1 Lecture 1: January 6, 2023

An alternative formulation of the triangle inequality:

$$||x - y|| \ge ||x|| - ||y||$$

2 Lecture 2: January 10, 2023

In 1D, the derivative of a function f at $x_0 \in \mathbb{R}$ is defined as $f'(x_0) = \lim_{x \to x_0} \frac{f(x) - f(x_0)}{x - x_0}$ If this limit exists, we say f is **differentiable** at x_0 .

$$f'(x_0) = \lim_{x \to x_0} \frac{f(x) - f(x_0)}{x - x_0}$$

To prepare our transition into multiple dimensions, we can rewrite the above equa-

$$\lim_{x \to x_0} \frac{f(x) - f(x_0)}{x - x_0} - f'(x_0) = 0$$

$$\lim_{x \to x_0} \frac{f(x) - f(x_0) - f'(x_0)(x - x_0)}{x - x_0} = 0$$

This is the same as questioning the existence of an
$$L = f'(x_0)$$
 that satisfies:
$$\lim_{x \to x_0} \frac{f(x) - f(x_0) - L(x - x_0)}{x - x_0} = 0$$