

# **Morphological epenthesis in Serbo-Croatian noun inflection**

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# Introduction

- Class I:

zavod	zavod-a
institute.NOM.SG.M	institute.GEN.SG.M
sel-o	sel-a
village.NOM.SG.N	village.GEN.SG.N
tele	telet-a
calf.NOM.SG.N	calf.GEN.SG.N
- Class II:

žen-a	žen-e
woman.NOM.SG.F	woman.GEN.SG.F
- Class III:

rečf	rečf-i
word.NOM.SG.F	word.GEN.SG.F

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morphologically  
conditioned consonant  
insertion  
—  
repairing vowel-final  
stems

# Introduction

- part of a wider algorithmic process of noun inflection
  - Boolean Monadic Recursive Schemes (BMRSs)
  - analyzed as logical transductions on strings
    - stem + [Case Num]  $\rightarrow$  inflected word  $\sim$  realization rules
  - hierarchical ordering of more specific and less specific blocking and licensing structures
    - $\sim$  realization rules intrinsically ordered by Pāṇini's principle (cf. Stump 2001)
- possibility to compose BMRSs into a complete inflectional system
  - algorithm of inflectional class assignment

# Morphologically conditioned consonant insertion

- SC stems are normally C-final; those that are not are repaired via consonant insertion  
→ if another suffix follows immediately

otherwise the word is vowel-final (bare stem) and considered well-formed (as the nom.sg. suffix is *-o/-e*)

	tele	‘calf.NOM.SG’
	telet-a	‘calf.GEN.SG.’
/tele + ji/	[teletɕi]	‘calf-like(ADJ.)’

# Morphologically conditioned consonant insertion

- *t* is not the general epenthetic consonant in this language

/zaova/            [zaova]            ‘sister-in-law’

/violina/            [vijolina]            ‘violin’

- *t* epenthesized only to repair vowel-final stems, does not depend on vowel hiatus

/tele + ji/        [teletɕi] ‘calf-like’ vs.        /koz + ji/        [kozji] ‘goat-like’

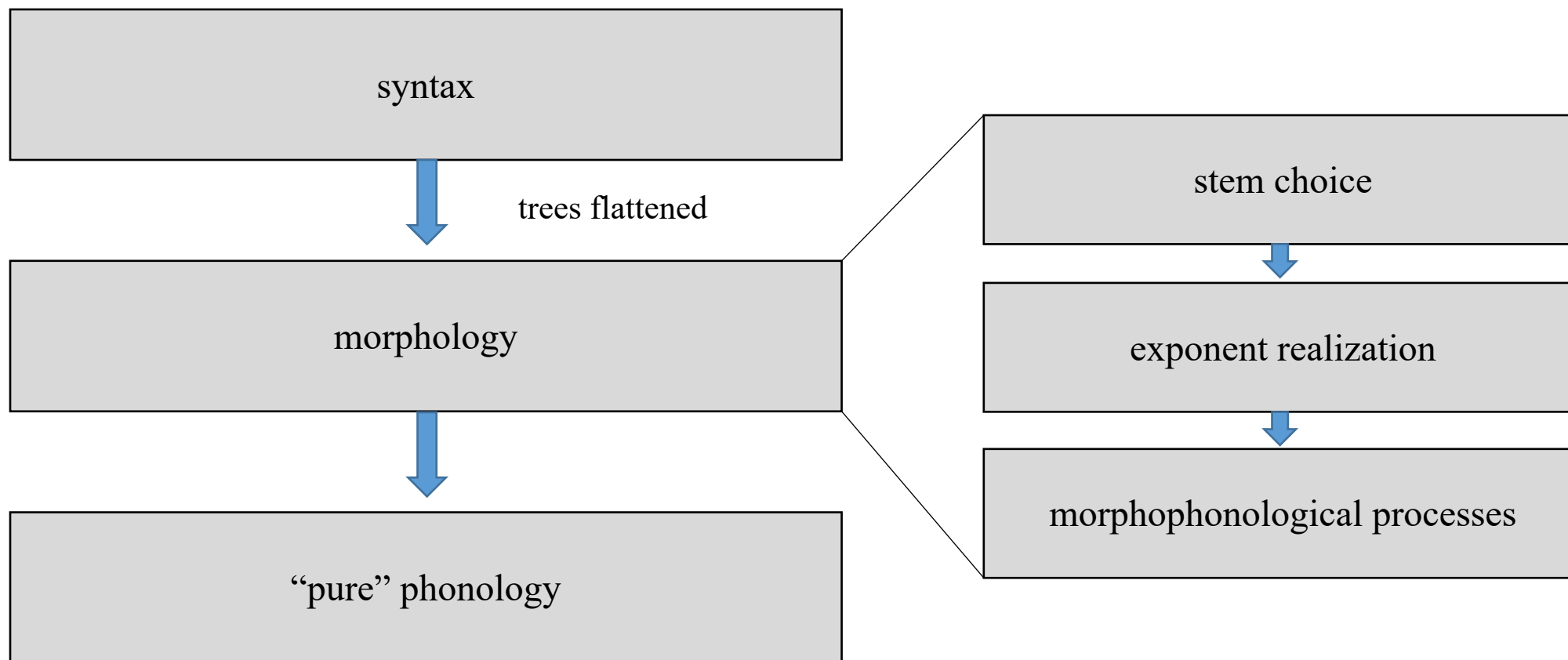
/sirtɕe + ni/    [sirtɕetni] ‘acetic’ vs.        /plod + ni/    [plodni] ‘fertile’

