

NB: The graded, first version of the report must be returned if you hand in a second time!

H1b: MD simulation – dynamic properties

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Task N ^o	Points	Avail. points
Σ		

Introduction

Already in antiquity people studied the effect of particles impinging on other particles. Since then the art has developed ... (If you like to do so, you may take the opportunity to put the methods in a wider perspective here.) Here is a random reference.[1]

Task 1

We determined the theoretical lattice parameter

Figure 2 shows the potential energy as a function of the lattice parameter. We used a quadratic fit to find the minimum energy, and obtained $V_{\text{eq}} \approx 65.38 \text{ \AA}^3$. This corresponds to the equilibrium lattice parameter $a_{\text{eq}} \approx 4.029 \text{ \AA}$ at 0 K, which we took as the initial lattice parameter for the following tasks.

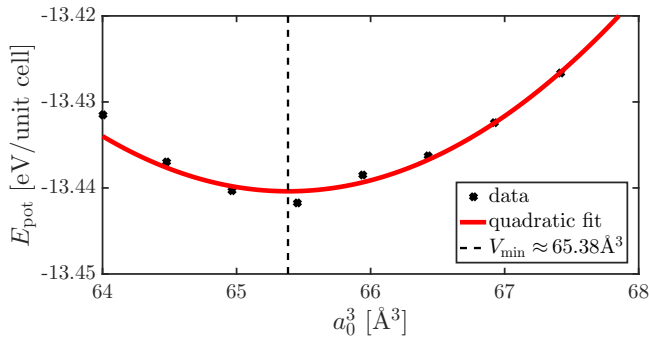


Figure 1: The potential energy per unit cell for aluminum as a function of the lattice parameter cubed.

We find that figure 2 looks similar to the figure 1 in the homework problem file.

Task 5

Equation (82) in MD lecture notes:

$$\Delta_{\text{MSD}}(t) = \lim_{T \rightarrow \infty} \frac{1}{T} \int_0^T dt' \frac{1}{N_{\text{atoms}}} \sum_{i=0}^{N_{\text{atoms}}-1} [\mathbf{r}_i(t+t') - \mathbf{r}_i(t')]^2 \quad (1)$$

\Rightarrow

$$\Delta_{\text{MSD}}(t_k) \approx \frac{1}{N_T - k} \frac{1}{N_{\text{atoms}}} \sum_{j=0}^{N_T-k-1} \sum_{i=0}^{N_{\text{atoms}}-1} [\mathbf{r}_i(t_{k+j}) - \mathbf{r}_i(t_j)]^2 \quad (2)$$

To determine M, we used mean of ... for t_i ...

Task 7

The average “power” content in variable $X(t')$, at some time, t , during some range of time, T , can be defined as

$$P_X(t, T) = \frac{1}{T} \int_{t-T/2}^{t+T/2} dt' X^2(t'). \quad (3)$$

This quantity can (in physically relevant systems) also be defined for the process over all,

$$P_X = \lim_{T \rightarrow \infty} P_X(T) = \lim_{T \rightarrow \infty} \frac{1}{T} \left\langle \int_0^T dt' X^2(t') \right\rangle. \quad (4)$$

At this stage, we can introduce a We have the Fourier transform

$$\hat{f}(\omega) = \int_{-\infty}^{\infty} dt f(t) e^{i\omega t}, \quad (5)$$

Using these two functions, we can define a power spectrum

$$\begin{aligned} \hat{P}(\omega) &= \langle |\hat{v}(\omega)|^2 \rangle_A = \langle \hat{v}(\omega) \cdot \tilde{\hat{v}}(\omega) \rangle_A \\ &= \left\langle \int_{-\infty}^{\infty} dt v(t) e^{i\omega t} \int_{-\infty}^{\infty} dt' v(t') e^{-i\omega t'} \right\rangle_A, \end{aligned} \quad (6)$$

where $\tilde{\hat{v}}$ denotes the complex conjugate of \hat{v} . We can now change variables to $t = t' + \tau$ and note that the atom averages only falls on the velocities, which gives

$$\hat{P}(\omega) = \int_{-\infty}^{\infty} d\tau e^{i\omega\tau} \int_{-\infty}^{\infty} dt' \langle v(t' + \tau) \cdot v(t') \rangle_A, \quad (7)$$

Problem 1

As a starting point we first look at scattering from a hard-sphere potential. We also consider the Lennard–Jones potential, which is depicted in Figure ?? *(Always refer to Figures in the text.)*

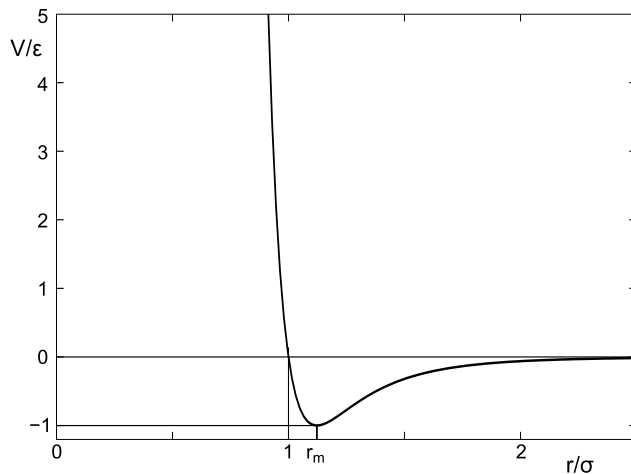


Figure 2: The Lennard–Jones potential. Make sure you label and have units on all axes! Also make sure that labels etc. are legible and that, if you print in black and white, that you use different line styles when required to differentiate between curves. In MATLAB you can export any figure to an .eps file from File → Export... in the Figure window.

Problem 2

In the following we give an example of how to produce a table. Use the code for Table 1 as a template.

Table 1: A dummy table		
Col. 1	Col. 2	Col. 3
the	quick	brown
fox	jumps	over
the	lazy	dog

Problem 3

If you find some part of the code particularly interesting you may include it in the text, otherwise it should be included in the appendix. If you do want to include code the following commands will print the text directly, with no \LaTeX commands executed:

```
% Hello world ten times in MATLAB
for i = 1 : 10
    fprintf('Hello world %d!\n',i);
end
```

```
# Hello world ten times in Python
for i in range(10):
    print 'Hello world %d!' % i
```

Problem 4

At some point it may be appropriate to include equations. It is done in the following way:

$$V(r) = 4\epsilon \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 \right] \quad (8)$$

Do number and reference all your equations.

Concluding discussion

Use your favourite flavor of \LaTeX to compile the file:

```
xelatex template.tex
pdflatex template.tex
latex template.tex
```

should all work. If you use `pdflatex` or `xelatex`, included figures need to be in pdf, jpg, or png format. If you want to include eps figures, you can easily convert them to pdf using the command

```
ps2pdf -dEPSCrop figure.eps figure.pdf
```

References

- [1] Leslie Lamport, *\LaTeX : A Document Preparation System*. Addison Wesley, Massachusetts, 2nd Edition, 1994.

A Source Code

Include all source code here in the appendix. Keep the code formatting clean, use indentation, and comment your code to make it easy to understand. Also, break lines that are too long. (Keep them under 80 characters!)

