NB: The graded, first version of the report must be returned if you hand in a second time!

H1b: MD simulation – dynamic properties

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Task №	Points	Avail. points
Σ		

Introduction

.... TODO... !!!!!!!!!!!!!!!!!!!!

Task 1: potential energy

The theoretical lattice parameter for aluminim can be determined by calculating the minimum potential energy per unit cell in a lattice with zero initial momenta for all particles.

Figure 1 shows the potential energy as a function of the lattice parameter. We used a quadratic fit to find the minimum energy, and obtained $V_{\text{eq}} \approx 65.38\,\text{Å}^3$. This corresponds to the equilibrium lattice parameter $a_{\text{eq}} \approx 4.029\,\text{Å}$ at 0 K, which we took as the initial lattice parameter for the following tasks.

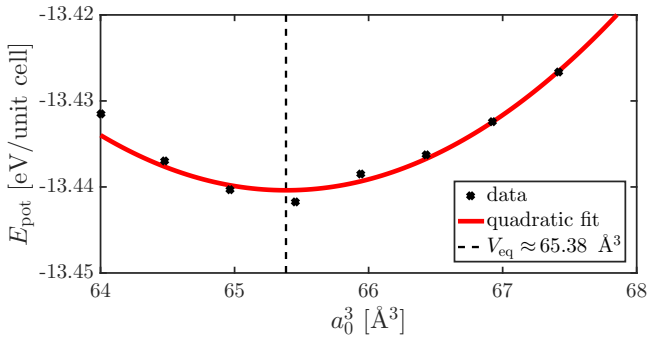

Figure 1: The potential energy per unit cell for aluminum as a function of the lattice parameter cubed.

We find that figure 1 looks similar to the figure 1 in the homework problem file.

Task 2: detmine the timestep

With the random noise, the temperature and the energy are differs between runs, but are in the same order of magnitude. From figure 2, we determine that $dt = 5 \cdot 10^{-3}$ ps = 5 fs is a sufficient time step. This is in line with the lecture notes, where it is stated that the a suitable timestep would normally be a few femtoseconds, or somewhat larger for heavy atoms.

We note that the temperature is higher than desired value of 600-800 K. The temperatures and energies up to one standard deviation are quantified in table 1.

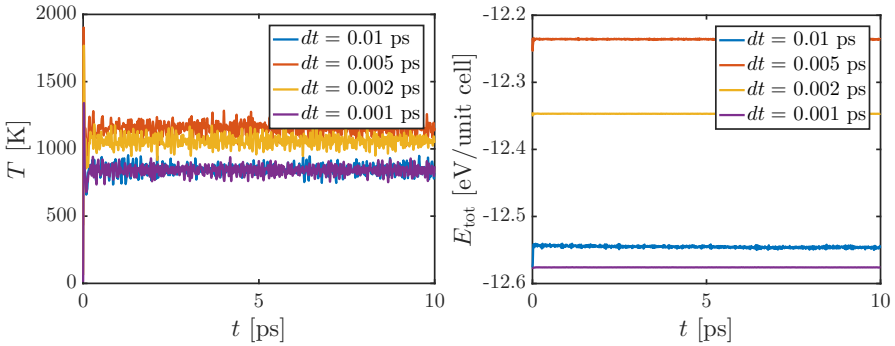

Figure 2: The temperature and kinetic energy per unit cell as a function of time for four different timesteps.

Table 1: Energies and temperatures with one standard deviation uncertainties for four different values of the time steps.

dt [ps]	T [K]	E_{tot} [eV/unit cell]
10^{-2}	$847 \pm 4.2\%$	$-12.55 \pm 1.2 \cdot 10^{-2}\%$
$5 \cdot 10^{-3}$	$1157 \pm 3.8\ \%$	$-12.24 \pm 3.6 \cdot 10^{-3}\%$
$2 \cdot 10^{-3}$	$1058 \pm 3.7\%$	$-12.35 \pm 6.6 \cdot 10^{-4}\%$
$1 \cdot 10^{-3}$	$841 \pm 3.7\%$	$-12.58 \pm 3.6 \cdot 10^{-4}\%$

