SetProcessDIS(string pr);
22
23
        sets process ("pr" = "EM", "NC", "CC", default
24
        "pr" = "EM").
25
    APFEL::SetProjectileDIS(string lept);
        sets the projectile ("lept" = "electron",
26
        "positron", "neutrino", "antineutrino", default
27
       "lept" = "electron").
28
    APFEL::SetTargetDIS(string tar);
29
       sets the target ("tar" = "proton", "neutron",
30
        "isoscalar", "iron", default "tar" = "proton")
31
    APFEL::SetZMass(double massz);
32
       sets the value of the mass of the Z boson
33
        (default "massz" = 91.1876 GeV).
34
    APFEL::SetWMass(double massw);
       sets the value of the mass of the {\tt W} boson
36
        (default "massw" = 80.385 GeV).
37
38
    APFEL::SetProtonMass(double massp);
39
       sets the value of the mass of the proton
        (default "massp" = 0.938272046 GeV).
40
    APFEL::SetSin2ThetaW(double sw);
41
       sets the value of sin^2(theta_W)
42
        (default "sw" = 0.23126).
43
    APFEL::SetGFermi(double gf);
44
        sets the value of Fermi constant
45
        (default "gf" = 1.1663787e-5).
46
47
    APFEL::SetCKM(double vud, double vus, double vub,
             double vcd, double vcs, double vcb,
48
             double vtd, double vts, double vtb);
49
       sets the absolute value of the entries of the
50
       CKM matrix
51
        (default: 0.97427d0, 0.22536d0, 0.00355d0,
52
                   0.22522d0, 0.97343d0, 0.04140d0,
53
                   0.00886d0, 0.04050d0, 0.99914d0).
54
    APFEL::SetRenQRatio(double ratio);
55
        sets the ratio muR / Q (default 1)
56
    APFEL::SetFacQRatio(double ratio);
57
        sets the ratio muF / Q (default 1)
58
    APFEL::EnableDynamicalScaleVariations(bool);
```

```
enables or disables the possibility to perform
         fact/ren scale variations point by point without
61
        requiring the ratio \mu_{R,F} / Q to be constant.
62
        Limitations: \mbox{\mbox{\mbox{mu}_F} = \mbox{\mbox{\mbox{\mbox{\mbox{mu}_R}}}} \mbox{\mbox{\mbox{and}}} \mbox{\mbox{\mbox{slower}}} \mbox{\mbox{\mbox{code}}}.
63
     APFEL::EnableTargetMassCorrections(bool);
64
         enables or disables the target mass corrections
65
        to the DIS structure functions due to the finite
66
67
        mass of the proton.
68
     APFEL::EnableDampingFONLL(bool);
69
         enables or disables the damping factor when the
        FONLL structure functions are computed.
70
71
     APFEL::SelectCharge(string selch);
        selects one particular charge in the NC structure
72
        functions ("selch" = "down", "up", "strange",
73
         "charm", "bottom", "top", "all", default
74
         "selch" = "all")
75
     APFEL::SetPropagatorCorrection(double dr);
76
         sets the correction to the Z propagator involved
77
         in the NC DIS structure functions
78
         (default "dr" = 0).
79
     APFEL::SetEWCouplings(double vd, double vu, double ad, double au);
81
         sets the vector and axial couplings of the up-
         and down-type quarks. If they are not set by the
82
        user the standard couplinglings are used.
83
84
    Output functions:
85
86
     APFEL::F2light(double x), F2charm(double x), F2bottom(double x),
87
      F2top(double x), F2total(double x);
88
     APFEL::FLlight(double x), FLcharm(double x), FLbottom(double x),
89
      FLtop(double x), FLtotal(double x);
90
     APFEL::F3light(double x), F3charm(double x), F3bottom(double x),
91
      F3top(double x), F3total(double x);
92
93
        return the F2, FL and xF3 struncture functions in
         "x" at the final scale "Q" [GeV] defined in
94
95
         "ComputeStructureFunctionsAPFEL".
     APFEL::GetZMass();
96
        returns the value of the mass of the Z boson
97
     APFEL::GetWMass():
98
        returns the value of the mass of the W boson
99
     APFEL::GetProtonMass();
100
        returns the value of the mass of the proton
101
     APFEL::GetSin2ThetaW();
102
        returns the value of sin^2(theta_W)
103
104
     APFEL::GetGFermi();
        returns the value of Fermi constant
105
     APFEL::GetCKM(int u, int d);
106
        returns the absolute value of the (u,d) entry
107
        of the CKM matrix
108
     APFEL::GetSIATotalCrossSection(int pto, double Q);
109
        returns the SIA total cross section in natural
110
        units at the perturbative order "pto" and at the
111
         scale "Q" in GeV (only for time-like evolution).
     <code>APFEL::ExternalDISOperator(string SF, int ihq, int i, double x, int</code> \hookleftarrow
         beta);
        returns the DIS operators.
114
```