A.1 Main program task 1: main_T1.c

```
1  /*
2  MD_main.c
3
4  Created by Anders Lindman on 2013-10-31.
5  */
6
7  #include <stdio.h>
8  #include <math.h>
9  #include <stdlib.h>
10
11 #include "initfcc.h"
12 #include "alpotential.h"
13
14 #define N_cells 4
15 #define N_lattice_params 25
16
17
18 /* Main program */
19 int main()
20 {
21
22     int N_atoms = 4*N_cells*N_cells*N_cells;
23     double a0;
24     double a0_min = 4.0;
25     double a0_max = 4.2;
26     double da0 = (a0_max - a0_min)/N_lattice_params;
27
28
29     double (*pos)[3] = malloc(sizeof(double[N_atoms][3]));
30     double *energy = malloc(sizeof(double[N_lattice_params]));
31
32
33     FILE *file_pointer;
34
35
36     /* ----- TASK 1 ----- */
37
38     for (int i=0; i<N_lattice_params; i++){
39         a0 = a0_min + i*da0;
40         init_fcc(pos, N_cells, a0);
41         // energy per unit cell
42         energy[i] = get_energy_AL(pos, N_cells*a0, N_atoms )*4/N_atoms;
43     }
44
45     file_pointer = fopen("../data/lattice_energies.tsv", "w");
46     for (int i=0; i<N_lattice_params; i++){
47         a0 = a0_min + i*da0;
48         fprintf(file_pointer, "%.8f \t %.8f \n", a0, energy[i]);
49     }
50     fclose(file_pointer);
51
52
53
54
55     free(pos); pos = NULL;
56     free(energy); energy = NULL;
57     return 0;
58 }
```

A.2 Main program Task 2: main_T2.c

```
1  /*
2  MD_main.c
3
4  Created by Anders Lindman on 2013-10-31.
5  */
6
7  #include <stdio.h>
8  #include <math.h>
9  #include <stdlib.h>
10 #include <time.h>
11
```

```

12 #include "initfcc.h"
13 #include "alpotential.h"
14 #include "funcs.h"
15
16 #define N_cells 4
17 #define AMU 1.0364e-4
18 #define kB 8.6173303e-5
19
20 /* Main program */
21 int main()
22 {
23
24     int N_atoms = 4*N_cells*N_cells*N_cells;
25     double m_Al = 27*AMU;
26
27     double a_eq = 4.03;
28
29     double noise_amplitude = 6.5e-2 * a_eq;
30     double t_max=10;
31     double dt = 1e-3;
32     int N_timesteps = t_max/dt;
33     double t, E_kin;
34
35     double (*pos)[3] = malloc(sizeof(double[N_atoms][3]));
36     double (*momentum)[3] = malloc(sizeof(double[N_atoms][3]));
37     double (*forces)[3] = malloc(sizeof(double[N_atoms][3]));
38     double *temperature = malloc(sizeof(double[N_timesteps]));
39     double *E_tot = malloc(sizeof(double[N_timesteps]));
40
41     FILE *file_pointer;
42
43
44     /* ----- TASK 2 ----- */
45
46     init_fcc(pos, N_cells, a_eq); // initialize fcc lattice
47     add_noise( N_atoms, 3, pos, noise_amplitude ); // adds random noise to pos
48     set_zero( N_atoms, 3, momentum); // set momentum to 0
49     get_forces_AL( forces, pos, a_eq*N_cells, N_atoms); //initial cond forces
50
51     for (int i=0; i<N_timesteps; i++){
52         /*
53          The loop over the timesteps first takes a timestep according to the
54          Verlet algorithm, then calculates the energies and temeperature.
55          */
56         timestep_Verlet (N_atoms, pos, momentum, forces, m_Al, dt, a_eq*N_cells);
57
58         E_kin =get_kin_energy(N_atoms, momentum, m_Al );
59         E_tot[i] =E_kin + get_energy_AL(pos, a_eq*N_cells, N_atoms);
60
61         /*  $3N \cdot kB \cdot T/2 = 1/(2m) \cdot \sum_{i=1}^N p_i^2 = p_{sq}/(2m)$  */
62         temperature[i] = E_kin * 2/(3*N_atoms*kB);
63     }
64
65     /* Write tempertaure to file */
66     char file_name[100];
67     sprintf(file_name, "../data/temperature_dt-%0.0e_Task2.tsv", dt);
68     file_pointer = fopen(file_name, "w");
69     for (int i=0; i<N_timesteps; i++){
70         t = i*dt; // time at step i
71         fprintf(file_pointer, "%.4f \t %.8f \n", t, temperature[i]);
72     }
73     fclose(file_pointer);
74
75     /* Write total energy to file */
76     sprintf(file_name, "../data/total_energy_dt-%0.0e_Task2.tsv", dt);
77     file_pointer = fopen(file_name, "w");
78     for (int i=0; i<N_timesteps; i++){
79         t = i*dt; // time at step i
80         fprintf(file_pointer, "%.4f \t %.8f \n", t, E_tot[i]);
81     }
82     fclose(file_pointer);
83
84     free(pos); pos = NULL;
85     free(momentum); momentum = NULL;
86     free(forces); forces = NULL;
87     free(temperature); temperature = NULL;
88     free(E_tot); E_tot = NULL;
89     return 0;
90 }

```

A.3 Temperature and pressure equilibration for tasks 3-7 : main.T3.c

```

1 /*
2 MD_main.c
3
4 Created by Anders Lindman on 2013-10-31.

```

```

5  */
6
7  #include <stdio.h>
8  #include <math.h>
9  #include <stdlib.h>
10 #include <time.h>
11
12 #include "initfcc.h"
13 #include "alpotential.h"
14 #include "funcs.h"
15
16 #define N_cells 4
17 /* define constants in atomic units: eV, , ps, K */
18 #define AMU 1.0364e-4
19 #define degC_to_K 273.15
20 #define bar 6.2415e-07
21 #define kB 8.61733e-5
22
23 /* Main program */
24 int main()
25 {
26     char file_name[100];
27
28     int N_atoms = 4*N_cells*N_cells*N_cells;
29     double m_Al = 27*AMU;
30     /*
31      Values of Young's and shear modulus, Y and G resp., taken from
32      Physics Handbook, table T 1.1. Bulk modulus then calculated as
33      B = Y*G / (9*G - 3*Y) [F 1.15, Physics Handbook]
34      kappa = 1/B
35      */
36     double kappa_Al = 100/(6.6444e+05 * bar); // STRANGE FACTOR 100 OFF !!!
37     double a_eq = 4.03;
38     double cell_length = a_eq*N_cells;
39     double inv_volume = pow(N_cells*cell_length, -3);
40     double noise_amplitude = 6.5e-2 * a_eq;
41
42     double T_final_C= 700;
43     int nRuns = 2; //2 if melt, 1 otherwise
44     double T_melt_C = 900;
45
46     double P_final_bar= 1;
47
48     double T_eq;
49     double P_eq = P_final_bar*bar;
50     double dt = 5e-3;
51     double tau_T = 100*dt;
52     double tau_P = 100*dt;
53     //double t_Teq= 10*tau_T; //equilibration times
54     double t_eq= 15*tau_P; //equilibration times
55     int N_timesteps = t_eq/dt;
56
57     double alpha_T, alpha_P,alpha_P_cube_root;
58     double t, E_kin, virial;
59
60
61     double (*pos)[3] = malloc(sizeof(double[N_atoms][3]));
62     double (*momentum)[3] = malloc(sizeof(double[N_atoms][3]));
63     double (*forces)[3] = malloc(sizeof(double[N_atoms][3]));
64     double *temperature = malloc(sizeof(double[N_timesteps]));
65     double *pressure = malloc(sizeof(double[N_timesteps]));
66
67
68     FILE *file_pointer;
69
70     /* ----- TASK 3 ----- */
71
72
73     init_fcc(pos, N_cells, a_eq); // initialize fcc lattice
74     add_noise( N_atoms, 3, pos, noise_amplitude ); // add random noise to pos
75     set_zero( N_atoms, 3, momentum); // set momentum to 0
76     get_forces_AL( forces, pos, cell_length, N_atoms); //initial cond forces
77
78     /*
79     for (int i=0; i<N_timesteps_T_eq; i++){
80         //
81         The loop over the timesteps first takes a timestep according to the
82         Verlet algorithm, then calculates the energies and temeperature.
83         //
84         timestep_Verlet(N_atoms, pos, momentum, forces, m_Al, dt, cell_length);
85
86         E_kin = get_kin_energy(N_atoms, momentum, m_Al );
87         virial = get_virial_AL(pos, cell_length, N_atoms);
88
89         // PV = NkT + virial
90         pressure[i] = inv_volume * (1.5*E_kin + virial);
91         // 3N*kB*T/2 = 1/(2m) * \sum_{i=1}^N p_i^2 = p_sq/(2m)
92         temperature[i] = E_kin * 1/(1.5*N_atoms*kB);
93
94
95         alpha_T = 1 + 2*dt*(T_eq - temperature[i]) / (tau_T * temperature[i]);