# The nature of morphological processes

- morphological processes are regular (Karttunen et al. 1992), most often subregular (Chandlee 2017)
- DM is a tree-based theory, but can be formalized over strings (Ermolaeva & Edmiston 2018)
  - yield function flattens trees, retaining necessary boundary symbols
- In terms of computational power, W&P morphology is equivalent to a collection of regular relations (Karttunen 2003)



# Proposed model



# Analysis

- *Boolean Monadic Recursive Schemes* (BMRS)
  - incorporates the observation that phonology is regular (Johnson 1972; Kaplan & Kay 1994; Heinz 2018)
  - morphology, too, is regular (Karttunen et al. 1992), most often subregular (Chandlee 2017)
  - unlike FSTs, captures linguistically significant generalizations – we can use representations that are common in linguistics
    - phonological, morphosyntactic features
    - Pāṇini's Principle (= Elsewhere condition) has no obvious finite-state implementation (Karttunen 2003), whereas it is directly captured with BMRS's 'if...then...else' syntax

# Analysis

- primitives:
  - *boolean values*  $\top$  and  $\perp$
  - *monadic predicates*  $P(t)$  – take a *single* argument  $t$ , and return  $\top$  or  $\perp$

$$\mathbb{V} = \{a, e, i, o, u\}$$

$$\mathbb{C} = \{b, \mathfrak{b}, \mathfrak{t}, \mathfrak{d}, \mathfrak{g}, \mathfrak{z}, f, g, h, j, k, l, \wedge, m, n, \mathfrak{n}, p, r, s, \int, t, v, z, 3\}$$

$$\mathbb{M} = \{[nom], [gen], [dat], [acc], [voc], [ins], [loc], [sg], [pl]\}$$

$$\Sigma = \mathbb{V} \cup \mathbb{C} \cup \mathbb{M} \qquad \Sigma_{\times} = \Sigma \cup \{\times, \times, +\}$$

# Analysis

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$$\mathbb{C} = \{b, t, f, d, g, h, j, k, l, m, n, p, r, s, v, z, 3\}$$

$$\mathbb{M} = \{[nom], [gen], [dat], [acc], [voc], [ins], [loc], [sg], [pl]\}$$

$$\Sigma = \mathbb{V} \cup \mathbb{C} \cup \mathbb{M} \quad \Sigma_{\bowtie} = \Sigma \cup \{\bowtie, \ltimes, +\}$$

$$\mathcal{I} = \{a(t), \dots, 3(t), [nom](t), \dots, [pl](t), \bowtie(t), \ltimes(t), +(t)\}$$

$$\mathcal{O} = \{a_o(t), \dots, 3_o(t), [nom]_o(t), \dots, [pl]_o(t), \bowtie_o(t), \ltimes_o(t), +_o(t)\}$$

# Analysis

- no right word boundary symbol  $\rightarrow$  stems are (contiguous) strings of characters occupying indices belonging to a *countably infinite* set of indices

$$\mathbf{S} = \langle D; \sigma_1, \sigma_2, \dots, p, s \rangle$$

$$D = \{1, 2, \dots\}$$

- the right word boundary is assigned at the end of the word only after the inflectional exponents are realized (look out for  $\bowtie(\mathbf{x})$  in the following slides!)
- (I do this to avoid using copy sets, which might not be a great idea.)

