NB: The graded, first version of the report must be returned if you hand in a second time!

H2a: Binary Alloy

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Task №	Points	Avail. points
Σ		

Introduction

....

Task 1: mean field theory

Fits: we obtained $\alpha \approx 0.494$

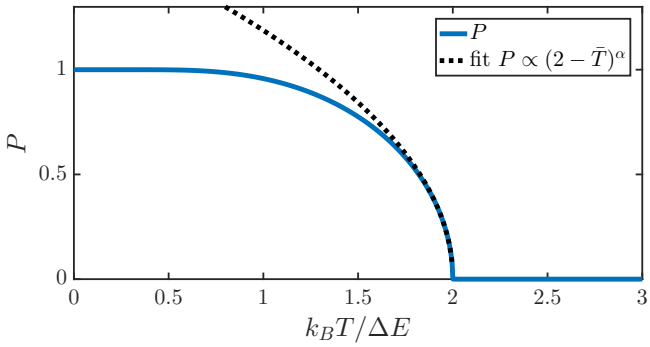

Figure 1: .....

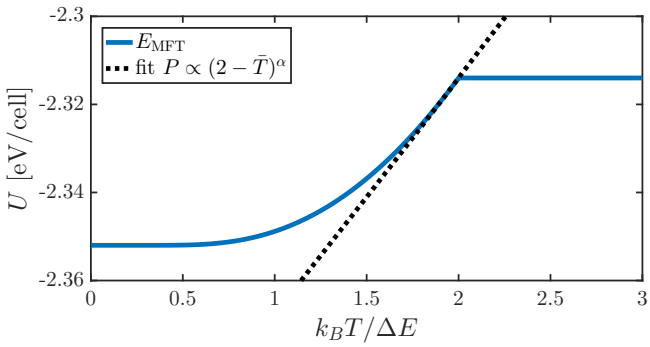

Figure 2: ......

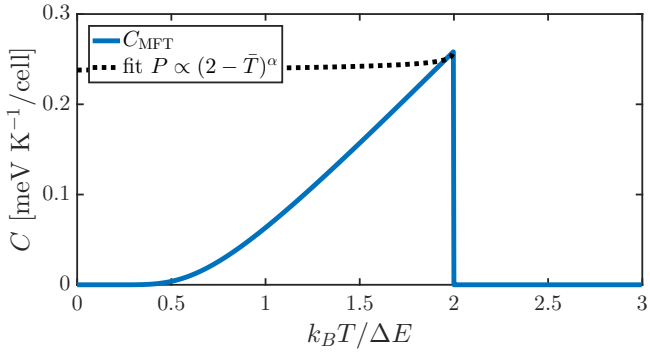

Figure 3: ......

Task 2: Ising model

$$E_{\mathrm{CuZn}} = -294\,\mathrm{meV} \tag{1}$$
$$E_{\mathrm{CuCu}} = -436\,\mathrm{meV} \tag{2}$$
$$E_{\mathrm{ZnZn}} = -133\,\mathrm{meV} \tag{3}$$
$$\tag{4}$$

Figure 4 shows the equilibration at three different temperatures. We note that the energy per bond is in the range $E_{\mathrm{CuZn}} \leq E \leq (E_{\mathrm{CuCu}} + E_{\mathrm{ZnZn}})/2 = 284.5\,\mathrm{meV}$, which it should be.

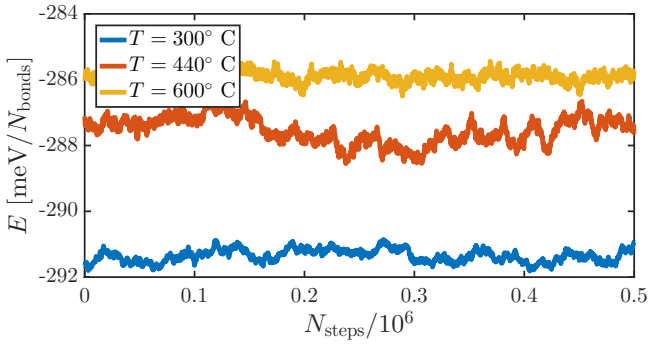

Figure 4: ...

Concluding discussion

...

