

# EC441: Lab 7

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## 7.0 Prelab

<b>Question 5.3</b>	Step	N	t	u	v	w	y	z
	0	x	-	-	3,x	6,x	6,x	8,x
	1	x,w	-	9,w	3,x	6,x	6,x	8,x
	2	x,w,u	11,u	9,w	3,x	6,x	6,x	8,x
	3	x,w,u,t	7,v	9,w	3,x	6,x	6,x	8,x
	4	x,w,u,t,v	7,v	9,w	3,x	6,x	6,x	8,x
	5	x,w,u,t,v,y	7,v	9,w	3,x	6,x	6,x	8,x
	6	x,w,u,t,x,y,z	7,v	9,w	3,x	6,x	6,x	8,x

<b>Question 5.5</b>	Dest	Cost	Next Hop
	u	6	x
	v	5	x
	x	2	x
	y	2	x

### Question 5.7

Part a)	Dest	Cost	Next Hop
	u	7	w
	w	2	w
	y	2	w

Part b) The link between x & w goes down

Part c) The cost of the link between x & y goes to 6.

### Question 6.8

Part a) Utility,  $U = Np(1 - p)^{N-1}$ . To find the optimal  $p$ , find the derivative of  $U$  with respect to  $p$  and solve for  $p$  when it is equal to 0. So,

$$\frac{dU}{dp} = N(1 - p)^{N-1} - N(N - 1)p(1 - p)^{N-2}$$

Then, when  $\frac{dU}{dp} = 0$

$$\begin{aligned} N(1 - p)^{N-1} &= N(N - 1)p(1 - p)^{N-2} \\ 1 - p &= (N - 1)p \\ 1 &= Np \\ p &= 1/N \end{aligned}$$

Thus, the optimal value for  $p$  is  $\frac{1}{N}$ .

Part b)

$$U(1/N) = (1 - \frac{1}{N})^{N-1}$$

Now, taking the limit as  $N \rightarrow \infty$ ,

$$\lim_{N \rightarrow \infty} (1 - \frac{1}{N})^{N-1} = \frac{1}{e}$$

Using the fact that  $\lim_{N \rightarrow \infty} (1 - \frac{1}{N})^N = 1/e$ .

### Question 6.10

Part a) Let  $P[S]$  represent the probability that a given time slot is successful. Then,

$$\begin{aligned} P[S] &= P[\text{only A or B is successful}] \\ &= (1 - p_A)p_A + (1 - p_A)p_A \\ &= p_A - p_B p_A + p_B - p_A p_B \\ &= p_A + p_B - 2p_A p_B. \end{aligned}$$

Part b) Let  $P[A]$  be the probability that for a given time slot, A is successfully sent. Thus,  $P[A] = (1 - p_B)p_A$  and  $P[B] = (1 - p_A)p_B$ . Then we can show that the ratio of  $P[A]$  to  $P[B]$  is less than 2.

$$\begin{aligned} \frac{P[A]}{P[B]} &= \frac{(1 - p_B)p_A}{(1 - p_A)p_B}, \text{ let } p_A = 2p_B \\ &= \frac{(1 - p_B)2p_B}{(1 - 2p_B)p_B} \\ &= 2 \frac{1 - p_B}{1 - 2p_B}. \end{aligned}$$

$2 \frac{1 - p_B}{1 - 2p_B} < 2$  because  $\frac{1 - p_B}{1 - 2p_B}$  is less than one.

If  $\frac{P[A]}{P[B]} = 2$ , then,

$$\begin{aligned}
 2 &= \frac{(1 - p_B)p_A}{(1 - p_A)p_B} \\
 2(1 - p_A)p_B &= p_A - p_A p_B \\
 2p_B &= p_A + p_A p_B \\
 0 &= p_A + p_A p_B - 2p_B \\
 0 &= 1 + p_B - 2\frac{p_A}{p_B} \\
 \frac{p_A}{p_B} &= \frac{1 + p_B}{2}
 \end{aligned}$$

Thus  $p_A$  and  $p_B$  should be chosen so that their ratio is  $\frac{1+p_B}{2}$ .

### Additional Question 1

Part a) If the link from B to C fails, B will send an update to A. A will get an update from B and see that it is an update from the next hop, and send an update back to B, with a cost of 2. B will get this update and send an update to A about its increase cost. This update will cause A to update and repeat the process.

Part b) Probability is 1.

Part c) Probability is 1.

**Additional Question 2** At  $t_1$  C will send out a triggered update to A and B notifying them about the topology change, both with sequence numbers 1. A will then send a packet to B and vice versa, both packets having sequence numbers 1. Also at  $t_1$ , D will send an update to E, telling about the link failure, with sequence number of 1. When the link is restored at  $t_2$ , C and D will send out lsp's to their neighbors, all with a sequence number of 1, and the same sequence of events will occur as before.

## 7.1 Static Routing

**Question 1** The route does not change because static routing tables do not change.

**Question 2** The route does not change because static routing tables do not change.

## 7.2 Distance Vector Routing

**Question 3** Row 0 in the table has the following elements: 0, 1, 1, 1, 6, 6, 6. This lists the next node to hop to in order to reach node j, where j is the destination node.

**Question 4** At  $t = 1.0s$ , the link between Nodes 4 & 5 fails and at  $t = 3.0s$ , it is restored. The failure of this link causes both Node 4 & 5 to send updates about their neighbors and costs to all other nodes. Once the update reaches Node 0, it stops sending packets to Node 6 and instead delivers packets to Node 4 by way of Nodes 1,2, & 3.

**Question 5** The percent overhead is 24.18%.

**Question 6** It takes about 0.05 seconds for routing tables to converge. 18 routing control packets are generated. The following table shows the global routing table after the link between Node 4 & 5 goes down. Element  $ij$  refers to source node  $i$  and destination node  $j$ , where each element as the format next hop, distance to destination.

	0	1	2	3	4	5	6
0	-	1,1	1,2	1,3	1,4	6,2	6,1
1	0,1	-	2,1	2,2	2,3	0,2	0,3
2	1,2	1,1	-	3,1	3,4	1,3	1,4
3	2,3	2,2	2,1	-	4,1	2,5	2,4
4	3,4	3,3	3,2	3,1	-	3,6	3,5
5	6,2	6,3	6,4	6,5	6,6	-	6,1
6	0,1	0,2	0,2	0,3	0,4	5,1	-

### 7.3 Link State Routing

**Question 7** Within in the first 0.5 seconds, nodes are sending updates about their neighbor so that each node gains information about the topology of the network. At  $t = 1.0s$ , the link between Nodes 4 and 5 fails and at  $t = 3.0s$ , it recovers. The route changes because the failure of the link forces Node 4 & 5 to update their tables and send out an update to all other nodes.

**Question 8** The percent overhead is 36.518%

**Question 9** It takes 0.06 seconds for the routing tables to converge. 24 routing control packets are generated. Link State Routing takes time to initialize and longer time to recover from link failure & generates more packets.