Tasks 3 and 4: Temperature and pressure equilibration

We set $\tau_P = \tau_T = 100dt$, where $dt = 5 \cdot 10^{-3}$ ps, and equilibrated the temperature and pressure by scaling the particle momenta and positions (and box size) respectively. Choosing a slower equilibration time did not affect the results qualitatively. Both temperature and pressure were equilibrated in the same Verlet loop, but for the higher temperature the the system was first melted by increasing the temperature to 900 °C. To determine the isothermal compressibility κ, the values of Young's modulus Y and shear modulus G were taken from Physics Handbook, table T 1.1. From F 1.15 in Physics Handbook, the bulk modulus can then calculated as

$$B = \frac{YG}{9G - 3Y} \qquad \kappa_{\text{Al}} = \frac{1}{B} \approx 6.6444 \cdot 10^5 \text{ bar}, \tag{1}$$

where $1\,\text{bar} = 6.2415 \cdot 10^{-7}\,\text{eV/Å}^3$ in atomic units. **However, we set $\kappa = 100\kappa_{\text{Al}}$ since the pressure equilibration happened on a much longer timescale than τ_P with $\kappa = \kappa_{\text{Al}}$. We have not yet figured out why this is.**

The results are shown in figure 3, where we overlay the instantaneous values of $\mathcal{T}$ and $\mathcal{P}$ with a moving average using 250 time steps. The desired temperatures and pressures were approximatelyh obtained in the equilibration process. Although the average pressure was slightly below zero, this is within the fluctuation error bars and is in line with the figure 2 in the homework problem document.

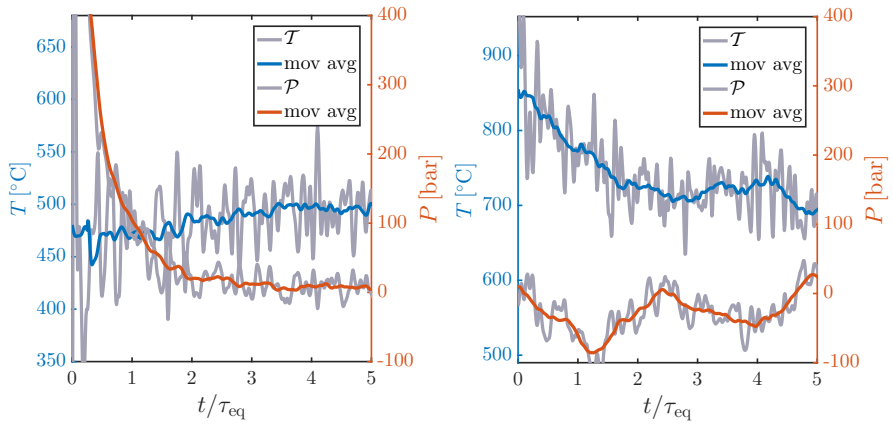

Figure 3: The instantaneous values of $\mathcal{T}$ and $\mathcal{P}$ overlayed with with a moving average using 100 time steps, which corresponds to $\Delta t = \tau_P/2$. Left panel: $T = 500$ °C, right panel: $T = 500$ °C.

The equilibrium values of the lattice parameter were found to be

$$a_0 \approx 4.10\,\text{Å}, \quad T = 500\,°\text{C}, \tag{2}$$

$$a_0 \approx 4.29\,\text{Å}, \quad T = 700\,°\text{C}. \tag{3}$$

These value are larger than the zero-temperature constants, and it is reasonable that the higher 700 °C case corresponds to a larger lattice parameter at constant pressure.

Tasks 3-5: particle trajectories

Starting with the temperature- and pressure equilibrated systems from the previous section, we study the particle trajectories for both systems. Here, we decrease the timestep to $dt = 5 \cdot 10^{-4}$ ps and the simulation length to $t_{\text{end}} = 5$ ps to get better statistics. This was mostly motivated by increasing the resolution in tasks 6-7.

First, we note that the cumulative averages of the instantaneous temperatures and pressures stayed close to their inital values. This is shown in figure 6.

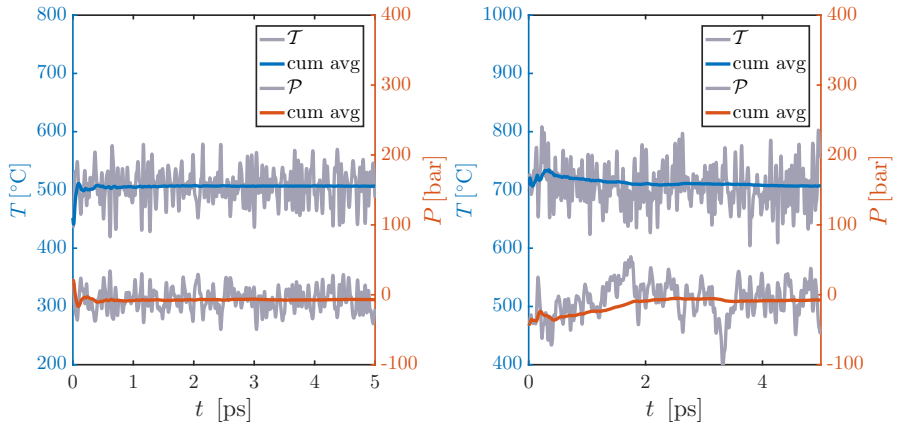

Figure 4: The instantaneous values, and the cumulative averages, of the temperature and the pressure in the production runs. Left panel: $T = 500\,°\text{C}$, right panel: $T = 500\,°\text{C}$