A Source Code

A.1 Main program task 2: `main_T2.c`

```c
/*
  H2a, Task 2
*/
#include <stdio.h>
#include <math.h>
#include <stdlib.h>

#include "funcs.h"

#define Nc 10 //number of cells
#define N_neigh 8
#define degC_to_K 273.15
#define kB 8.61733e-5

/* Main program */
int main()
{
  int N_Cu = Nc*Nc*Nc;
  int N_atoms = 2*N_Cu;
  int N_bonds = 8*N_Cu;
  double Etot, E_Var, r, P; // Macro parameters
  gsl_rng *q = init_random(); // initialize random number generator

  /* done for all saved steps: */
  int N_timesteps = 1e7;
  int N_eq = 1e6;
  int N_eq_short = 5e5;
  double *E_equilibration = malloc(sizeof(double[N_eq]));
  double *P_equilibration = malloc(sizeof(double[N_eq]));
  double *E_production = malloc(sizeof(double[N_timesteps]));

  /* statistical inefficiency */
  int N_k = 500;
  int N_skip = 1000; // k_Max = N_k * N_skip;
  double *phi = malloc(sizeof(double[N_k]));
  double *var_F = malloc(sizeof(double[N_k]));

  /* set Temperature steps */
  double dT_small = 2;
  double dT_large = 10;
  double T_start = -200;
  double T_end = 600;
  double T_start_fine = 410;
  double T_end_fine = 460;
  int nT;
  double *T_degC = init_temps(&nT, dT_small, dT_large, T_start, T_end,
                  T_start_fine, T_end_fine);
  double beta;
  // save equilibration data and stat inefficiency at T%20 =0
  int T_save_step = 20;
  /* done for all temps: */
  double *E_mean = malloc(sizeof(double[nT]));
  double *E_mean_approx = malloc(sizeof(double[nT]));
  double *E_sq_mean = malloc(sizeof(double[nT]));
  double *P_mean = malloc(sizeof(double[nT]));
  double *P_sq_mean = malloc(sizeof(double[nT]));
  double *r_mean = malloc(sizeof(double[nT]));
  double *r_sq_mean = malloc(sizeof(double[nT]));

  // initialize lattice
  int (*nearest)[N_neigh] = malloc(sizeof(int[N_atoms][N_neigh])); // nearest ↩
      neighbors
  int *lattice = malloc(sizeof(int[N_atoms]));
  init_nearestneighbor(Nc, nearest);
  init_ordered_lattice(N_atoms, N_Cu, lattice);
  // initialize macro parameters
  Etot = get_Etot(lattice, N_atoms, nearest);
  P = get_order_parameter(lattice, N_Cu);
  r = get_short_range_order_parameter(lattice, nearest, N_Cu);


  // start simulation
  for (int iT=0; iT<nT; iT++){ // loop over all temps
    printf("Now running T = %.0f degC\n",T_degC[iT]);
    beta = 1/(kB*(T_degC[iT] + degC_to_K));

    // equilibration run
    if (iT!=0){// First run needs longer equlibration
      N_eq=N_eq_short;
    }
    for( int i=0; i<N_eq; i++){
      //take Monte Carlo step.
      MC_step( &Etot, &r, &P, q, lattice, nearest, beta, N_Cu);
```

```
      E_equilibration[i] = Etot;
      P_equilibration[i]= P;
    }
    //Print to file
    if ( ((int)T_degC[iT]) % T_save_step==0){
      write_equil_to_file(T_degC[iT], E_equilibration,N_bonds,P_equilibration,↩
          N_eq);
    }

    // initialize at temperature[iT]
    E_mean_approx[iT] = Etot; // shift to get higher accuracy in variance
    E_mean[iT]        = 0;
    E_sq_mean[iT]     = 0;
    P_mean[iT]        = 0;
    P_sq_mean[iT]     = 0;
    r_mean[iT]        = 0;
    r_sq_mean[iT]     = 0;
    // production run
    for( int i=0; i<N_timesteps; i++){
      MC_step( &Etot, &r, &P, q, lattice, nearest, beta, N_Cu);
      E_production[i] = Etot- E_mean_approx[iT];
      update_E_P_r(iT, Etot-E_mean_approx[iT], E_mean, E_sq_mean, P, P_mean,
           P_sq_mean, r, r_mean,r_sq_mean, lattice, nearest, N_Cu);
    }
    E_mean[iT]    *= 1/(double)N_timesteps;
    E_sq_mean[iT] *= 1/(double)N_timesteps;
    P_mean[iT]    *= 1/(double)N_timesteps;
    P_sq_mean[iT] *= 1/(double)N_timesteps;
    r_mean[iT]    *= 1/(double)N_timesteps;
    r_sq_mean[iT] *= 1/(double)N_timesteps;

    if ( ((int)T_degC[iT]) %T_save_step==0){ // calculate stat inefficiency
      E_Var = E_sq_mean[iT] - E_mean[iT]*E_mean[iT];
      printf("Calculating statistical inefficiencies \n");
      get_phi (phi, N_timesteps, E_mean[iT], E_Var, E_production,N_k,N_skip);
      get_varF_block_average(var_F, N_timesteps, E_mean[iT], E_Var,
                E_production, N_k, N_skip);
      write_stat_inefficiency_to_file(T_degC[iT], phi, var_F, N_k, N_skip);
    }
  }//END temp for


  //PRINT TO FILE
  write_production(T_degC, nT, E_mean_approx, E_mean, E_sq_mean,
           P_mean, P_sq_mean, r_mean, r_sq_mean);

  // DON'T FORGET TO FREE ALL malloc's.
  free(nearest);          nearest = NULL;
  free(lattice);          lattice = NULL;
  free(E_equilibration);  E_equilibration = NULL;
  free(P_equilibration);  P_equilibration = NULL;
  free(E_mean);           E_mean = NULL;
  free(E_mean_approx);    E_mean_approx = NULL;
  free(E_sq_mean);        E_sq_mean = NULL;
  free(P_mean);           P_mean = NULL;
  free(P_sq_mean);        P_sq_mean = NULL;
  free(r_mean);           r_mean = NULL;
  free(r_sq_mean);        r_sq_mean = NULL;
  free(E_production);     E_production = NULL;
  free(phi);              phi = NULL;
  free(var_F);            var_F = NULL;
  free(T_degC);           T_degC = NULL;

  gsl_rng_free(q); // deallocate  rng
  return 0;
}
```