```

```

96     scale_mat(N_atoms, 3, momentum, sqrt(alpha_T));
97     temperature[i]*=alpha_T;
98 }
99 */
100
101
102 for (int irun=0; irun < nRuns; irun++){// last run: final, irun = 0
103     if (irun == nRuns - 1){ // final run
104         T_eq = T_final_C + degC_to_K;
105     }else{
106         T_eq = T_melt_C + degC_to_K;
107     }
108     for (int i=0; i<N_timesteps; i++){
109         /*
110          The loop over the timesteps first takes a timestep according to the
111          Verlet algorithm, then calculates the energies and temeperature.
112          */
113         timestep_Verlet(N_atoms, pos, momentum, forces, m_Al, dt, cell_length);
114
115
116         E_kin = get_kin_energy(N_atoms, momentum, m_Al );
117         virial = get_virial_AL(pos, cell_length, N_atoms);
118
119         /*  $3N \cdot k_B \cdot T/2 = 1/(2m) \cdot \sum_{i=1}^N p_i^2 = p\_sq/(2m)$  */
120         temperature[i] = E_kin * 1/(1.5*N_atoms*kB);
121         /*  $PV = NkT + \text{virial}$  */
122         pressure[i] = inv_volume * (1.5*E_kin + virial);
123
124         /* Equilibrate temperature by scaling momentum by a factor sqrt(alpha_T).
125            N.B. It is equally valid to scale the momentum instead of the velocity←
126            since they only differ by a constant factor m.
127         */
128         alpha_T = 1 + 2*dt*(T_eq - temperature[i]) / (tau_T * temperature[i]);
129         scale_mat(N_atoms, 3, momentum, sqrt(alpha_T));
130
131         // Equilibrate pressure by scaling the posistions by a factor of alpha_P←
132         //  $^{(1/3)}$ 
133
134         alpha_P = 1 - kappa_Al* dt*(P_eq - pressure[i])/tau_P;
135         alpha_P_cube_root = pow(alpha_P, 1.0/3.0);
136         scale_mat(N_atoms, 3, pos, alpha_P_cube_root);
137
138         cell_length*=alpha_P_cube_root;
139         inv_volume*=1/alpha_P;
140
141         temperature[i]*=alpha_T;
142         pressure[i]*=alpha_P;
143     }
144 }
145
146 /* Write tempertaure to file */
147 sprintf(file_name, "../data/temp-%d_pres-%d_Task3.tsv",
148         (int) T_final_C, (int) P_final_bar);
149 file_pointer = fopen(file_name, "w");
150 for (int i=0; i<N_timesteps; i++){
151     t = i*dt; // time at step i
152     fprintf(file_pointer, "%.4f \t %.8f \t %.8f \n",
153             t, temperature[i], pressure[i]);
154 }
155 fclose(file_pointer);
156
157 /* Write phase space coordinates to file */
158 sprintf(file_name, "../data/phase-space-temp-%d_pres-%d.tsv",
159         (int) T_final_C, (int) P_final_bar);
160 file_pointer = fopen(file_name, "w");
161 for (int i=0; i<N_atoms; i++){
162     for (int j=0; j<3; j++){
163         fprintf(file_pointer, " %.16e \t", pos[i][j]);
164     }
165     for (int j=0; j<3; j++){
166         fprintf(file_pointer, " %.16e \t", momentum[i][j]);
167     }
168     fprintf(file_pointer, "\n");
169 }
170 fclose(file_pointer);
171
172 /* save equilibrated position and momentum as a binary file */
173 sprintf(file_name, "../data/INIDATA-temp-%d_pres-%d.bin",
174         (int) T_final_C, (int) P_final_bar);
175 file_pointer = fopen(file_name, "wb");
176 fwrite(pos, sizeof(double), 3*N_atoms, file_pointer);
177 fwrite(momentum, sizeof(double), 3*N_atoms, file_pointer);
178 fwrite(&cell_length, sizeof(double), 1, file_pointer);
179 fclose(file_pointer);
180
181
182 /*
183 printf("T=%0.2f\tP=%0.2e\n",
184         temperature[N_timesteps-1], pressure[N_timesteps-1]);

```



```

185  */
186
187  free(pos); pos = NULL;
188  free(momentum); momentum = NULL;
189  free(forces); forces = NULL;
190  free(temperature); temperature = NULL;
191  free(pressure); pressure = NULL;
192  //free(volume); volume = NULL;
193  return 0;
194  }

```

A.4 Production runs for tasks 3-7 : main_Prod.c

```

1  /*
2  MD_main.c
3
4  Created by Anders Lindman on 2013-10-31.
5  */
6
7  #include <stdio.h>
8  #include <math.h>
9  #include <stdlib.h>
10 #include <time.h>
11
12 #include "initfcc.h"
13 #include "alpotential.h"
14 #include "funcs.h"
15
16 #define N_cells 4
17 /* define constants in atomic units: eV, , ps, K */
18 #define AMU 1.0364e-4
19 #define degC_to_K 273.15
20 #define bar 6.2415e-07
21 #define kB 8.61733e-5
22
23 /* Main program */
24 int main()
25 {
26     char file_name[100];
27
28     int N_atoms = 4*N_cells*N_cells*N_cells;
29     double m_Al = 27*AMU;
30     /*
31      Values of Young's and shear modulus, Y and G resp., taken from
32      Physics Handbook, table T 1.1. Bulk modulus then calculated as
33      B = Y*G / (9*G - 3*Y) [F 1.15, Physics Handbook]
34      kappa = 1/B
35      */
36     // double kappa_Al = 100/(6.6444e+05 * bar); // STRANGE FACTOR 100 OFF !!!
37     double cell_length = 0;
38     double inv_volume;
39
40
41     double T_eq_C = 500;
42     double P_eq_bar = 1;
43     // double T_eq = T_eq_C + degC_to_K;
44     // double P_eq = P_eq_bar*bar;
45     double dt = 5e-4; // higher res for spectral function
46     double t_end = 5;
47     // double tau_T = 100*dt;
48     // double tau_P = 100*dt;
49
50     int N_timesteps = t_end/dt;
51
52     int N_between_steps = 1;
53     int N_save_timesteps = N_timesteps / N_between_steps; //for the displacements
54     int N_save_atoms = 5;
55
56     // double alpha_T, alpha_P,alpha_P_cube_root;
57     double t, E_kin, virial;
58
59     double (*pos)[3] = malloc(sizeof(double[N_atoms][3]));
60     double (*pos_0)[3] = malloc(sizeof(double[N_atoms][3]));
61     double (*momentum)[3] = malloc(sizeof(double[N_atoms][3]));
62     double (*forces)[3] = malloc(sizeof(double[N_atoms][3]));
63     double (*displacements)[N_save_atoms] =
64         malloc(sizeof(double[N_save_timesteps][N_save_atoms]));
65     double (*pos_all)[N_atoms][3] =
66         malloc(sizeof(double[N_save_timesteps][N_atoms][3]));
67     double (*vel_all)[N_atoms][3] =
68         malloc(sizeof(double[N_save_timesteps][N_atoms][3]));
69     double *temperature = malloc(sizeof(double[N_timesteps]));
70     double *pressure = malloc(sizeof(double[N_timesteps]));
71     double *msd = malloc(sizeof(double[N_save_timesteps]));
72     double *vel_corr = malloc(sizeof(double[N_save_timesteps]));
73     double *pow_spec = malloc(sizeof(double[N_save_timesteps]));

