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CSCI 3155

1.

2.

a.

2a. $A ::= A \& A \mid \vee$

$V ::= a \mid b$

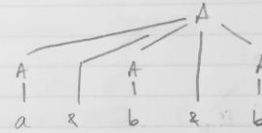
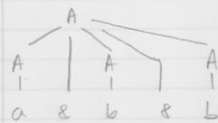
$A \in \text{Aobjects}$

$A \in \text{Aobjects}$

$\vee \in \text{Aobjects}$

$n \in \text{Aobjects}$
 $n \& n \in \text{Aobjects}$

2b



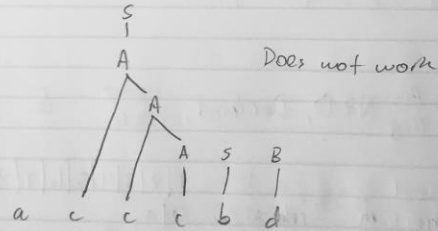
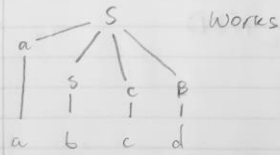
2c $S ::= A \mid B \mid C$

$A ::= aA \mid a$

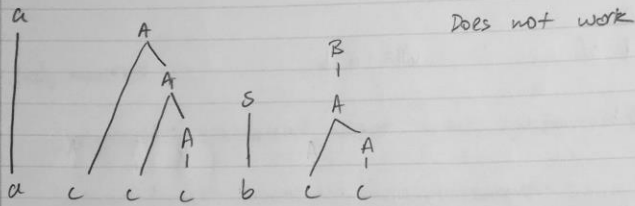
$B ::= bB \mid b$

$C ::= cC \mid c$

2e

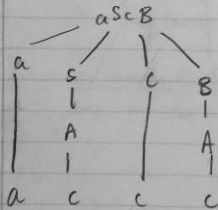


b.



$a \ A \ B$
 $| \ | \ |$
 $a \ c \ d$

Does not work



- c. $L(S)$ is the set of strings that have any number of a's, any number of b's, any number of c's, or nothing.

$$L(S) = \{ "", "a^n", "b^n", "c^n" : n \text{ in the set of Natural Numbers} \}$$

d.

i. $S \Rightarrow AaBb \text{ (baa)}$

$$S \Rightarrow baBb$$

$$S \Rightarrow baab$$

ii. $S \Rightarrow AaBb \text{ (bbbab)}$

$$S \Rightarrow AbaBb$$

$$S \Rightarrow AbbaBb$$

$$S \Rightarrow bbbaB \Rightarrow \text{cannot go further}$$

iii. $S \Rightarrow AaBb \text{ (bbaaaaa)}$

$$S \Rightarrow AbaBb$$

$$S \Rightarrow bbaBb$$

$$S \Rightarrow bbaaB \Rightarrow \text{cannot go further}$$

iv. $S \Rightarrow AaBb \text{ (bbaab)}$

$$S \Rightarrow AbaBb$$

$$S \Rightarrow bbaBb$$

$$S \Rightarrow bbaab$$

3.

a.

- i. The first grammar generates an operand, or recursively, an operator operand. This means the expression will always begin with an operand, and can have an infinite number of operator operand sequences, ending with an operand.

The second grammar starts with an operand followed by up to an infinite number of operator operand sequences, or an epsilon (nothing).

- ii. These grammars generate the same expression because they both begin with an operand, then a variable number of operator operand sequences, and end with an operand.

- b. Using $10 - 2 \ll 1$ as an example:

$10 - 2 \ll 1$	\Rightarrow		\Rightarrow	16
$(10 - 2) \ll 1$	\Rightarrow	$8 \ll 1$	\Rightarrow	16
$10 - (2 \ll 1)$	\Rightarrow	$10 - 4$	\Rightarrow	6

Without parenthesis to force precedence, the scala interpreter evaluated the expression with “-” having a higher precedence than “<<”.

- c. $n ::= 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$
- $N ::= N \mid nN$
- $s ::= \epsilon \mid -N$
- $E ::= Esn \mid EsNn$
- $z ::= 0 \mid 0z$
- $fp ::= z.z \mid sN.Nz \mid sz.NzE \mid sN.NzE$