A.2 Misc functions : `funcs.c`

```
#include "funcs.h"

/*********************** get functions ************************************/
double get_bond_E(int site_1, int site_2){
  double tmp=0;
  switch(site_1 + site_2 ) {
  case 0 :
    //return E_ZnZn;
    tmp=-0.113;
    break;
  case 1 :
    //return E_CuZn;
    tmp= -0.294;
    break;
  case 2 :
    //return E_CuCu;
    tmp=-0.436;
```

```
    break;
  }
  return tmp;
}

double get_order_parameter(int *lattice, int N_Cu){
  int N_Cu_in_Cu_lattice=0;
  for(int i=0;i<N_Cu;i++){
    N_Cu_in_Cu_lattice+=lattice[i];
  }
  return (double)N_Cu_in_Cu_lattice/N_Cu *2 -1;
}

double get_short_range_order_parameter(int *lattice, int(*nearest)[N_neigh],
                       int N_Cu){
  int N_CuZnBonds=0;
  for(int i=0;i<N_Cu;i++){
    for( int j=0; j<N_neigh; j++){
      N_CuZnBonds+= (lattice[i] + lattice[nearest[i][j]]) == 1 ;
    }
  }
  return (double) N_CuZnBonds/(4*N_Cu)-1;
}

double get_Etot(int *lattice, int N_atoms, int (*nearest)[N_neigh]){
  double Etot=0;
  for(int i=0; i<N_atoms; i++){
    for( int j=0; j<N_neigh; j++){
      Etot+= get_bond_E(lattice[i], lattice[nearest[i][j]]);
    }
  }
  return Etot/2;
}

void get_phi (double *phi, int N_times, double f_mean,
          double f_var, double *data, int N_k, int N_skip){
  for (int k=0; k<N_k; k++) {
    phi[k] = 0;
    for (int i=0; (i+k)*N_skip<N_times; i++) {
      phi[k] += data[i*N_skip]*data[(i+k)*N_skip];
    }
    phi[k] = (phi[k]/(N_times/N_skip - k) - f_mean*f_mean)/f_var;
  }
}

void get_varF_block_average(double *var_F, int N_times, double f_mean,
                double f_var, double *data, int N_k, int N_skip){
  // block average
  int block_size;
  double Fj;
  int number_of_blocks;
  for (int k=0; k<N_k; k++) { // block size loop
    block_size = N_skip * (k+1);
    number_of_blocks = N_times/block_size;
    var_F[k] = 0;
    for (int j=0; j<number_of_blocks; j++) {// loop over all blocks
      Fj = 0;
      for (int i=0; i<block_size; i++) {// internal block loop
        Fj += data[j*block_size + i];
      }
      Fj *= 1/(double)block_size; // these are the values we need the variance ↩
          of F
      var_F[k] += Fj*Fj; // will become the variance soon
    }
    var_F[k] = var_F[k]/number_of_blocks - f_mean*f_mean;
    var_F[k] *= block_size/f_var;
  }
}

/************** Monte Carlo step functions ***********************************/
void MC_step( double *Etot, double *r, double *P, gsl_rng *q,
              int *lattice, int (*nearest)[N_neigh], double beta, int N_Cu){
  /*
     takes a Monte Carlo step. Updates the lattice and `Etot`
  */
  // Picks two random sites in the whole lattice.
  int i1 = (int)(2*N_Cu*gsl_rng_uniform(q));
  int i2 = (int)(2*N_Cu*gsl_rng_uniform(q));
  // saves the original values
  int old_1 = lattice[i1];
  int old_2 = lattice[i2];
  // Used to clacluate the change in `Etot` and `r`
  double dr = 0;
  double dE = 0;
  // We only need to do something if the two atoms aer different
  if (old_1 != old_2){
    for( int j=0; j<N_neigh; j++){
      /*
     The change in `Etot` and `r` are first _minus_ the old energies and `r`
     contributtions.
      */
```

```
      dE-= get_bond_E(lattice[i1], lattice[nearest[i1][j]])
      +get_bond_E(lattice[i2], lattice[nearest[i2][j]]);

      dr -= ((lattice[i1] + lattice[nearest[i1][j]]) == 1)
       +((lattice[i2] + lattice[nearest[i2][j]]) == 1);
    }
    /* Then we do the change of the two atoms */
    lattice[i1] = old_2;
    lattice[i2] = old_1;
    for( int j=0; j<N_neigh; j++){
      /*
     And _add_ the contribtions to `Etot` and `r` from the updated lattice.
      */
      dE+= +get_bond_E(lattice[i1], lattice[nearest[i1][j]])