```

```

74 double *freq          = malloc(sizeof(double[N_save_timesteps]));
75
76 for (int i = 0; i<N_save_timesteps; i++){
77     msd[i] = 0;
78     pow_spec[i] = 0;
79     vel_corr[i] = 0;
80 }
81 FILE *file_pointer;
82
83 /* ----- TASK 3 ----- */
84
85 // read positions, momenta and cell_length
86 sprintf(file_name, "../data/INIDATA_temp-%d_pres-%d.bin",
87         (int) T_eq_C, (int) P_eq_bar);
88 file_pointer = fopen(file_name, "rb");
89 fread(pos, sizeof(double), 3*N_atoms, file_pointer);
90 fread(momentum, sizeof(double), 3*N_atoms, file_pointer);
91 fread(&cell_length, sizeof(double), 1, file_pointer);
92 fclose(file_pointer);
93
94 for (int i=0; i<N_atoms; i++){
95     for (int j=0; j<3; j++){
96         pos_0[i][j]=pos[i][j];
97     }
98 }
99 inv_volume = pow(N_cells*cell_length, -3);
100 get_forces_AL( forces, pos, cell_length, N_atoms); //initial cond forces
101
102 printf("Initialized. Starting with Verlet timestepping.\n");
103 for (int i=0; i<N_timesteps; i++){
104     /*
105      * The loop over the timesteps first takes a timestep according to the
106      * Verlet algorithm, then calculates the energies and temeperature.
107      */
108     timestep_Verlet(N_atoms, pos, momentum, forces, m_AL, dt, cell_length);
109
110     E_kin = get_kin_energy(N_atoms, momentum, m_AL );
111     virial = get_virial_AL(pos, cell_length, N_atoms);
112
113     /* PV = NkT + virial */
114     pressure[i] = inv_volume * (1.5*E_kin + virial);
115     /* 3N*kB*T/2 = 1/(2m) * \sum_{i=1}^N p_i^2 = p_sq/(2m) */
116     temperature[i] = E_kin * 1/(1.5*N_atoms*kB);
117
118     if (i % N_between_steps == 0){
119         int k = i/N_between_steps; // number of saved timesteps so far
120         get_displacements(N_save_atoms, pos, pos_0, displacements[k]);
121         copy_mat(N_atoms, 3, pos, pos_all[k]);
122
123         copy_mat(N_atoms, 3, momentum, vel_all[k]);
124         scale_mat(N_atoms, 3, vel_all[k], 1/m_AL);
125     }
126     if ((i*10) % N_timesteps == 0){
127         printf("done %d %% of Verlet timestepping\n", (i*10)/N_timesteps);
128     }
129 }
130 printf("calculating MSD\n");
131 get_MSD(N_atoms, N_save_timesteps, pos_all, msd);
132
133 printf("calculating velocity correlation\n");
134 get_vel_corr(N_atoms, N_save_timesteps, vel_all, vel_corr);
135
136 printf("calculating power spectrum\n");
137 get_powerspectrum(N_atoms, N_save_timesteps, vel_all, pow_spec);
138 fft_freq(freq, dt, N_save_timesteps);
139
140
141
142 printf("writing to file\n");
143 /* Write tempertaure to file */
144
145 sprintf(file_name, "../data/temp-%d_pres-%d_Prod-test.tsv",
146         (int) T_eq_C, (int) P_eq_bar);
147 file_pointer = fopen(file_name, "w");
148 for (int i=0; i<N_timesteps; i++){
149     t = i*dt; // time at step i
150     fprintf(file_pointer, "%.4f \t %.8f \t %.8f \n",
151             t, temperature[i], pressure[i]);
152 }
153 fclose(file_pointer);
154
155 /* Write displacements to file */
156 sprintf(file_name, "../data/temp-%d_pres-%d_displacements.tsv",
157         (int) T_eq_C, (int) P_eq_bar);
158 file_pointer = fopen(file_name, "w");
159 for (int i=0; i<N_save_timesteps; i++){
160     t = i*dt*N_between_steps; // time at step i
161     fprintf(file_pointer, "%.4f", t);
162     for (int j=0; j<N_save_atoms; j++){
163         fprintf(file_pointer, "\t %.8f", displacements[i][j]);
164     }

```

```

165     fprintf(file_pointer, "\n");
166 }
167 fclose(file_pointer);
168
169 /* Write MSD to file */
170 sprintf(file_name, "../data/temp-%d_pres-%d_dynamicProperties.tsv",
171         (int) T_eq_C, (int) P_eq_bar);
172 file_pointer = fopen(file_name, "w");
173 // write header
174 fprintf(file_pointer, "%% t[ps] \t MSD[A^2] \t vel_corr [A/ps]^2 \n");
175 for (int i=0; i<N_save_timesteps; i++){
176     t = i*dt*N_between_steps; // time at step i
177     fprintf(file_pointer, "%.4f \t %.8f \t %.8f \n", t, msd[i], vel_corr[i]);
178 }
179 fclose(file_pointer);
180
181 sprintf(file_name, "../data/temp-%d_pres-%d_power-spectrum.tsv",
182         (int) T_eq_C, (int) P_eq_bar);
183 file_pointer = fopen(file_name, "w");
184 // write header
185 fprintf(file_pointer, "%% f[1/ps] \t P[A/ps]^2 \n");
186 for (int i=0; i<N_save_timesteps/2; i++){ // only print from f=0 to f_crit
187     fprintf(file_pointer, "%.4f \t %.8f \n", freq[i], pow_spec[i]);
188 }
189 fclose(file_pointer);
190
191 free(pos);          pos = NULL;
192 free(pos_0);        pos_0 = NULL;
193 free(momentum);     momentum = NULL;
194 free(forces);        forces = NULL;
195 free(temperature);  temperature = NULL;
196 free(pressure);     pressure = NULL;
197 free(displacements); displacements = NULL;
198 free(pos_all);      pos_all = NULL;
199 free(vel_all);      vel_all = NULL;
200 free(msd);          msd = NULL;
201 free(vel_corr);     vel_corr = NULL;
202 free(pow_spec);     pow_spec = NULL;
203 free(freq);         freq = NULL;
204 return 0;
205 }

```

A.5 Production runs for tasks 3-7 : main_Prod.c

```

1  /*
2  MD_main.c
3
4  Created by Anders Lindman on 2013-10-31.
5  */
6
7  #include <stdio.h>
8  #include <math.h>
9  #include <stdlib.h>
10 #include <time.h>
11
12 #include "initfcc.h"
13 #include "alpotential.h"
14 #include "funcs.h"
15
16 #define N_cells 4
17 /* define constants in atomic units: eV, , ps, K */
18 #define AMU 1.0364e-4
19 #define degC_to_K 273.15
20 #define bar 6.2415e-07
21 #define kB 8.61733e-5
22
23 /* Main program */
24 int main()
25 {
26     char file_name[100];
27
28     int N_atoms = 4*N_cells*N_cells*N_cells;
29     double m_Al = 27*AMU;
30     /*
31      Values of Young's and shear modulus, Y and G resp., taken from
32      Physics Handbook, table T 1.1. Bulk modulus then calculated as
33      B = Y*G / (9*G - 3*Y) [F 1.15, Physics Handbook]
34      kappa = 1/B
35      */
36     // double kappa_Al = 100/(6.6444e+05 * bar); // STRANGE FACTOR 100 OFF !!!
37     double cell_length = 0;
38     double inv_volume;
39
40
41     double T_eq_C = 500;
42     double P_eq_bar = 1;