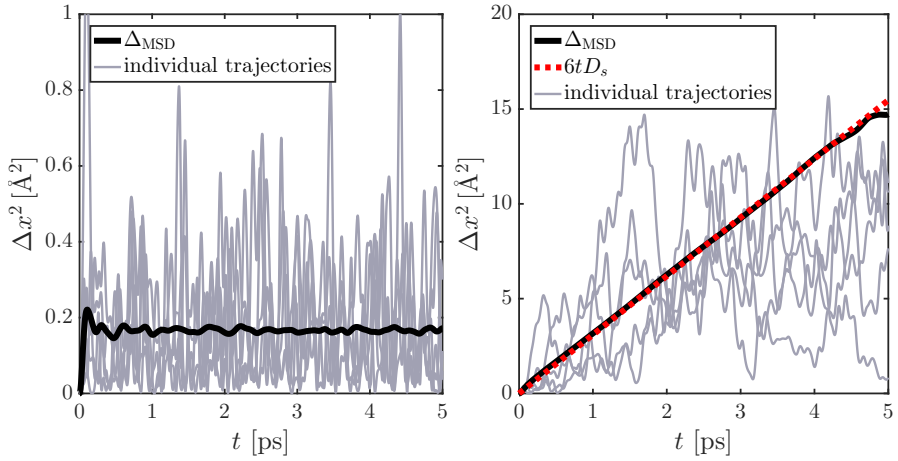

Figure 5: The instantaneous values, and the cumulative averages, of the temperature and the pressure in the production runs. Left panel: $T = 500\,°\text{C}$, right panel: $T = 500\,°\text{C}$

Task 5

Equation (82) in MD lecture notes:

$$\Delta_{\text{MSD}}(t) = \lim_{T\to\infty} \frac{1}{T} \int_0^T dt' \frac{1}{N_{\text{atoms}}} \sum_{i=0}^{N_{\text{atoms}}-1} \left[\mathbf{r}_i(t+t') - \mathbf{r}_i(t')\right]^2 \tag{4}$$

$$\Rightarrow$$

$$\Delta_{\text{MSD}}(t_k) \approx \frac{1}{N_T - k} \frac{1}{N_{\text{atoms}}} \sum_{j=0}^{N_T-k-1} \sum_{i=0}^{N_{\text{atoms}}-1} \left[\mathbf{r}_i(t_{k+j}) - \mathbf{r}_i(t_j)\right]^2 \tag{5}$$

To determine M, we used mean of ... for t > ...

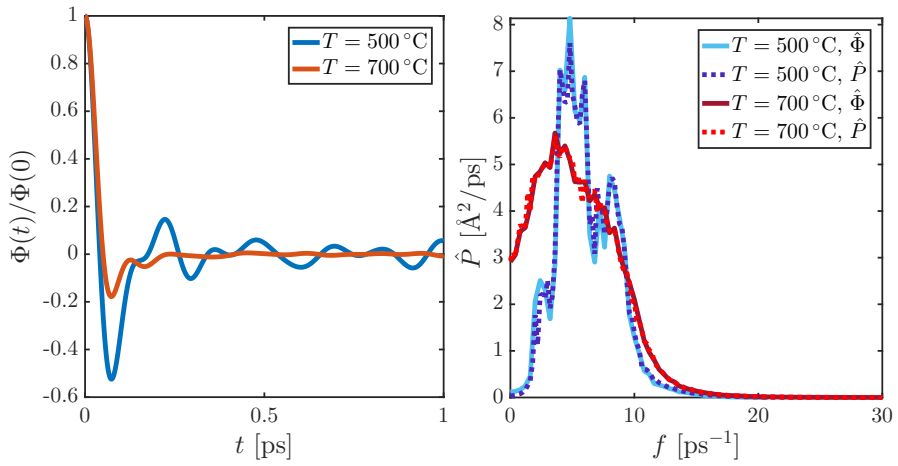

Figure 6: The instantaneous values, and the cumulative averages, of the temperature and the pressure in the production runs. Left panel: $T = 500\,^\circ$C, right panel: $T = 500\,^\circ$C