```
Special functions for the production of FK tables:
116
117
     APFEL::SetFKObservable(string obs);
118
     APFEL::GetFKObservable();
119
     APFEL::FKSimulator(string obs, double x, double q, double y, int i, int\leftarrow
120
          beta):
     APFEL::FKObservables(string obs, double x, double q, double y);
121
     APFEL::ComputeHardCrossSectionsDY(string inputfile, string outputfile);
122
     APFEL::ComputeFKTables(string inputfile, double Q0, int flmap[196]);
123
```

Using the dafualt settings of APFEL this is how the evolution banner would look like:

```
Welcome to
2
                  _/_/_/ _/_/ _/_/
3
4
5
6
7
   ____v2.6.1 A PDF Evolution Library, arXiv:1310.1394
8
        Authors: V. Bertone, S. Carrazza, J. Rojo
10
   Report of the evolution parameters:
11
   QCD evolution
12
   Space-like evolution (PDFs)
13
   Evolution scheme: VFNS at N2L0
   Solution of the DGLAP equation: "exactmu" with maximum 6 active flavours
15
   Solution of the coupling equations: "exact" with maximum 6 active \hookleftarrow
       flavours
   Coupling reference value:
17
   - AlphaQCD( 1.4142 \text{ GeV}) = 0.350000
   Pole heavy quark thresholds:
   - Mc = 1.414 GeV
20
21
   - \text{ Mb} = 4.500 \text{ GeV}
   - Mt = 175.000 GeV
22
   muR / muF = 1.0000
23
24
   Allowed evolution range [ 0.50 : 100000.00 ] GeV
25
   Fast evolution enabled
```

As clear, the most important settings are reported in the banner and we recommand to consult the banner every time that APFEL is run to make sure that the desired setting are actually used.

Here is the complete set of default settings used by APFEL:

```
APFEL::EnableWelcomeMessage(true);
APFEL::SetQLimits(0.5,100000);
APFEL::SetPerturbativeOrder(2);
APFEL::SetVFNS
APFEL::SetTheory("QCD");
APFEL::SetFastEvolution(true);
APFEL::SetTimeLikeEvolution(false);
APFEL::SetSmallxResummation(false,"NLL");
```

```
APFEL::SetAlphaQCDRef(0.35, sqrt(2););
9
    APFEL::SetAlphaQEDRef (7.496252e-3,1.777);
10
    APFEL::SetLambdaQCDRef(0.220,5);
11
    APFEL::SetEpsilonTruncation(1e-5);
12
    APFEL::SetAlphaEvolution("exact");
13
    APFEL::SetPDFEvolution("exactmu");
14
    APFEL::SetRenFacRatio(1);
15
    APFEL::SetPoleMasses(sqrt(2), 4.5, 175);
16
17
    APFEL::SetMassScaleReference(sqrt(2),4.5,175);
18
    APFEL::SetTauMass(1.777);
    APFEL::EnableMassRunning(true);
19
    APFEL::SetMaxFlavourPDFs(6);
20
21
    APFEL::SetMaxFlavourAlpha(6);
    APFEL::SetPDFset("ToyLH");
22
    APFEL::SetReplica(0);
23
    APFEL::EnableEvolutionOperator(false);
24
    APFEL::EnableLeptonEvolution(false);
25
    APFEL::LockGrids(false);
26
    APFEL::SetLHgridParameters(100,50,1e-9,1e-1,1,50,1,1e10);
27
    APFEL::SetNumberOfGrids(3);
28
    APFEL::SetGridParameters(1,80,3,1e-5);
30
    APFEL::SetGridParameters(2,50,5,1e-1)
    APFEL::SetGridParameters(3,40,5,8e-1);
```

As an illustration, if the user wants to perform the QCD evolution at NLO instead of the default NNLO, she/he needs to add to the code above, before the initialization routine InitializeAPFEL, a call to the corresponding function, that is:

```
APFEL::SetPerturbativeOrder(1);
```

or if the user wants to use as a boundary condition for the PDF evolution a particular set available through the LHAPDF interface, say NNPDF23\_nlo\_as\_0118\_qed.LHgrid, she/he needs to call before the initialization the following function:

```
APFEL::SetPDFSet("NNPDF23_nlo_as_0118_qed.LHgrid");
```

By default, APFEL will use the central replica of the selected PDF set. Varying any other setting is similar, various example programs have been collected in the examples folder in the APFEL source folder.

When modifying the default settings, particular care must be taken with the number of interpolation grids, the number of points in each grid and the order of the interpolation. The default settings in APFEL use three grids whose ranges and number of points have been tuned to give accurate and fast results over a wide range of x. If the default parameters are modified, the user should check that the accuracy is still good enough, by comparing for instance with another run of APFEL with the default interpolation parameters.

The folder examples in the APFEL source directory contains several examples that further illustrate the functionalities of the code, and that can be used by the user as a starting point towards a program that suits her/his particular physics needs. All these examples are available in the three possible interfaces to APFEL: FORTRAN 77, C/C++ and Python.

3 The DIS module