    +get_bond_E(lattice[i2], lattice[nearest[i2][j]]);

      dr += ((lattice[i1] + lattice[nearest[i1][j]]) == 1)
       +((lattice[i2] + lattice[nearest[i2][j]]) == 1);
    }

    if ( (dE<=0)|| (exp(-beta * dE) >  gsl_rng_uniform(q)) ){
      /*
     The test is accepted if dE < 0 (accept immediately), OR
     otherwise it's accepted with a probability of `exp(-beta * dE)`
      */
      // Updates P
      if (i1 < N_Cu) *P += (double)(lattice[i1] - old_1 )/N_Cu *2;
      if (i2 < N_Cu) *P += (double)(lattice[i2] - old_2 )/N_Cu *2;
    }else{
      /*
     If the test failed, we change back to the old lattice configuration
     and no change happes to `Etot` or `r`
      */
      lattice[i1] = old_1;
      lattice[i2] = old_2;
      dE = 0;
      dr = 0;
    }// end if step is accepted
    *Etot += dE;
    *r += dr/(4*N_Cu);
  }// end if atoms are different
}

void update_E_P_r(int iT, double E_dev, double *E_mean, double *E_sq_mean,
          double P, double *P_mean, double *P_sq_mean,
          double r, double *r_mean, double *r_sq_mean,
          int *lattice, int (*nearest)[N_neigh], int N_Cu){
  /*
    Updates the macro parameters `E`, `P`, and `r`, as well as their squares.
    Runs in every Monte Carlo step during the producction run.
  */
  E_mean[iT] += E_dev;
  E_sq_mean[iT] += E_dev * E_dev;

  P_mean[iT] += P;
  P_sq_mean[iT] += P*P;

  r_mean[iT] += r;
  r_sq_mean[iT] += r*r;
}

/************************ initializing functions*****************************/
void * init_temps( int *nT, double dT_small, double dT_large,
           double T_start, double T_end, double T_start_fine,
           double T_end_fine){
  /*
    Creates an array `T_degC` with the temperatures to loop over in the main
    function, given the fine temperature step range and the sizes of the
    temperature steps.
  */
  *nT = (int) ((T_end_fine - T_start_fine)/dT_small
           +(T_start_fine-T_start + T_end-T_end_fine)/dT_large +1);
  double *T_degC = malloc(sizeof(double[*nT]));
  T_degC[0] = T_start;
  for (int iT=1; iT<*nT; iT++){ // loop over all temps
    if (T_degC[iT-1]>=T_start_fine && T_degC[iT-1]<T_end_fine){
      T_degC[iT] = T_degC[iT-1] + dT_small;
    }else{
      T_degC[iT] = T_degC[iT-1] + dT_large;
    }
  }
  return T_degC;
}


void init_ordered_lattice(int N_atoms, int N_Cu, int *lattice){
  /*
     Initialize lattice with Cu atoms (1) in Cu lattice (i=0:N_Cu-1)
     and Zn (0) in Zn lattice (i=N_cu:N_atoms-1):
  */
  for( int i=0; i<N_Cu; i++){
```

```
    lattice[i] = 1;
  }
  for( int i=N_Cu; i<N_atoms; i++){
    lattice[i] = 0;
  }
}

void init_random_lattice(int N_atoms, int N_Cu, int *lattice, gsl_rng *q){
  /*
    Initialize lattice with Cu and Zn atoms randomly distributed:
  */
  for( int i=0; i<N_Cu; i++){
    lattice[i] = (int)(gsl_rng_uniform(q)+0.5);
    lattice[i+N_Cu] = 1-lattice[i];
  }
}


void init_nearestneighbor(int Nc, int (*nearest)[N_neigh]){
  /*
    Create a matrix `nearest[i][j]` with the index of the `j`th neares
    neighbors to site `i`.
    N.B. Each site has `N_neigh` (8) nearest neighbors.
  */
  int i_atom;
  int N_Cu = Nc*Nc*Nc;
  for( int i=0; i<Nc; i++){
    for( int j=0; j<Nc; j++){
      for( int k=0; k<Nc; k++){
        i_atom = k + Nc*j + Nc*Nc*i;
        // k i j in one lattice <=> "k-0.5" "i-0.5" "j-0.5" in the other lattice
        // use mod to handle periodic boundary conditions
        nearest[i_atom][0] = k        + Nc*j          + Nc*Nc*i           +N_Cu;
        nearest[i_atom][1] = k        + Nc*j          + Nc*Nc*((i+1)%Nc)  +N_Cu;
        nearest[i_atom][2] = k        + Nc*((j+1)%Nc) + Nc*Nc*i           +N_Cu;
        nearest[i_atom][3] = k        + Nc*((j+1)%Nc) + Nc*Nc*((i+1)%Nc)  +N_Cu;