```

```

43 // double T_eq      = T_eq_C + degC_to_K;
44 // double P_eq      = P_eq_bar*bar;
45 double dt          = 5e-4; // higher res for spectral function
46 double t_end       = 5;
47 // double tau_T     = 100*dt;
48 // double tau_P     = 100*dt;
49
50 int N_timesteps = t_end/dt;
51
52 int N_between_steps = 1;
53 int N_save_timesteps = N_timesteps / N_between_steps; //for the displacements
54 int N_save_atoms = 5;
55
56 // double alpha_T, alpha_P, alpha_P_cube_root;
57 double t, E_kin, virial;
58
59 double (*pos)[3]      = malloc(sizeof(double)[N_atoms][3]);
60 double (*pos_0)[3]    = malloc(sizeof(double)[N_atoms][3]);
61 double (*momentum)[3] = malloc(sizeof(double)[N_atoms][3]);
62 double (*forces)[3]   = malloc(sizeof(double)[N_atoms][3]);
63 double (*displacements)[N_save_atoms] =
64     malloc(sizeof(double)[N_save_timesteps][N_save_atoms]);
65 double (*pos_all)[N_atoms][3] =
66     malloc(sizeof(double)[N_save_timesteps][N_atoms][3]);
67 double (*vel_all)[N_atoms][3] =
68     malloc(sizeof(double)[N_save_timesteps][N_atoms][3]);
69 double *temperature = malloc(sizeof(double)[N_timesteps]);
70 double *pressure     = malloc(sizeof(double)[N_timesteps]);
71 double *msd          = malloc(sizeof(double)[N_save_timesteps]);
72 double *vel_corr     = malloc(sizeof(double)[N_save_timesteps]);
73 double *pow_spec     = malloc(sizeof(double)[N_save_timesteps]);
74 double *freq         = malloc(sizeof(double)[N_save_timesteps]);
75
76 for (int i = 0; i < N_save_timesteps; i++){
77     msd[i] = 0;
78     pow_spec[i] = 0;
79     vel_corr[i] = 0;
80 }
81 FILE *file_pointer;
82
83 /* ----- TASK 3 ----- */
84
85 // read positions, momenta and cell_length
86 sprintf(file_name, "../data/INIDATA_temp-%d_pres-%d.bin",
87         (int) T_eq_C, (int) P_eq_bar);
88 file_pointer = fopen(file_name, "rb");
89 fread(pos, sizeof(double), 3*N_atoms, file_pointer);
90 fread(momentum, sizeof(double), 3*N_atoms, file_pointer);
91 fread(&cell_length, sizeof(double), 1, file_pointer);
92 fclose(file_pointer);
93
94 for (int i=0; i<N_atoms; i++){
95     for (int j=0; j<3; j++){
96         pos_0[i][j]=pos[i][j];
97     }
98 }
99 inv_volume = pow(N_cells*cell_length, -3);
100 get_forces_AL( forces, pos, cell_length, N_atoms); //initial cond forces
101
102 printf("Initialized. Starting with Verlet timestepping.\n");
103 for (int i=0; i<N_timesteps; i++){
104     /*
105      The loop over the timesteps first takes a timestep according to the
106      Verlet algorithm, then calculates the energies and temeperature.
107     */
108     timestep_Verlet(N_atoms, pos, momentum, forces, m_Al, dt, cell_length);
109
110     E_kin = get_kin_energy(N_atoms, momentum, m_Al );
111     virial = get_virial_AL(pos, cell_length, N_atoms);
112
113     /* PV = NkT + virial */
114     pressure[i] = inv_volume * (1.5*E_kin + virial);
115     /* 3N*kB*T/2 = 1/(2m) * \sum_{i=1}^N p_i^2 = p_sq/(2m) */
116     temperature[i] = E_kin * 1/(1.5*N_atoms*kB);
117
118     if (i % N_between_steps == 0){
119         int k = i/N_between_steps; // number of saved timesteps so far
120         get_displacements (N_save_atoms, pos, pos_0, displacements[k]);
121         copy_mat(N_atoms, 3, pos, pos_all[k]);
122
123         copy_mat(N_atoms, 3, momentum, vel_all[k]);
124         scale_mat(N_atoms, 3, vel_all[k], 1/m_Al);
125     }
126     if ((i*10) % N_timesteps == 0){
127         printf("done %d0 %% of Verlet timestepping\n", (i*10)/N_timesteps);
128     }
129 }
130 printf("calculating MSD\n");
131 get_MSD(N_atoms, N_save_timesteps, pos_all, msd);
132
133 printf("calculating velocity correlation\n");

```

```

134 get_vel_corr(N_atoms, N_save_timesteps, vel_all, vel_corr);
135
136 printf("calculating power spectrum\n");
137 get_powerspectrum(N_atoms, N_save_timesteps, vel_all, pow_spec);
138 fft_freq(freq, dt, N_save_timesteps);
139
140
141
142 printf("writing to file\n");
143 /* Write tempertaure to file */
144
145 sprintf(file_name, "../data/temp-%d_pres-%d_Prod-test.tsv",
146         (int) T_eq_C, (int) P_eq_bar);
147 file_pointer = fopen(file_name, "w");
148 for (int i=0; i<N_timesteps; i++){
149     t = i*dt; // time at step i
150     fprintf(file_pointer, "%.4f \t %.8f \t %.8f \n",
151             t, temperature[i], pressure[i]);
152 }
153 fclose(file_pointer);
154
155 /* Write displacements to file */
156 sprintf(file_name, "../data/temp-%d_pres-%d_displacements.tsv",
157         (int) T_eq_C, (int) P_eq_bar);
158 file_pointer = fopen(file_name, "w");
159 for (int i=0; i<N_save_timesteps; i++){
160     t = i*dt*N_between_steps; // time at step i
161     fprintf(file_pointer, "%.4f", t);
162     for (int j=0; j<N_save_atoms; j++){
163         fprintf(file_pointer, "\t %.8f", displacements[i][j]);
164     }
165     fprintf(file_pointer, "\n");
166 }
167 fclose(file_pointer);
168
169 /* Write MSD to file */
170 sprintf(file_name, "../data/temp-%d_pres-%d_dynamicProperties.tsv",
171         (int) T_eq_C, (int) P_eq_bar);
172 file_pointer = fopen(file_name, "w");
173 // write header
174 fprintf(file_pointer, "%s t[ps] \t MSD[A^2] \t vel_corr [A/ps]^2 \n");
175 for (int i=0; i<N_save_timesteps; i++){
176     t = i*dt*N_between_steps; // time at step i
177     fprintf(file_pointer, "%.4f \t %.8f \t %.8f \n", t, msd[i], vel_corr[i]);
178 }
179 fclose(file_pointer);
180
181 sprintf(file_name, "../data/temp-%d_pres-%d_power-spectrum.tsv",
182         (int) T_eq_C, (int) P_eq_bar);
183 file_pointer = fopen(file_name, "w");
184 // write header
185 fprintf(file_pointer, "%s f[1/ps] \t P[A/ps]^2 \n");
186 for (int i=0; i<N_save_timesteps/2; i++){ // only print from f=0 to f_crit
187     fprintf(file_pointer, "%.4f \t %.8f \n", freq[i], pow_spec[i]);
188 }
189 fclose(file_pointer);
190
191 free(pos);          pos = NULL;
192 free(pos_0);        pos_0 = NULL;
193 free(momentum);     momentum = NULL;
194 free(forces);        forces = NULL;
195 free(temperature);   temperature = NULL;
196 free(pressure);      pressure = NULL;
197 free(displacements); displacements = NULL;
198 free(pos_all);       pos_all = NULL;
199 free(vel_all);       vel_all = NULL;
200 free(msd);           msd = NULL;
201 free(vel_corr);      vel_corr = NULL;
202 free(pow_spec);      pow_spec = NULL;
203 free(freq);          freq = NULL;
204 return 0;
205 }