Task 7

What we did

We calculated the discrete auto-correlation function similarly to the MSD,

$$\Phi_j = \frac{1}{N-j} \sum_{i=0}^{N-j-1} \left\langle v_{i+j} v_i \right\rangle, \tag{6}$$

where $j = 0, 1, \ldots, N-1$ and the average is taken over all atoms. We then preceded to numerically approximate the integral

$$\hat{\Phi}(f) = 2 \int_0^\infty \mathrm{d}t \ \Phi(t) \cos(2\pi f t) \approx 2 \int_0^{T_s} \mathrm{d}t \ \Phi(t) \cos(2\pi f t) \tag{7}$$

using a trapeziodal method in MATLAB, with a frequency range $f = 0$ to $f = 1/(2\Delta t) = f_{\text{Nyqvist}}$, and frequency steps $\Delta f = 1/T_s$, where T_s is a time at about half the simulation end time. This is to avoid including noisy data in $\Phi(t)$ at later times, where the statistics are poor.

We then calculated the powerspectrum according to

$$\begin{aligned} \hat{P}(\omega) &= \lim_{T\to\infty} \frac{1}{T} \left\langle \left| \int_0^T \mathrm{d}t \ v(t) \mathrm{e}^{\mathrm{i}\omega t} \right|^2 \right\rangle \\ &\approx \frac{1}{T} \left\langle \left| \int_0^T \mathrm{d}t \ v(t) \mathrm{e}^{\mathrm{i}\omega t} \right|^2 \right\rangle \\ \implies \quad \hat{P}_k &= \frac{1}{T} \left\langle \left| \frac{T}{N} \sum_{i=0}^{N-1} v_i \exp\left(\mathrm{i}2\pi \frac{ik}{N} \right) \right|^2 \right\rangle = \frac{T}{N} \left\langle |\hat{\boldsymbol{v}}_k|^2 \right\rangle \end{aligned} \tag{8}$$

where the averages is taken over all atoms, and

$$\hat{\boldsymbol{v}}_k = \sqrt{N} \sum_{i=0}^{N-1} \boldsymbol{v}_i \exp\left(\mathrm{i}2\pi \frac{ik}{N} \right) \tag{9}$$

is the discrete Fourier transform of v_i.

When we compare $\hat{\Phi}_k$ and $\hat{P}_k$ in Figure **??**, we find that they are very similar, as, indeed, they should be acording to the Wiener-Khinthchine theorem.

Concluding discussion

!!!!!!!!!!!!!!!!!!!!!!!!1

A Source Code

Include all source code here in the appendix. Keep the code formatting clean, use indentation, and comment your code to make it easy to understand. Also, break lines that are too long. (Keep them under 80 characters!)

A.1 Main program task 1: `main_T1.c`

```c
/*
  main_T1.c Task 1 H1b
  In this task, we scan over a range of lattice parameters, a0, to determine
  which results in the lowest potetntial energy stored in the lattice.

  System of units:
  Energy - eV
  Time   - ps
  Length - Angstrom
  Temp   - K
*/
#include <stdio.h>
#include <math.h>
#include <stdlib.h>

#include "initfcc.h"
#include "alpotential.h"

#define N_cells 4
#define N_lattice_params 25

/* Main program */
int main()
{
  int N_atoms = 4*N_cells*N_cells*N_cells;
  double a0;
  double a0_min = 4.0;
  double a0_max = 4.2;
  double da0 = (a0_max - a0_min)/N_lattice_params;

  double (*pos)[3] = malloc(sizeof(double[N_atoms][3]));
  double *energy = malloc(sizeof(double[N_lattice_params]));

  FILE *file_pointer;

  for (int i=0; i<N_lattice_params; i++){
    a0 = a0_min + i*da0;        // The lattice constant of this iteration
    init_fcc(pos, N_cells, a0); // Init, FCC cells with lattice constant `a0`
    // energy per unit cell
    energy[i] = get_energy_AL(pos, N_cells*a0, N_atoms )*4/N_atoms;
  }

  // Write to files
  file_pointer = fopen("../data/lattice_energies.tsv", "w");
  for (int i=0; i<N_lattice_params; i++){
    a0 = a0_min + i*da0;
    fprintf(file_pointer, "%.8f \t %.8f \n", a0, energy[i]);
  }
  fclose(file_pointer);

  free(pos);    pos = NULL;
  free(energy); energy = NULL;
  return 0;
}
```