        nearest[i_atom][4] = (k+1)%Nc + Nc*j          + Nc*Nc*i           +N_Cu;
        nearest[i_atom][5] = (k+1)%Nc + Nc*j          + Nc*Nc*((i+1)%Nc)  +N_Cu;
        nearest[i_atom][6] = (k+1)%Nc + Nc*((j+1)%Nc) + Nc*Nc*i           +N_Cu;
        nearest[i_atom][7] = (k+1)%Nc + Nc*((j+1)%Nc) + Nc*Nc*((i+1)%Nc)  +N_Cu;

        // k i j in one lattice <=> "k+0.5" "i+0.5" "j+0.5" in the other lattice
        // use mod to handle periodic boundary conditions
        // note that mod([negative])<0 :
        i_atom += N_Cu;
        nearest[i_atom][0] =k          + Nc*j            + Nc*Nc*i;
        nearest[i_atom][1] =k          + Nc*j            + Nc*Nc*((i-1+Nc)%Nc)↩
            ;
        nearest[i_atom][2] =k          + Nc*((j-1+Nc)%Nc) + Nc*Nc*i;
        nearest[i_atom][3] =k          + Nc*((j-1+Nc)%Nc) + Nc*Nc*((i-1+Nc)%Nc)↩
            ;
        nearest[i_atom][4] =(k-1+Nc)%Nc + Nc*j            + Nc*Nc*i;
        nearest[i_atom][5] =(k-1+Nc)%Nc + Nc*j            + Nc*Nc*((i-1+Nc)%Nc)↩
            ;
        nearest[i_atom][6] =(k-1+Nc)%Nc + Nc*((j-1+Nc)%Nc) + Nc*Nc*i;
        nearest[i_atom][7] =(k-1+Nc)%Nc + Nc*((j-1+Nc)%Nc) + Nc*Nc*((i-1+Nc)%Nc)↩
            ;
      }
    }
  }
}

void* init_random(){
  /*
    Initializes a GSL random nuber generator, and returns the pointer.
  */
  gsl_rng *q;
  const  gsl_rng_type *rng_T;    // static  info  about  rngs
  gsl_rng_env_setup ();          // setup  the  rngs
  rng_T = gsl_rng_default;       // specify  default  rng
  q = gsl_rng_alloc(rng_T);      // allocate  default  rng
  gsl_rng_set(q,time(NULL));     // Initialize  rng
  return q;
}


/************************ file I/O functions *********************************/
void write_equil_to_file(double T_degC, double *E_equilibration, int N_bonds,
             double *P, int N_eq){
  /*
    Writes the energy per bond `E_equilibration`/`N_bonds` and order
    parameter `P`, at each Monte Carlo step during the equlibration runs.
  */
  FILE *file_pointer;
  char file_name[256];
  sprintf(file_name,"../data/E_equilibration-T%d.tsv", (int) T_degC);
  file_pointer = fopen(file_name, "w");
  for (int i=0; i<N_eq; i++){
    fprintf(file_pointer, "%.8f\t%.8f \n", E_equilibration[i]/N_bonds,P[i]);
  }
  fclose(file_pointer);
```

```
}

void write_production(double *T_degC, int nT, double *E_mean_approx,
              double *E_mean, double *E_sq_mean,
              double *P_mean, double *P_sq_mean,
              double *r_mean, double *r_sq_mean){
  /*
    Writes the macro parameters `E_mean_approx`, `E_mean`, `E_sq_mean`,
    `P_mean`, `P_sq_mean`, `r_mean`, and `r_sq_mean` for each temperature
    to file.
  */
  void* init_random();
  FILE *file_pointer;
  char file_name[256];
  sprintf(file_name,"../data/E_production.tsv");
  file_pointer = fopen(file_name, "w");
  fprintf(file_pointer, "%% T[degC]\t E_approx\t<E-E_approx>\t<(E-E_approx)^2>\↩
      tP\tr\n");
  for (int iT=0; iT<nT; iT++){
    fprintf(file_pointer, "%.2f\t%.8e\t%.8e\t%.8e\t%.8f\t%.8f\t %.8f\t%.8f \n",
        T_degC[iT], E_mean_approx[iT], E_mean[iT], E_sq_mean[iT], P_mean[iT],
        P_sq_mean[iT], r_mean[iT], r_sq_mean[iT]);
  }
  fclose(file_pointer);
}

void write_stat_inefficiency_to_file(double T_degC, double *phi, double *var_F,
                     int N_k, int N_skip){
  /*
    Writes the auto-correlation `phi` and block varaiances `var_F` for each
    tested temperature to file.
  */
  FILE *file_pointer;
  char file_name[256];
  sprintf(file_name,"../data/stat_inefficiency-T%d.tsv", (int) T_degC);
  file_pointer = fopen(file_name, "w");
  for (int i=0; i<N_k; i++){
    fprintf(file_pointer, "%d\t%.8f\t%.8f \n", i*N_skip, phi[i],var_F[i]);
  }
  fclose(file_pointer);
}
```