# Analysis

- In BMRS, we can refer to both input and output predicates, and define new ones

<u>input</u>							
1	2	3	4	5	6	7	...
×	t	e	l	e	+	[dat sg]	...

<u>output</u>							
t e l e t u							

- Examples of defining new input predicates: case/number feature combinations, syncretism, defining the class of FCs

# Analysis

- necessary combinations of case and number features available for neuter nouns:

$[\text{nom/acc/voc sg}](x) = \text{if } [\text{nom/acc/voc}](x) \text{ then } [\text{sg}](x) \text{ else } \perp$   
 $[\text{dat/loc sg}](x) = \text{if } [\text{dat/loc}](x) \text{ then } [\text{sg}](x) \text{ else } \perp$   
 $[\text{ins sg}](x) = \text{if } [\text{ins}](x) \text{ then } [\text{sg}](x) \text{ else } \perp$   
 $[\text{nom/acc/voc pl}](x) = \text{if } [\text{nom/acc/voc}](x) \text{ then } [\text{pl}](x) \text{ else } \perp$   
 $[\text{gen pl}](x) = \text{if } [\text{gen}](x) \text{ then } [\text{pl}](x) \text{ else } \perp$   
 $[\text{dat/loc pl}](x) = \text{if } [\text{dat/loc}](x) \text{ then } [\text{pl}](x) \text{ else } \perp$   
 $[\text{ins pl}](x) = \text{if } [\text{ins}](x) \text{ then } [\text{pl}](x) \text{ else } \perp$

(one would expect  $14 - 7 \text{ cases} \times 2 \text{ numbers}$  – but we do not have 14 distinct phonological forms of overt suffixes)

# Analysis

- (non-directional) syncretism

$[\text{dat/loc}](x) = \text{if } [\text{dat}](x) \text{ then } \tau \text{ else } [\text{loc}](x)$

$[\text{nom/acc/voc}](x) = \text{if } [\text{nom}](x) \text{ then } \tau \text{ else}$   
 $\quad \text{if } [\text{acc}](x) \text{ then } \tau \text{ else } [\text{voc}]$

$[\text{gen/ nom/acc/voc pl}](x) = \text{if } [\text{gen}](x) \text{ then } \tau$   
 $\quad \text{else } [\text{nom/acc/voc pl}](x)$

$[\text{dat/loc pl/ins pl}](x) = \text{if } [\text{dat/loc pl}](x) \text{ then } \tau$   
 $\quad \text{else } [\text{ins pl}](x)$



# Analysis

- effect of fronting consonants (i.e. fronting of  $\text{ɔ}$  to  $\text{e}$  after stem-final FCs)

(FC = C[cor, -ant] +  $\text{ʊ}$ )

$[\text{FC}](x) =$

- if  $\text{ʊ}(x)$  then  $\text{ʊ}$  else
- if  $\text{ɪ}(x)$  then  $\text{ʊ}$  else
- if  $\text{ʌ}(x)$  then  $\text{ʊ}$  else
- if  $\text{ɔ}(x)$  then  $\text{ʊ}$  else
- if  $\text{ɔ̃}(x)$  then  $\text{ʊ}$  else
- if  $\text{ɔ̃}(x)$  then  $\text{ʊ}$  else
- if  $\text{ɔ̃}(x)$  then  $\text{ʊ}$  else
- if  $\text{ɔ̃}(x)$  then  $\text{ʊ}$  else
- if  $\text{ɔ̃}(x)$  then  $\text{ʊ}$  else
- if  $\text{ɔ̃}(x)$  then  $\text{ʊ}$  else  $\text{ɔ̃}(x)$