A.2 Main program Task 2: `main_T2.c`

```c
/*
  main_T2.c, Task 2, H1b
  In this task, we add random noise to the particle positions and see how the
  system evolves in time. Using the kinetic energy of the particles, we can
  derive an instantaneous temperature of the system.

  System of units:
  Energy - eV
  Time   - ps
  Length - Angstrom
  Temp   - K
*/

#include <stdio.h>
#include <math.h>
```

```c
#include <stdlib.h>
#include <time.h>

#include "initfcc.h"
#include "alpotential.h"
#include "funcs.h"

#define N_cells 4
#define AMU 1.0364e-4
#define kB 8.6173303e-5

/* Main program */
int main()
{
  int N_atoms = 4*N_cells*N_cells*N_cells;
  double m_Al = 27*AMU;

  double a_eq = 4.03; // Min potential energy lattice constant

  double noise_amplitude = 6.5e-2 * a_eq;
  double t_max=10; //
  double dt = 1e-3;
  int N_timesteps = t_max/dt;
  double t, E_kin;

  double (*pos)[3] = malloc(sizeof(double[N_atoms][3]));
  double (*momentum)[3] = malloc(sizeof(double[N_atoms][3]));
  double (*forces)[3] = malloc(sizeof(double[N_atoms][3]));
  double *temperature = malloc(sizeof(double[N_timesteps]));
  double *E_tot = malloc(sizeof(double[N_timesteps]));

  FILE *file_pointer;


  /* ----------------------------- TASK 2 ----------------------------------*/

  init_fcc(pos, N_cells, a_eq); // initialize fcc lattice
  add_noise( N_atoms, 3, pos, noise_amplitude ); // adds random noise to pos
  set_zero( N_atoms, 3, momentum); // set momentum to 0
  get_forces_AL( forces, pos, a_eq*N_cells, N_atoms); //initial cond forces

  for (int i=0; i<N_timesteps; i++){
    /*
       The loop over the timesteps first takes a timestep according to the
       Verlet algorithm, then calculates the energies and temeperature.
    */
    timestep_Verlet (N_atoms, pos,  momentum, forces, m_Al, dt, a_eq*N_cells);

    E_kin    = get_kin_energy(N_atoms, momentum, m_Al );
    E_tot[i] = (E_kin + get_energy_AL(pos, a_eq*N_cells, N_atoms))*4/N_atoms;

    /* 3N*kB*T/2 = 1/(2m) * \sum_{i=1}^{N} p_i^2  = p_sq/(2m) */
    temperature[i] =  E_kin * 2/(3*N_atoms*kB);
  }

  /* Write tempertaure to file */
  char file_name[100];
  sprintf(file_name,"../data/temperature_dt-%0.0e_Task2.tsv", dt);
  file_pointer = fopen(file_name, "w");
  for (int i=0; i<N_timesteps; i++){
    t = i*dt; // time at step i
    fprintf(file_pointer, "%.4f \t %.8f \n", t, temperature[i]);
  }
  fclose(file_pointer);

  /* Write total energy to file */
  sprintf(file_name,"../data/total_energy_dt-%0.0e_Task2.tsv", dt);
  file_pointer = fopen(file_name, "w");
  for (int i=0; i<N_timesteps; i++){
    t = i*dt; // time at step i
    fprintf(file_pointer, "%.4f \t %.8f \n", t, E_tot[i]);
  }
  fclose(file_pointer);

  free(pos);         pos = NULL;
  free(momentum);    momentum = NULL;
  free(forces);      forces = NULL;
  free(temperature); temperature = NULL;
  free(E_tot);       E_tot = NULL;
  return 0;
}
```