B Auxiliary

B.1 Makefile

```
CC = gcc
CFLAGS = -O3 -Wall

LIBS = -lm -lgsl -lgslcblas

HEADERS = funcs.h
OBJECTS = funcs.o


%.o: %.c $(HEADERS)
    $(CC) -c -o $@ $< $(CFLAGS)

all: Task2



Task2: $(OBJECTS) main_T2.c
    $(CC) -o $@ $^ $(CFLAGS) $(LIBS)

# $(PROGRAMS): $(OBJECTS) main_T1.c
#   $(CC) -o $@ $^ $(CFLAGS) $(LIBS)

clean:
    rm -f *.o
    touch *.c
```

C MATLAB scripts

C.1 Task 1 and analysis scripts for Task 2

```
%% initial
```

```
2
3  tmp = matlab.desktop.editor.getActive; %% cd to current path
4  cd(fileparts(tmp.Filename));
5  set(0,'DefaultFigureWindowStyle','docked');
6  warning('off','MATLAB:handle_graphics:exceptions:SceneNode'); % interpreter
7  GRAY = 0.7*[0.9 0.9 1];
8  kB = 8.61733e-5;
9  %% task 1: MFT
10 doSave = 0;
11 clc
12
13 Pmin = 0;
14 Pmax = 1;
15
16 E_CuCU = -.436;
17 E_ZnZn = -.133;
18 E_CuZn = -.294;
19
20 E0=2*(E_CuCU+E_ZnZn+2*E_CuZn);
21 Delta_E=(E_CuCU+E_ZnZn-2*E_CuZn);
22
23 E0_bar=E0/Delta_E;
24 E_MFT=@(P) E0 - 2*P.^2*Delta_E;
25 E_MFT_bar=@(P) E0_bar - 2*P.^2;
26 dE_MFTdP =@(P) - 4*P*Delta_E;
27
28 F_MFT = @(P,Tbar) E_MFT_bar(P) + Tbar*(-2*log(2) + (1+P).*log(1+P)+(1-P).*log(1-↩
       P));
29 P_eq=@(Tbar)  fminbnd(@(P)F_MFT(P, Tbar), Pmin, Pmax, optimset('TolX',1e-9));
30
31 Tbar = linspace(0,3,1000)';
32 T_MFT=Tbar*Delta_E/kB;
33 T_MFT_degC = T_MFT - 273.15;
34 Peq = zeros(size(Tbar));
35 for iT = 1:numel(Tbar)
36     Peq(iT) = P_eq(Tbar(iT));
37 end
38
39 % plot P(T) and make a fit
40 figure(1);clf
41 plot(Tbar, Peq);hold on
42
43 dT=2-Tbar(Tbar<2);
44 Peq_nonzero = Peq(Tbar<2);
45
46 I_good = (dT<0.1);
47 log_dT = log(dT(I_good));
48 log_P  = log(Peq_nonzero(I_good));
49 A=[ones(size(log_dT)), log_dT]\log_P;
50 b      = exp(A(1));
51 alpha = A(2);
52 fprintf('alpha = %.3f\n', alpha)
53
54 P_approx = @(alpha,b,Tbar) b*(2-Tbar).^alpha;
55 plot(Tbar(Tbar<2),P_approx(alpha,b,Tbar(Tbar<2)),'k:')
56 xlabel('$k_B T/ \Delta E$')
57 ylabel('$P$')
58 legend('$P$', 'fit $P \propto (2-\bar T)^\alpha$')
59 ylim([0 1.3]);
60 if doSave; setFigureSize(gcf, 300, 600); end
61
62 % plot E_MFT and the fit
63 figure(2);clf
64 plot(Tbar,E_MFT(Peq)); hold on
65 plot(Tbar,E_MFT(P_approx(alpha,b,Tbar)),'k:')
66 xlabel('$k_B T/ \Delta E$')
67 ylabel('$U$ [eV/cell]')
68 legend('$E_{\rm MFT}$', 'fit $P \propto (2-\bar T)^\alpha$', 'location', '↩
       NorthWest');
69 ylim([-2.36 -2.3]);
70 if doSave; setFigureSize(gcf, 300, 600); end
71
72 figure(3);clf
73 C=diff(E_MFT(Peq))./diff(T_MFT);
74 plot(Tbar(1:end-1), C*1e3); hold on
75 C_approx=4*b^2*kB*alpha*(2-Tbar).^(2*alpha-1);
76 plot(Tbar(Tbar<2),1e3*C_approx(Tbar<2),'k:')
77 xlabel('$k_B T/ \Delta E$')
78 ylabel('$C$ [meV K$^{-1}$/cell]')
79 legend('$C_{\rm MFT}$', 'fit $P \propto (2-\bar T)^\alpha$', 'location', '↩
       NorthWest');
80 ylim([0 0.3])
81 if doSave; setFigureSize(gcf, 300, 600); end
82
83 ImproveFigureCompPhys()
84 if doSave
85     saveas(1, '../figures/P_MFT.eps', 'epsc');
86     saveas(2, '../figures/E_MFT.eps', 'epsc');
87     saveas(3, '../figures/C_MFT.eps', 'epsc');
88 end
89 %% task 2: ...
```

```
clc;
doSave = 1;
Ts=[-200:20:600]';
TsToPlot = [300 440 600]';
t_eq=0;

figure(10);clf;

for i=1:numel(TsToPlot)
    data = load(sprintf('../data/E_equilibration-T%d.tsv',TsToPlot(i)));
    E = data(:,1);
    steps = 1:length(E);
    %P = data(:,2);
    plot(steps/1e6, E*1000); hold on
end
legstr = strcat({'$T='}, num2str(TsToPlot), '^\circ$ C');