```

A.6 Misc functions : funcs.c

```

1 #include "funcs.h"
2
3 void add_noise(int M, int N, double mat[M][N], double noise_amplitude )
4 {
5     const gsl_rng_type *T; /* static info about rngs */
6     gsl_rng *q; /* rng instance */
7     gsl_rng_env_setup (); /* setup the rngs */
8     T = gsl_rng_default; /* specify default rng */
9     q = gsl_rng_alloc(T); /* allocate default rng */
10    gsl_rng_set(q, time(NULL)); /* Initialize rng */
11 }

```

```

12 for (int i=0; i<N; i++){
13     for (int j=0; j<M; j++){
14         // adds uniformly distributed random noise in range +/-`noise_amplitude`
15         mat[i][j] += noise_amplitude * (2*gsl_rng_uniform(q)-1);
16     }
17 }
18 gsl_rng_free(q); /* deallocate rng */
19 }
20
21 void timestep_Verlet ( int N_atoms, double (*pos)[3], double (*momentum)[3],
22                     double (*forces)[3], double m, double dt,
23                     double cell_length){
24     for (int i = 0; i < N_atoms; i++) {
25         for (int j = 0; j < 3; j++) {
26             /* p(t+dt/2) */
27             momentum[i][j] += dt * 0.5 * forces[i][j];
28             /* q(t+dt) */
29             pos[i][j] += dt * momentum[i][j] / m;
30         }
31     }
32     /* F(t+dt) */
33     get_forces_AL( forces, pos, cell_length, N_atoms);
34     for (int i = 0; i < N_atoms; i++) {
35         for (int j = 0; j < 3; j++) {
36             /* p(t+dt/2) */
37             momentum[i][j] += dt * 0.5 * forces[i][j];
38         }
39     }
40 }
41
42 double get_kin_energy ( int N_atoms, double (*momentum)[3], double m ) {
43     double p_sq=0; // momentum squared
44     for (int i = 0; i < N_atoms; i++) {
45         for (int j = 0; j < 3; j++) {
46             p_sq += momentum[i][j] * momentum[i][j];
47         }
48     }
49     return p_sq / (2*m);
50 }
51
52 void get_displacements ( int N_atoms, double (*positions)[3],
53                       double (*initial_positions)[3], double disp[]) {
54     for (int i = 0; i < N_atoms; i++) {
55         for (int j = 0; j < 3; j++) {
56             disp[i] += (positions[i][j] - initial_positions[i][j])
57                       * (positions[i][j] - initial_positions[i][j]);
58         }
59         disp[i] = sqrt(disp[i]);
60     }
61 }
62
63
64 void get_MSD ( int N_atoms, int N_times, double all_pos[N_times][N_atoms][3],
65              double MSD[N_times]) {
66     /* all_pos = positions of all particles at all (saved) times */
67     /* outer time index it starts at outer it = 1, since MSD[0] = 0 */
68     for (int it = 1; it < N_times; it++) { //
69         for (int jt = 0; jt < N_times-it; jt++) { // summed time index
70             for (int kn = 0; kn < N_atoms; kn++) { // particle index
71                 for (int kd = 0; kd < 3; kd++) { // three dimensions
72                     MSD[it] += (all_pos[it+jt][kn][kd] - all_pos[jt][kn][kd])
73                             * (all_pos[it+jt][kn][kd] - all_pos[jt][kn][kd]);
74                 }
75             }
76         }
77         MSD[it] *= 1/( (double)N_atoms * (N_times-it));
78     }
79 }
80
81 void get_vel_corr ( int N_atoms, int N_times, double all_vel[N_times][N_atoms][3],
82                  double vel_corr[N_times]) {
83     /* all_vel = velocity of all particles at all (saved) times */
84     for (int it = 0; it < N_times; it++) { //
85         for (int jt = 0; jt < N_times-it; jt++) { // summed time index
86             for (int kn = 0; kn < N_atoms; kn++) { // particle index
87                 for (int kd = 0; kd < 3; kd++) { // three dimensions
88                     vel_corr[it] += (all_vel[it+jt][kn][kd] * all_vel[jt][kn][kd]);
89                 }
90             }
91         }
92         vel_corr[it] *= 1/( (double)N_atoms * (N_times-it));
93     }
94 }
95
96 void get_powerspectrum ( int N_atoms, int N_times, double all_vel[N_times][N_atoms][3],
97                       double pow_spec[N_times]) {
98     /* all_vel = velocity of all particles at all (saved) times */
99     double vel_component[N_times]; // "all_vel[:,i][j]"
100    double pow_spec_component[N_times];

```

```

101 double normalization_factor = 1/( (double)N_atoms * (N_times));
102 for (int kn = 0; kn < N_atoms; kn++) { // particle index
103     for (int kd = 0; kd < 3; kd++) { // three dimensions
104         for (int it = 0; it < N_times; it++) { //
105             vel_component[it] = all_vel[it][kn][kd];
106         }
107         powerspectrum(vel_component, pow_spec_component, N_times);
108         for (int iw = 0; iw < N_times; iw++) { // for all frequencies
109             pow_spec[iw] += pow_spec_component[iw];
110         }
111     }
112 }
113 for (int iw = 0; iw < N_times; iw++) { // for all frequencies
114     pow_spec[iw] *= normalization_factor;
115 }
116 }
117
118
119 void copy_mat (int M, int N, double mat_from[M][N], double mat_to[M][N]){
120     /* Copies matrix `mat_from` to `mat_to` */
121     for (int i = 0; i < M; i++) {
122         for (int j = 0; j < N; j++) {
123             mat_to[i][j] = mat_from[i][j];
124         }
125     }
126 }
127
128
129 void set_zero (int M, int N, double mat[M][N]){
130     /* Sets the matrix `mat` to zero */
131     for (int i = 0; i < M; i++) {
132         for (int j = 0; j < N; j++) {
133             mat[i][j] = 0;
134         }
135     }
136 }
137
138 void scale_mat (int M, int N, double mat[M][N], double alpha){
139     /* Scales the matrix `mat` by factor `alpha` */
140     for (int i = 0; i < M; i++) {
141         for (int j = 0; j < N; j++) {
142             mat[i][j] *= alpha;
143         }
144     }
145 }

```

B Auxiliary

B.1 Makefile

```

1
2 CC = gcc
3 CFLAGS = -O3 -Wall -Wno-unused-result
4
5 LIBS = -lm -lgsl -lgslcblas
6
7 HEADERS = initfcc.h alpotential.h funcs.h fft_func.h
8 OBJECTS = initfcc.o alpotential.o funcs.o fft_func.o
9
10
11 %.o: %.c $(HEADERS)
12     $(CC) -c -o $@ $< $(CFLAGS)
13
14 all: Task1 Task2 Task3 main_Prod.c
15
16 Task1: $(OBJECTS) main_T1.c
17     $(CC) -o $@ $^ $(CFLAGS) $(LIBS)
18
19 Task2: $(OBJECTS) main_T2.c
20     $(CC) -o $@ $^ $(CFLAGS) $(LIBS)
21
22 Task3: $(OBJECTS) main_T3.c
23     $(CC) -o $@ $^ $(CFLAGS) $(LIBS)
24
25 Prod: $(OBJECTS) main_Prod.c
26     $(CC) -o $@ $^ $(CFLAGS) $(LIBS)
27
28 # $(PROGRAMS): $(OBJECTS) main_T1.c
29 #     $(CC) -o $@ $^ $(CFLAGS) $(LIBS)
30
31 clean:
32     rm -f *.o
33     touch *.c