# Analysis

- $t$ -insertion

$\text{outseg}(x) =$  if  $a_o(x)$  then  $\top$  else  
          if  $b_o(x)$  then  $\top$  else  
          if  $c_o(x)$  then  $\top$  else  
          (...)  
          if  $z_o(x)$  then  $\top$  else  $z_o(x)$

$t_o(x) =$  if  $+(x)$  then  
          if  $e(p(x))$  then  $\text{outseg}(s(x))$  else  $\perp$   
          else  $t(x)$

# Analysis

- Output predicates: ( $\sim$  realization rules)

$u_o(x) = \text{if } [\text{dat/loc sg}](x) \text{ then } \top \text{ else } u(x)$   
 $a_o(x) = \text{if } [\text{gen/ nom/acc/voc pl}](x) \text{ then } \top \text{ else}$   
           $\text{if } [\text{gen pl}](p(x)) \text{ then } \top \text{ else}$   
           $\text{if } [\text{ins pl}](p(p(x))) \text{ then } \top \text{ else } a(x)$   
 $o_o(x) = \text{if } [\text{nom/acc/voc sg}](x) \text{ then } \top \text{ else}$   
           $\text{if } [\text{ins sg}](x) \text{ then } \top \text{ else } o(x)$   
 $m_o(x) = \text{if } [\text{ins}](p(x)) \text{ then } \top \text{ else } m(x)$   
 $i_o(x) = \text{if } [\text{ins pl}](x) \text{ then } \top \text{ else } i(x)$   
 $e_o(x) = \text{if } o_o(x) \text{ then}$   
           $\text{if } +(p(x)) \text{ then } [\text{pal}](p(p(x))) \text{ else } \perp$   
           $\text{else } e(x)$

$l_o(x) = l(x)$

$b_o(x) = b(x)$

(etc., for  $\{\text{t}, \text{t}^{\flat}, \text{t}^{\flat}, \text{d}, \text{d}^{\flat}, \text{d}^{\flat}, \text{f}, \text{g}, \text{h}, \text{j}, \text{k}, \text{l}, \text{K}, \text{n}, \text{n}, \text{p}, \text{r}, \text{s}, \text{f}, \text{v}, \text{z}, \text{z}\}$ )

# Analysis

<u>input</u>								
1	2	3	4	5	6	7	8	9
×	t	e	l	e	+	[ins sg]		...
<u>output</u>								
	t	e	l	e	t	o	m	

- Output predicates:

$u_o(x) = \text{if } [\text{dat/loc sg}](x) \text{ then } \top \text{ else } u(x)$

$a_o(x) = \text{if } [\text{gen/ nom/acc/voc pl}](x) \text{ then } \top \text{ else}$   
            $\text{if } [\text{gen pl}](p(x)) \text{ then } \top \text{ else}$   
            $\text{if } [\text{ins pl}](p(p(x))) \text{ then } \top \text{ else } a(x)$

$o_o(x) = \text{if } [\text{nom/acc/voc sg}](x) \text{ then } \top \text{ else}$   
            $\text{if } [\text{ins sg}](x) \text{ then } \top \text{ else } o(x)$

$m_o(x) = \text{if } [\text{ins}](p(x)) \text{ then } \top \text{ else } m(x)$

$i_o(x) = \text{if } [\text{ins pl}](x) \text{ then } \top \text{ else } i(x)$

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$l_o(x) = l(x)$

$b_o(x) = b(x)$

(etc., for { $\text{ts, tf, tg, d, dz, dz, f, g, h, j, k, l, \text{K}, n, \text{n}, p, r, s, \text{f}, v, z, 3\}$ )

# Analysis

$\bowtie(x) =$  if [nom sg]( $x$ ) then  $e(p(x))$  else  
if [nom/acc/voc sg]( $p(x)$ ) then  $\top$  else  
if [dat/loc sg]( $p(x)$ ) then  $\top$  else  
if [gen/ nom/acc/voc pl]( $x$ ) then  $\top$  else  
if [ins sg]( $p(p(x))$ ) then  $\top$  else  
if [dat/loc pl/ins pl]( $p(p(p(x)))$ ) then  $\top$  else  $\perp$