legend(legstr, 'location', 'NorthWest');
ylabel('$E$ [meV/$N_{\rm bonds}$]')
xlabel('$N_{\rm steps}/10^6$')
if doSave
    ImproveFigureCompPhys(gcf)
    setFigureSize(gcf, 300, 600);
    saveas(gcf, '../figures/equilibration.eps', 'epsc');
end


figure(1000); clf;
[ns_Phi,ns_block] = deal(nan(size(Ts)));
Nskip = 10;
for i=1:numel(Ts)
    data = load(sprintf('../data/stat_inefficiency-T%d.tsv',Ts(i)));
    k = data(:,1);
    block_size = k+Nskip;
    phi = data(:,2);
    VarF_norm = data(:,3);
    kstar = k(find(log(phi)<-2, 1, 'first'));
    if ~isempty(kstar)
        ns_Phi(i) = kstar;
    end
    N_avg = 20;
    filtereddata = movmean(VarF_norm,N_avg);
    ns_block(i) = filtereddata(end);

    if any(Ts(i) == TsToPlot)
        subplot(2,1,1)
        plot(k, log(phi));hold on;

        plot([0 kstar kstar], [-2 -2 -6],':k')
        ylim([-4 0]);
        legend('data', 'estimated $n_s$', 'location', 'northeast');
        xlabel('$k$'); ylabel('ln $\phi_k$');
        xlim([0 2e5])

        subplot(2,1,2);
        plot(block_size, VarF_norm); hold on;

        plot(block_size(N_avg:end), filtereddata(N_avg:end));
        plot(block_size, filtereddata(end)*ones(size(block_size)), ':k');
        legend('data', 'moving average', 'estimated $n_s$', 'location', '↩
            northwest');
        xlabel('block size $B$'); ylabel('$B$ Var[$F$]/Var[$f$] ');
        ylim([0 2e5])
    end
end
%Ts = Ts(~isnan(ns_Phi));
%ns_Phi = ns_Phi(~isnan(ns_Phi));
%ns_block = ns_block(~isnan(ns_Phi));

ImproveFigureCompPhys()
%%

data = load('../data/E_production.tsv');
T_degC = data(:,1);
N_Cu = 1e3;
N_timeSteps = 1e7;

Emean_approx = data(:,2);
Emean_shifted = data(:,3);
E_sq_mean_shifted = data(:,4);

E_Var = (E_sq_mean_shifted - Emean_shifted.^2);

Cv = 1./(kB * (T_degC+273.15).^2).*E_Var;
U = Emean_shifted + Emean_approx;
U_std = sqrt(E_Var/N_timeSteps);
P = data(:,5);
P_std = sqrt((data(:,6)-P.^2)/N_timeSteps); % without ns so far
r = data(:,7);
r_std = sqrt((data(:,8)- r.^2)/N_timeSteps);

ind = zeros(size(Ts));
```

```
for i = 1:numel(Ts)
    ind(i) = find(Ts(i) == T_degC);
end

figure(11);clf;

errorbar(Ts, U(ind), 2*U_std(ind).*sqrt(ns_Phi), '.k','linewidth', 1.5); hold on;
plot(T_degC, U); hold on;

plot(T_degC, cumtrapz(T_degC, Cv) + U(1));

figure(12); clf;
plot(T_degC, Cv/N_Cu); hold on;
plot(T_MFT_degC(1:end-1), C); hold on

figure(13);clf;
errorbar(Ts, P(ind), 2*P_std(ind).*sqrt(ns_Phi), '.k', 'linewidth', 1.5); hold on;
%errorbar(Ts, P(ind), 2*P_std(ind).*sqrt(ns_block), '.r','linewidth', 1.5);hold on;
plot(T_degC, P, 'color', GRAY); hold on;

plot(T_MFT_degC, Peq, '--k');

figure(14);clf;
errorbar(Ts, r(ind), 2*r_std(ind).*sqrt(ns_Phi), '.k','linewidth', 1.5);hold on;
hold on; plot(T_degC, r, T_degC, P.^2, T_MFT_degC, Peq.^2, 'k');

legend('$r$','$P^2$',  '$r_{\rm MFT}$ ')
ImproveFigureCompPhys('linewidth', 2)

% for ifig = 1:2
%     figure(ifig);
%     h = legend(strcat({'$dt = $ '}, num2str(round(dt',4)) , ' ps'));
%     xlabel('$t$ [ps]');
%     ax = gca;
%     if ifig ==1
%         ylabel('$T$ [K]')
%         ax.YLim = [400 1800];
%     else
%         ylabel('$E_{\rm tot}$ [eV/unit cell]');
%         ax.YTick = (-13:0.1:-10);
%         ax.YLim = [-12.6 -12.0];
%     end
%     ImproveFigureCompPhys(gcf,'Linewidth', 2);setFigureSize(gcf, 400, 400);
% end
% saveas(1, '../figures/dt-scan-temperature.eps', 'epsc')
% saveas(2, '../figures/dt-scan-energy.eps', 'epsc')

%%
```