A.3 Temperature and pressure equilibration for tasks 3-7 : `main_T3.c`

```c
/*
  main_T3.c
```

```
3
4
5   */
6
7   #include <stdio.h>
8   #include <math.h>
9   #include <stdlib.h>
10  #include <time.h>
11
12  #include "initfcc.h"
13  #include "alpotential.h"
14  #include "funcs.h"
15
16  #define N_cells 4
17  /* define constants in atomic units: eV,   , ps, K */
18  #define AMU 1.0364e-4
19  #define degC_to_K 273.15
20  #define bar 6.2415e-07
21  #define kB 8.61733e-5
22
23  /* Main program */
24  int main()
25  {
26     char file_name[100];
27
28     int N_atoms = 4*N_cells*N_cells*N_cells;
29     double m_Al = 27*AMU;
30     /*
31       Values of Young's and shear modulus, Y and G resp., taken from
32       Physics Handbook, table T 1.1. Bulk mudulus then calculated as
33       B = Y*G / (9*G - 3*Y)   [F 1.15, Physics Handbook]
34       kappa = 1/B
35     */
36     double kappa_Al = 100/(6.6444e+05 * bar); // STRANGE FACTOR 100 OFF !!!
37     double a_eq = 4.03;
38     double cell_length = a_eq*N_cells;
39     double inv_volume = pow(N_cells*cell_length, -3);
40     double noise_amplitude = 6.5e-2 * a_eq;
41
42     double T_final_C= 500;
43     int nRuns = 1; //2 if melt, 1 otherwise
44     double T_melt_C = 900;
45
46     double P_final_bar= 1;
47
48    double T_eq;
49    double P_eq  = P_final_bar*bar;
50    double dt    = 5e-3;
51    double tau_T = 100*dt;
52    double tau_P = 100*dt;
53    //double t_T_eq= 10*tau_T; //equlibration times
54    double t_eq= 15*tau_P; //equlibration times
55    int N_timesteps = t_eq/dt;
56
57    double alpha_T, alpha_P,alpha_P_cube_root;
58    double t, E_kin, virial;
59
60
61    double (*pos)[3] = malloc(sizeof(double[N_atoms][3]));
62    double (*momentum)[3] = malloc(sizeof(double[N_atoms][3]));
63    double (*forces)[3] = malloc(sizeof(double[N_atoms][3]));
64    double *temperature = malloc(sizeof(double[N_timesteps]));
65    double *pressure = malloc(sizeof(double[N_timesteps]));
66
67
68    FILE *file_pointer;
69
70    /* ----------------------------- TASK 3 ----------------------------------*/
71
72
73    init_fcc(pos, N_cells, a_eq); // initialize fcc lattice
74    add_noise( N_atoms, 3, pos, noise_amplitude ); // adds random noise to pos
75    set_zero( N_atoms, 3, momentum); // set momentum to 0
76    get_forces_AL( forces, pos, cell_length, N_atoms); //initial cond forces
77
78    /*
79    for (int i=0; i<N_timesteps_T_eq; i++){
80      //
81         The loop over the timesteps first takes a timestep according to the
82         Verlet algorithm, then calculates the energies and temeperature.
83      //
84      timestep_Verlet(N_atoms, pos,  momentum, forces, m_Al, dt, cell_length);
85
86      E_kin  = get_kin_energy(N_atoms, momentum, m_Al );
87      virial = get_virial_AL(pos, cell_length, N_atoms);
88
89      // PV = NkT + virial
90      pressure[i] = inv_volume * (1.5*E_kin + virial);
91      // 3N*kB*T/2 = 1/(2m) * \sum_{i=1}^{N} p_i^2  = p_sq/(2m)
92      temperature[i] =  E_kin * 1/(1.5*N_atoms*kB);
93
```

```
    alpha_T = 1 + 2*dt*(T_eq - temperature[i]) / (tau_T * temperature[i]);
    scale_mat(N_atoms, 3, momentum, sqrt(alpha_T));
    temperature[i]*=alpha_T;
  }
  */