$\text{out}(x) =$  if  $+(x)$  then  $t_o(x)$  else  
if  $\bowtie(x)$  then  $\perp$  else  
if  $\bowtie(x)$  then  $\perp$  else  $\top$

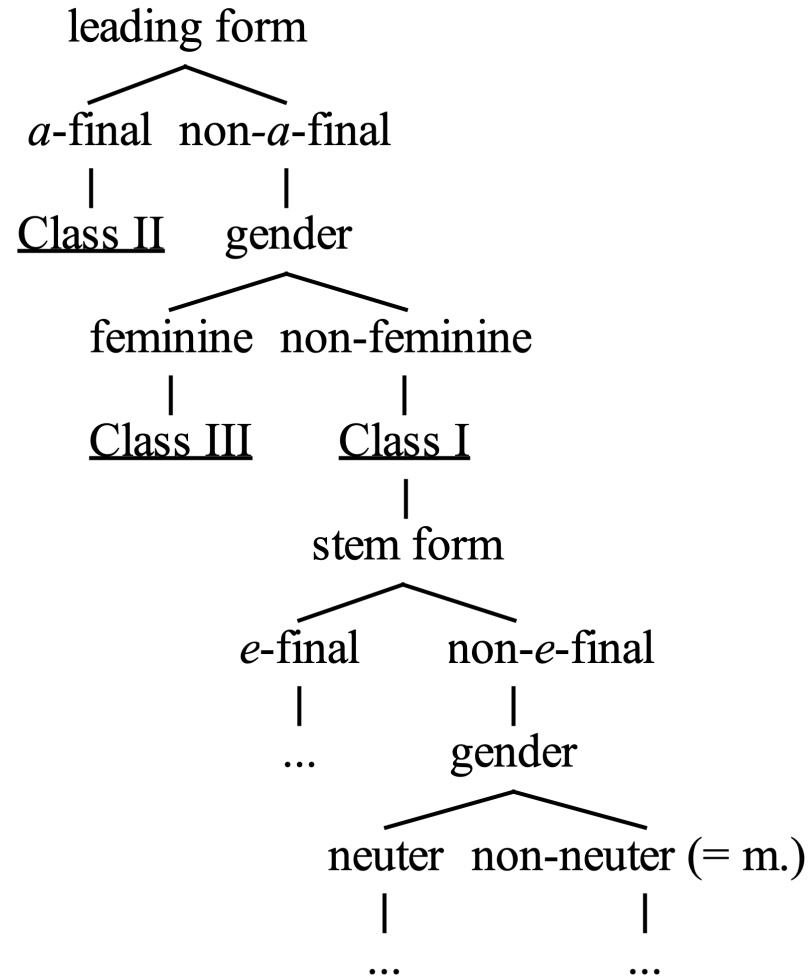
# Analysis

- no copy sets = no epenthesis/insertion of material longer than 1 symbol ☹
- is there a smart way to do this (+ more → non-concatenative morphology) without copy sets? The non-computationally minded often find them counterintuitive

# Class membership assignment in SC

- Class membership assignment in SC can be modeled as a predictable process if we take into account a *leading form/base* (Wurzel 1990, McCarthy 2005, Albright 2008)
- This I argue to be the nominative singular: it is the most frequent form (subject case), and it ranks highest in the Case Hierarchy (Blake 2001).
- loanwords do not (necessarily) have an oblique form – they are incorporated into the declension system on the basis of their input form (which is borrowed as nominative singular)
- so, lexical entry = {stem, leading form, morphosyntactic info}, but the algorithm should work with a deficient lexical entry too

# Class membership assignment in SC





# Conclusions

- Inserting *t* repairs aberrant, V-final stems (whenever an overt suffix is attached)
- This happens regardless of whether that suffix is vowel- or consonant-initial
- A means to avoid stipulating listed stems – assuming unpredictable stem allomorphs would basically reduce the phenomenon to an accident
- Assuming morphological epenthesis enables us to express the generalizations explicitly and overtly

# Conclusions

- BMRSs can directly capture morphological and phonological generalizations, retaining the computationally restrictive nature of such processes
- Intuitive, easily implementable, extendable to a wider range of phenomena
- Future work: noun class membership assignment base on ‘if...then...else’ syntax; class membership does not have to be listed information

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