C.2 Improve figure appearance: `ImproveFigureCompPhys.m`

```
function ImproveFigureCompPhys(varargin)
%ImproveFigureCompPhys Improves the figures of supplied handles
%  Input:
% - none (improve all figures) or handles to figures to improve
% - optional:
%       LineWidth  int
%       LineStyle  column vector cell, e.g. {'-','--'}',
%       LineColor  column vector cell, e.g. {'k',[0 1 1], 'MYBLUE'}'
%                           colors: MYBLUE,MYORANGE,MYGREEN,MYPURPLE, MYYELLOW,
%                           MYLIGHTBLUE, MYRED
%       Marker column vector cell, e.g. {'.', 'o', 'x'}'

% ImproveFigure was originally written by Adam Stahl, but has been heavily
% modified by Linnea Hesslow


%%% Handle inputs
% If no inputs or if the first argument is a string (a property rather than
% a handle), use all open figures
if nargin == 0 || ischar(varargin{1})
    %Get all open figures
    figHs = findobj('Type','figure');
    nFigs = length(figHs);
else
    % Check the supplied figure handles
    figHs = varargin{1};
    figHs = figHs(ishandle(figHs) == 1); %Keep only those handles that are
        proper graphics handles
    nFigs = length(figHs);
end

% Define desired properties
```

```
titleSize = 24;
interpreter = 'latex';
lineWidth = 4;
axesWidth = 1.5;
labelSize = 22;
textSize = 20;
legTextSize = 18;
tickLabelSize = 18;
LineColor = {};
LineStyle = {};
Marker = {};

% define colors
co =  [ 0    0.4470    0.7410
    0.8500    0.3250    0.0980
    0.9290    0.6940    0.1250
    0.4940    0.1840    0.5560
    0.4660    0.6740    0.1880
    0.3010    0.7450    0.9330
    0.6350    0.0780    0.1840 ];
colors = struct('MYBLUE', co(1,:),...
    'MYORANGE', co(2,:),...
    'MYYELLOW', co(3,:),...
    'MYPURPLE', co(4,:),...
    'MYGREEN', co(5,:),...
    'MYLIGHTBLUE', co(6,:),...
    'MYRED',co(7,:),...
    'GERIBLUE', [0.3000    0.1500    0.7500],...
    'GERIRED', [1.0000    0.2500    0.1500],...
    'GERIYELLOW', [0.9000    0.7500    0.1000],...
    'LIGHTGREEN', [0.4    0.85    0.4],...
    'LINNEAGREEN', [7 184 4]/255);

% Loop through the supplied arguments and check for properties to set.
for i = 1:nargin
    if ischar(varargin{i})
        switch lower(varargin{i})   %Compare lower case strings
            case 'linewidth'
                lineWidth = varargin{i+1};
            case 'linestyle'
                LineStyle = varargin{i+1};
            case 'linecolor'
                LineColor = varargin{i+1};
                for iLineColor = 1:numel(LineColor)
                    if isfield(colors, LineColor{iLineColor})
                        LineColor{iLineColor} = colors.(LineColor{iLineColor});
                    end
                end
            case 'marker'
                Marker = varargin{i+1};
        end
    end
end
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

%%% Improve the figure(s)

for iFig = 1:nFigs

    fig = figHs(iFig);

    lineObjects = findall(fig, 'Type', 'line');
    textObjects = findall(fig, 'Type', 'text');
    axesObjects = findall(fig, 'Type', 'axes');
    legObjects =  findall(fig, 'Type', 'legend');
    contourObjects = findall(fig,'Type','contour'); % not counted as lines

    %%% TEXT APPEARANCE: first set all to textSize and then change the ones
    %%% that need to be changed again

    %Change size of any text objects in the plot
    set(textObjects,'FontSize',textSize);
    set(legObjects,'FontSize',legTextSize);

    %%% FIX LINESTYLE, COLOR ETC. FOR EACH PLOT SEPARATELY
    for iAx =  1:numel(axesObjects)
        lineObjInAx = findall(axesObjects(iAx), 'Type', 'line');

        %set line style and color style (only works if all figs have some
        %number of line plots..)
        if ~isempty(LineStyle)
            set(lineObjInAx, {'LineStyle'}, LineStyle)
            set(contourObjects, {'LineStyle'}, LineStyle); %%%%%%
        end
        if ~isempty(LineColor)
            set(lineObjInAx, {'Color'}, LineColor)
            set(contourObjects, {'LineColor'}, LineColor); %%%%%%
        end
        if ~isempty(Marker)
            set(lineObjInAx, {'Marker'}, Marker)
```

```
            set(lineObjInAx, {'Markersize'}, num2cell(10+22*strcmp(Marker, '.'))↩
                )
        end

        %%% change font sizes.
        % Tick label size
        xLim = axesObjects(iAx).XLim;
        axesObjects(iAx).FontSize = tickLabelSize;
        axesObjects(iAx).XLim = xLim;
        %Change label size
        axesObjects(iAx).XLabel.FontSize = labelSize;
        axesObjects(iAx).YLabel.FontSize = labelSize;

        %Change title size
        axesObjects(iAx).Title.FontSize = titleSize;
    end

    %%% LINE APPEARANCE
    %Change line thicknesses
    set(lineObjects,'LineWidth',lineWidth);
    set(contourObjects, 'LineWidth', lineWidth);
    set(axesObjects, 'LineWidth',axesWidth)

    % set interpreter: latex or tex
    set(textObjects, 'interpreter', interpreter)
    set(legObjects, 'Interpreter', interpreter)
    set(axesObjects,'TickLabelInterpreter', interpreter);
end
end
```

C.3 Change size of figures: `setFigureSize.m`

```
function [ fig ] = setFigureSize( fig, H, W )
fig.Units = 'points';
fig.WindowStyle = 'normal'; % undock
fig.Position(3:4) = [W H];
end
```