```

C Matlab scripts

C.1 Analysis scripts for tasks 3-7: A1_energies.m

```
1 tmp = matlab.desktop.editor.getActive;
2 cd(fileparts(tmp.Filename));
3 set(0,'DefaultFigureWindowStyle','docked');
4 GRAY = 0.7*[0.9 0.9 1];
5
6 %% task 1
7 clc
8
9 energy_data = load('../data/lattice_energies.tsv');
10 a0 = energy_data(:,1);
11 v0 = a0.^3;
12
13 energy = energy_data(:,2);
14 figure(1);clf;
15 plot(v0,energy, 'xk');
16
17 start_v = 64;
18 end_v = 68;
19 indToInclude = (v0 > start_v) & (v0 < end_v);
20 p = polyfit(v0(indToInclude),energy(indToInclude),2);
21 hold on;
22
23 vvec = linspace(start_v, end_v);
24 plot(vvec, p(1)*vvec.^2 + p(2)*vvec + p(3), '-r');
25 xlim([64 68]);
26
27 v_min = -p(2)/(2*p(1));
28 a_min = v_min^(1/3);
29
30 ax = gca;
31 ax.YLim = [-13.45 -13.42];
32 h1 = plot(v_min*[1 1], ax.YLim, '--k'); % plot vertical line at v_min
33
34
35 ax.YTick = (-13.45:0.01:-13.42);
36 ylabel('$E_{\rm pot}$ [eV/unit cell]');
37 xlabel('$a_0^3$ [\AA^3]');
38 legend('data', 'quadratic fit', ['$V_{\rm eq}$ \approx \, $' num2str(round(v_min↵
,2)) '\, \AA^3$'], ...
39 'location', 'southeast')
40 ImproveFigureCompPhys(gcf); h1.LineWidth = 2; setFigureSize(gcf);
41
42 %axis([63 68 ylim(1) 0]);
43 saveas(gcf, '../figures/potential_energy.eps', 'eps')
44
45
46 %% task 2
47 %clc;
48 clf;clear
49
50 dt=[1e-2,5e-3,2e-3,1e-3];
51 for i=1:4
52 T_data = load(sprintf('../data/temperature_dt-%0.0e_Task2.tsv',dt(i)));
53 E_data = load(sprintf('../data/total_energy_dt-%0.0e_Task2.tsv',dt(i)));
54 t = T_data(:,1);
55 T = T_data(:,2);
56 E = E_data(:,2);
57
58 t_eq=0.5;
59
60
61 fprintf('dt = %0.0e\n',dt(i));
62
63 T_avg=mean(T(t>t_eq));
64 T_std=std(T(t>t_eq));
65 fprintf('\tT = %0.2f +- %0.1f %%\n', T_avg, abs(T_std/T_avg)*100);
66
67 E_avg=mean(E(t>t_eq));
68 E_std=std(E(t>t_eq));
69 fprintf('\tE = %0.2f +- %0.1e %%\n', E_avg, abs(E_std/E_avg)*100);
70
71 figure(i);clf
72 plot(t, T)
73 yyaxis right
74 plot(t, E)
75 ylim(E_avg*(1+0.001*[1,-1]));
76 end
77
78
79 %% test production pressure and temp
80 clc; clf;
81 %clear
82
```



```

83
84
85 %data = load(sprintf('../data/temperature_dt-1e-02_Task3.tsv'));
86 %data = load('../data/temp-700_pres-1_Task3.tsv');
87 data = load('../data/temp-500_pres-1_Prod-test.tsv');
88 %data = load('../data/temp-700_pres-1_Prod-test.tsv');
89 bar = 6.2415e-07;
90
91 t = data(:,1);
92 T = data(:,2)-273.15;
93 P = data(:,3)/bar;
94
95
96 t_eq=0.5;
97
98
99 %fprintf('dt = %0.0e\n',dt(i));
100
101 T_avg=mean(T(t>t_eq));
102 T_std=std(T(t>t_eq));
103 fprintf('\tT = %0.2f +- %0.1f %%\n', T_avg, abs(T_std/T_avg)*100);
104
105 P_avg=mean(P(t>t_eq));
106 P_std=std(P(t>t_eq));
107 fprintf('\tP = %0.2f +- %0.1f %%\n', P_avg, abs(P_std/P_avg)*100);
108
109 yyaxis left
110 plot(t,T, 'color', GRAY),hold on
111 plot(t, cumsum(T)./(1:length(t))', '-k')
112 ylabel('$T \, [\circ \rm C]$')
113
114 ylim([400,800])
115
116
117 yyaxis right
118 plot(t,P),hold on
119 plot(t,cumsum(P)./(1:length(t))', '-k')
120
121
122 ylabel('$P \, [\rm bar]$')
123 ylim([-50,200])
124
125 xlabel('$t \, [\rm ps]$')
126
127 ImproveFigureCompPhys(gcf, 'linewidth', 3, 'LineColor', {'MYORANGE', GRAY, 'MYBLUE', GRAY});
128
129 %% determine displacements and MSD
130 temperatures = num2str([500;700]);
131 clc; clf;
132 figure(10); clf;
133 FILENAMES = strcat({'../data/temp-'}, temperatures, '_pres-1_displacements.tsv')↵
134 ;
135 FILENAMES_Dyn = strcat({'../data/temp-'}, temperatures, '_pres-1_↵
136 _dynamicProperties.tsv');
137 FILENAMES_Pow = strcat({'../data/temp-'}, temperatures, '_pres-1_power-spectrum.↵
138 tsv');
139 for iFile = 1:numel(FILENAMES)
140
141     figure(iFile); clf;
142     data = load(FILENAMES{iFile});
143     t = data(:,1);
144     dx = data(:,2:end);
145
146     plot(t, dx.^2); hold on;
147
148     data = load(FILENAMES_Dyn{iFile});
149     MSD = data(:,2);
150     vel_corr = data(:,3);
151     plot(t, MSD, 'k')
152
153     if iFile ==2 % liquid
154         tStart = 1;
155         D = MSD(t>tStart)./(6*t(t>tStart));
156         selfDiffusionCoeff = mean(D); % in  $\text{\AA}^2/\text{ps}$ 
157         plot(t, 6*t*selfDiffusionCoeff, ':');
158     end
159
160     leg = legend( strcat({'$n=$'}, num2str((1:size(dx,2))'))');
161     leg.Location='northwest';
162     xlabel('$t \, [\rm ps]$')
163     ylabel('$\Delta x^2 \, [\rm \AA^2]$')
164     if iFile ==1
165         ylim([0 1.0]);
166     else
167         ylim([0 200]);
168     end
169     ImproveFigureCompPhys(gcf);
170
171     figure(10)

```

```

170     plot(t, vel_corr/vel_corr(1)); hold on;
171     xlim([0 1])
172
173 end
174
175 % velocity correlation
176 figure(10);clf; figure(11);clf;
177 n_average_points = 1;%30;
178 for iFile = 1:numel(FILENAMES)
179     data = load(FILENAMES_Dyn{iFile});
180     t = data(:,1);
181     vel_corr = data(:,3);
182
183     data = load(FILENAMES_Pow{iFile});
184     freq = data(:,1);
185     pow_spec = data(:,2);
186
187     figure(10);
188     plot(t, vel_corr/vel_corr(1)); hold on;
189
190     dt = t(2)-t(1);
191     N_times = round(length(t)/2); % we have too bad statistics at later times.
192     deltaf = 1/(N_times * dt);
193     omegavec = 0:deltaf:(1/(2*dt));
194     %PhiHat = 2 * trapz(t(1:N_times), (vel_corr(1:N_times) * ones(size(omegavec)←
195         )) .* cos(t(1:N_times) * omegavec ), 1); %dimension 1
196     PhiHat = 1/2 * 1/N_times * 2 * sum( (vel_corr(1:N_times) * ones(size(←
197         omegavec))) .* cos(t(1:N_times) * omegavec ), 1); %dimension 1
198
199     figure(11);
200     plot(omegavec/(2*pi), PhiHat); hold on;
201     plot(freq, pow_spec, ':'); hold on;
202     if iFile ==2 % liquid
203         tStart = 1;
204         selfDiffusionCoeff_spectral = PhiHat(1)/6; % in  $\text{\AA}^2/\text{ps}$ 
205     end
206 end
207
208 disp([selfDiffusionCoeff selfDiffusionCoeff_spectral]);
209
210 figure(10)
211 xlim([0 1])
212 leg = legend(strcat({'$T='}, num2str([500;700]), '\,\'circ $C'));
213 leg.Location='northeast';
214 xlabel('$t$ [ps]')
215 ylabel('$\Phi(t)/\Phi(0)$')
216
217
218 figure(11)
219 leg = legend('$T= 500 \, \text{\AA}^2/\text{ps}$', '$T= 500 \, \text{\AA}^2/\text{ps}$', '$T= 700 \, \text{\AA}^2/\text{ps}$', '$T= 700 \, \text{\AA}^2/\text{ps}$');
220 xlim([0 30])
221 ylim([0 Inf])
222 ImproveFigureCompPhys('LineColor', {'r', 'MYRED', 'GERIBLUE', 'MYLIGHTBLUE'});
223 %%
224 clf;clf;
225
226
227 FILENAME = '../data/INIDATA_temp-700_pres-1.bin';
228 fID=fopen(FILENAME,'rb');
229 data1=fread(fID,[3,inf],'real*8').';
230 fclose(fID);
231
232
233 AMU = 1.0364e-4;
234 m_A1 = 27*AMU;
235 kB= 8.61733e-5;
236 N_atoms=4^4;
237
238 T=sum(sum(data1.^2,2),1) / (3*m_A1*N_atoms*kB)
239
240
241 data2=load('../data/phase-space_temp-500_pres-1.tsv');
242
243 T=sum(sum(data2(:,4:end).^2,2),1) / (3*m_A1*N_atoms*kB)