    for (int irun=0; irun < nRuns; irun++){// last run: final, irun = 0
       if (irun == nRuns - 1){ // final run
          T_eq = T_final_C + degC_to_K;
       }else{
          T_eq = T_melt_C + degC_to_K;
       }
        for (int i=0; i<N_timesteps; i++){
      /*
         The loop over the timesteps first takes a timestep according to the
         Verlet algorithm, then calculates the energies and temeperature.
      */
      timestep_Verlet(N_atoms, pos,  momentum, forces, m_Al, dt, cell_length);


      E_kin  = get_kin_energy(N_atoms, momentum, m_Al );
      virial = get_virial_AL(pos, cell_length, N_atoms);

      /* 3N*kB*T/2 = 1/(2m) * \sum_{i=1}^{N} p_i^2  = p_sq/(2m) */
      temperature[i] =  E_kin * 1/(1.5*N_atoms*kB);
      /* PV = NkT + virial */
      pressure[i] = inv_volume * (1.5*E_kin + virial);

      /* Equlibrate temperature by scaling momentum by a factor sqrt(alpha_T).
          N.B. It is equally valid to scale the momentum instead of the velocity
          ,
          since they only differ by a constant factor m.
      */
      alpha_T = 1 + 2*dt*(T_eq - temperature[i]) / (tau_T * temperature[i]);
      scale_mat(N_atoms, 3, momentum, sqrt(alpha_T));

      // Equlibrate pressure by scaling the posistions by a factor of alpha_P
          ^(1/3)

      alpha_P = 1 - kappa_Al* dt*(P_eq - pressure[i])/tau_P;
      alpha_P_cube_root = pow(alpha_P, 1.0/3.0);
      scale_mat(N_atoms, 3, pos, alpha_P_cube_root);

      cell_length*=alpha_P_cube_root;
      inv_volume*=1/alpha_P;

      temperature[i]*=alpha_T;
      pressure[i]*=alpha_P;
      }
    }

    printf("equilibrium a0 = %.4f A\n", cell_length/N_cells);

  /* Write tempertaure to file */
  sprintf(file_name,"../data/temp-%d_pres-%d_Task3.tsv",
      (int) T_final_C, (int) P_final_bar);
  file_pointer = fopen(file_name, "w");
  for (int i=0; i<N_timesteps; i++){
    t = i*dt; // time at step i
    fprintf(file_pointer, "%.4f \t %.8f \t %.8f \n",
        t, temperature[i],pressure[i]);
  }
  fclose(file_pointer);

  /* Write phase space coordinates to file */
  sprintf(file_name,"../data/phase-space_temp-%d_pres-%d.tsv",
      (int) T_final_C, (int) P_final_bar);
  file_pointer = fopen(file_name, "w");
  for (int i=0; i<N_atoms; i++){
    for (int j=0;j<3;j++){
      fprintf(file_pointer, " %.16e \t", pos[i][j]);
    }
    for (int j=0;j<3;j++){
      fprintf(file_pointer, " %.16e \t", momentum[i][j]);
    }
    fprintf(file_pointer,"\n");
  }
  fclose(file_pointer);

  /* save equlibrated position and momentum as a binary file */
  sprintf(file_name,"../data/INIDATA_temp-%d_pres-%d.bin",
      (int) T_final_C, (int) P_final_bar);
  file_pointer = fopen(file_name, "wb");
  fwrite(pos, sizeof(double), 3*N_atoms, file_pointer);
  fwrite(momentum, sizeof(double), 3*N_atoms, file_pointer);
  fwrite(&cell_length, sizeof(double), 1, file_pointer);
  fclose(file_pointer);
```

```
  /*
  printf("T=%0.2f\tP=%0.2e\n",
     temperature[N_timesteps-1],pressure[N_timesteps-1]);
  */

  free(pos); pos = NULL;
  free(momentum); momentum = NULL;
  free(forces); forces = NULL;
  free(temperature); temperature = NULL;
  free(pressure); pressure = NULL;
  //free(volume); volume = NULL;
  return 0;
}
```

