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1 # Import modules
2
3 import matplotlib.pyplot as plt
4 from numpy import inf, exp, sqrt, linspace, array, pi
5 import numpy as np
6 from scipy.integrate import quad
7
8
9 def N_eq(x):
10     '''
11     Calculates the equilibrium co-moving number density for the WIMP particle
12
13     Parameters
14     -----
15     x - Defined to be  $x=m_x/T$ 
16
17     Returns
18     -----
19     N_eq : float/array : Equilibrium co-moving number density
20
21     '''
22     A = 45 / (4 * pi ** 4)
23     g_x = 4
24     g_s = 106.75
25
26     const = A * g_x / g_s
27
28     if isinstance(x, np.float64) or type(x) == float:
29         # If x is a float and N_eq is wished to be determined at a point
30         return const * quad(lambda a: a ** 2 / (exp(sqrt(a ** 2 + x ** 2)) - 1), 0
, inf, epsabs=inf)[0]
31     else:
32         # If x is an array and N_eq is wished to be determined at multiple points
33         return array(
34             [const * quad(lambda a: a ** 2 / (exp(sqrt(a ** 2 + x_ ** 2)) - 1), 0
, inf, epsabs=inf)[0] for x_
35                 in
36                 x])
37
38
39 # Set-up x space
40 x_min = 0.1
41 x_max = 50
42 x = linspace(x_min, x_max, 200)
43
44 # Plot Solution
45 plt.loglog(x, N_eq(x), 'k--', linewidth=0.5, label=r'$N_{eq}(x)$')
46 plt.title(r'$N_{x^{eq}}(x)$')
47 plt.ylabel(r'$N_{x^{eq}}$')
48 plt.xlabel(r'$x$')
49 plt.xlim(x_min, x_max)
50 plt.ylim(1e-10, 1e-1)
51 plt.savefig('N_eq_plot', dpi=300)
52 plt.show()
53
54 # Print Critical Values
55 x_vals = [0.1, 1., 10.]

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56 for x in x_vals:
57     print("N_eq({}) = {}".format(x, "{:.3e}".format(N_eq(x))))
58
```