```

C.2 Improve figure appearance: ImproveFigureCompPhys.m

```

1 function ImproveFigureCompPhys(varargin)
2 %ImproveFigureCompPhys Improves the figures of supplied handles
3 % Input:
4 % - none (improve all figures) or handles to figures to improve
5 % - optional:
6 %     LineWidth int

```

```

7 % LineStyle column vector cell, e.g. {'-','--'}',
8 % LineColor column vector cell, e.g. {'k',[0 1 1], 'MYBLUE'}'
9 % colors: MYBLUE,MYORANGE,MYGREEN,MYPURPLE, MYYELLOW,
10 % MYLIGHTBLUE, MYRED
11 % Marker column vector cell, e.g. {'.', 'o', 'x'}'
12
13 % ImproveFigure was originally written by Adam Stahl, but has been heavily
14 % modified by Linnea Hesslow
15
16
17 %%% Handle inputs
18 % If no inputs or if the first argument is a string (a property rather than
19 % a handle), use all open figures
20 if nargin == 0 || ischar(varargin{1})
21 %Get all open figures
22 figHs = findobj('Type','figure');
23 nFigs = length(figHs);
24 else
25 % Check the supplied figure handles
26 figHs = varargin{1};
27 figHs = figHs(ishandle(figHs) == 1); %Keep only those handles that are ←
    proper graphics handles
28 nFigs = length(figHs);
29 end
30
31 % Define desired properties
32 titleSize = 24;
33 interpreter = 'latex';
34 lineWidth = 4;
35 axesWidth = 1.5;
36 labelSize = 22;
37 textSize = 20;
38 legTextSize = 18;
39 tickLabelSize = 18;
40 LineColor = {};
41 LineStyle = {};
42 Marker = {};
43
44 % define colors
45 co = [ 0 0.4470 0.7410
46 0.8500 0.3250 0.0980
47 0.9290 0.6940 0.1250
48 0.4940 0.1840 0.5560
49 0.4660 0.6740 0.1880
50 0.3010 0.7450 0.9330
51 0.6350 0.0780 0.1840 ];
52 colors = struct('MYBLUE', co(1,:),...
53 'MYORANGE', co(2,:),...
54 'MYYELLOW', co(3,:),...
55 'MYPURPLE', co(4,:),...
56 'MYGREEN', co(5,:),...
57 'MYLIGHTBLUE', co(6,:),...
58 'MYRED',co(7,:),...
59 'GERIBLUE', [0.3000 0.1500 0.7500],...
60 'GERIRED', [1.0000 0.2500 0.1500],...
61 'GERIYELLOW', [0.9000 0.7500 0.1000],...
62 'LIGHTGREEN', [0.4 0.85 0.4],...
63 'LINNEAGREEN', [7 184 4]/255);
64
65 % Loop through the supplied arguments and check for properties to set.
66 for i = 1:nargin
67 if ischar(varargin{i})
68     switch lower(varargin{i}) %Compare lower case strings
69         case 'linewidth'
70             lineWidth = varargin{i+1};
71         case 'linestyle'
72             LineStyle = varargin{i+1};
73         case 'linecolor'
74             LineColor = varargin{i+1};
75             for iLineColor = 1:numel(LineColor)
76                 if isfield(colors, LineColor{iLineColor})
77                     LineColor{iLineColor} = colors.(LineColor{iLineColor});
78             end
79         end
80         case 'marker'
81             Marker = varargin{i+1};
82     end
83 end
84 end
85 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
86
87 %%% Improve the figure(s)
88
89 for iFig = 1:nFigs
90     fig = figHs(iFig);
91
92     lineObjects = findall(fig, 'Type', 'line');
93     textObjects = findall(fig, 'Type', 'text');
94     axesObjects = findall(fig, 'Type', 'axes');
95     legObjects = findall(fig, 'Type', 'legend');

```

```

97 contourObjects = findall(fig,'Type','contour'); % not counted as lines
98
99 %%% TEXT APPEARANCE: first set all to textSize and then change the ones
100 %%% that need to be changed again
101
102 %Change size of any text objects in the plot
103 set(textObjects,'FontSize',textSize);
104 set(legObjects,'FontSize',legTextSize);
105
106 %%% FIX LINESTYLE, COLOR ETC. FOR EACH PLOT SEPARATELY
107 for iAx = 1:numel(axesObjects)
108     lineObjInAx = findall(axesObjects(iAx), 'Type', 'line');
109
110     %set line style and color style (only works if all figs have some
111     %number of line plots..)
112     if ~isempty(LineStyle)
113         set(lineObjInAx, {'LineStyle'}, LineStyle)
114         set(contourObjects, {'LineStyle'}, LineStyle); %%%%%%%%%
115     end
116     if ~isempty(LineColor)
117         set(lineObjInAx, {'Color'}, LineColor)
118         set(contourObjects, {'LineColor'}, LineColor); %%%%%%%%%
119     end
120     if ~isempty(Marker)
121         set(lineObjInAx, {'Marker'}, Marker)
122         set(lineObjInAx, {'Markersize'}, num2cell(10+22*strcmp(Marker, '.'))↵
123         )
124     end
125
126     %%% change font sizes.
127     % Tick label size
128     xLim = axesObjects(iAx).XLim;
129     axesObjects(iAx).FontSize = tickLabelSize;
130     axesObjects(iAx).XLim = xLim;
131     %Change label size
132     axesObjects(iAx).XLabel.FontSize = labelSize;
133     axesObjects(iAx).YLabel.FontSize = labelSize;
134
135     %Change title size
136     axesObjects(iAx).Title.FontSize = titleSize;
137 end
138
139 %%% LINE APPEARANCE
140 %Change line thicknesses
141 set(lineObjects,'LineWidth',lineWidth);
142 set(contourObjects, 'LineWidth', lineWidth);
143 set(axesObjects, 'LineWidth', axesWidth)
144
145 % set interpreter: latex or tex
146 set(textObjects, 'interpreter', interpreter)
147 set(legObjects, 'Interpreter', interpreter)
148 set(axesObjects, 'TickLabelInterpreter', interpreter);
149 end
end

```

C.3 Change size of figures: setFigureSize.m

```

1 function [ fig ] = setFigureSize( fig )
2 %figureSizePaper1
3 fig.Units = 'points';
4 W = 600;
5 H = 300;
6
7 fig.WindowStyle = 'normal'; % undock
8 fig.Position(3:4) = [W H];
9
10 end

```