A.4 Production runs for tasks 3-7 : `main_Prod.c`

```
/*
 MD_main.c

 Created by Anders Lindman on 2013-10-31.
 */

#include <stdio.h>
#include <math.h>
#include <stdlib.h>
#include <time.h>

#include "initfcc.h"
#include "alpotential.h"
#include "funcs.h"

#define N_cells 4
/* define constants in atomic units: eV,   , ps, K */
#define AMU 1.0364e-4
#define degC_to_K 273.15
#define bar 6.2415e-07
#define kB 8.61733e-5

/* Main program */
int main()
{
  char file_name[100];

  int N_atoms = 4*N_cells*N_cells*N_cells;
  double m_Al = 27*AMU;
  /*
    Values of Young's and shear modulus, Y and G resp., taken from
    Physics Handbook, table T 1.1. Bulk mudulus then calculated as
    B = Y*G / (9*G - 3*Y)   [F 1.15, Physics Handbook]
    kappa = 1/B
  */
//  double kappa_Al = 100/(6.6444e+05 * bar); // STRANGE FACTOR 100 OFF !!!
  double cell_length = 0;
  double inv_volume;


  double T_eq_C   = 500;
  double P_eq_bar = 1;
//  double T_eq     = T_eq_C + degC_to_K;
//  double P_eq     = P_eq_bar*bar;
  double dt       = 5e-4; // higher res for spectral function
  double t_end    = 5;
//  double tau_T = 100*dt;
//  double tau_P = 100*dt;

  int N_timesteps = t_end/dt;

  int N_between_steps = 1;
  int N_save_timesteps = N_timesteps / N_between_steps; //for the displacements
  int N_save_atoms = 5;

//  double alpha_T, alpha_P,alpha_P_cube_root;
  double t, E_kin, virial;

  double (*pos)[3]      = malloc(sizeof(double[N_atoms][3]));
  double (*pos_0)[3]    = malloc(sizeof(double[N_atoms][3]));
  double (*momentum)[3] = malloc(sizeof(double[N_atoms][3]));
  double (*forces)[3]   = malloc(sizeof(double[N_atoms][3]));
  double (*displacements)[N_save_atoms] =
            malloc(sizeof(double[N_save_timesteps][N_save_atoms]));
  double (*pos_all)[N_atoms][3] =
            malloc(sizeof(double[N_save_timesteps][N_atoms][3]));
  double (*vel_all)[N_atoms][3] =
            malloc(sizeof(double[N_save_timesteps][N_atoms][3]));
  double *temperature   = malloc(sizeof(double[N_timesteps]));
  double *pressure      = malloc(sizeof(double[N_timesteps]));
```

```
  double *msd           = malloc(sizeof(double[N_save_timesteps]));
  double *vel_corr      = malloc(sizeof(double[N_save_timesteps]));
  double *pow_spec      = malloc(sizeof(double[N_save_timesteps]));
  double *freq            = malloc(sizeof(double[N_save_timesteps]));

  for (int i = 0; i<N_save_timesteps; i++){
    msd[i] = 0;
    pow_spec[i] = 0;
    vel_corr[i] = 0;
  }
  FILE *file_pointer;

  /* ------------------------------ TASK 3 ----------------------------------*/

  // read positions, momenta and cell_length
  sprintf(file_name,"../data/INIDATA_temp-%d_pres-%d.bin",
      (int) T_eq_C, (int) P_eq_bar);
  file_pointer = fopen(file_name, "rb");
  fread(pos, sizeof(double), 3*N_atoms, file_pointer);
  fread(momentum, sizeof(double), 3*N_atoms, file_pointer);
  fread(&cell_length, sizeof(double), 1, file_pointer);
  fclose(file_pointer);

  for (int i=0; i<N_atoms; i++){
    for (int j=0; j<3; j++){
      pos_0[i][j]=pos[i][j];
    }
  }
  inv_volume = pow(N_cells*cell_length, -3);
  get_forces_AL( forces, pos, cell_length, N_atoms); //initial cond forces

  printf("Initialized. Starting with Verlet timestepping.\n");
  for (int i=0; i<N_timesteps; i++){
    /*
       The loop over the timesteps first takes a timestep according to the
       Verlet algorithm, then calculates the energies and temeperature.
    */
    timestep_Verlet(N_atoms, pos,  momentum, forces, m_Al, dt, cell_length);

    E_kin  = get_kin_energy(N_atoms, momentum, m_Al );
    virial = get_virial_AL(pos, cell_length, N_atoms);

    /* PV = NkT + virial */
    pressure[i] = inv_volume * (1.5*E_kin + virial);
    /* 3N*kB*T/2 = 1/(2m) * \sum_{i=1}^{N} p_i^2  = p_sq/(2m) */
    temperature[i] =  E_kin * 1/(1.5*N_atoms*kB);

    if (i % N_between_steps == 0){
         int k = i/N_between_steps; // number of saved timesteps so far
          get_displacements (N_save_atoms,  pos, pos_0, displacements[k]);
         copy_mat(N_atoms, 3, pos, pos_all[k]);

         copy_mat(N_atoms, 3, momentum, vel_all[k]);
         scale_mat(N_atoms, 3, vel_all[k], 1/m_Al);
     }
    if ((i*10) % N_timesteps == 0){
       printf("done %d0 %% of Verlet timestepping\n", (i*10)/N_timesteps);
    }
  }
  printf("calculating MSD\n");
  get_MSD(N_atoms, N_save_timesteps, pos_all, msd);

  printf("calculating velocity correlation\n");
  get_vel_corr(N_atoms, N_save_timesteps, vel_all, vel_corr);

  printf("calculating power spectrum\n");
  get_powerspectrum(N_atoms, N_save_timesteps, vel_all, pow_spec);
  fft_freq(freq, dt, N_save_timesteps);



  printf("writing to file\n");
  /* Write tempertaure to file */

  sprintf(file_name,"../data/temp-%d_pres-%d_Prod-test.tsv",
      (int) T_eq_C, (int) P_eq_bar);
  file_pointer = fopen(file_name, "w");
  for (int i=0; i<N_timesteps; i++){
    t = i*dt; // time at step i
    fprintf(file_pointer, "%.4f \t %.8f \t %.8f \n",
        t, temperature[i],pressure[i]);
  }
  fclose(file_pointer);

  /* Write displacements to file */
  sprintf(file_name,"../data/temp-%d_pres-%d_displacements.tsv",
      (int) T_eq_C, (int) P_eq_bar);
  file_pointer = fopen(file_name, "w");
  for (int i=0; i<N_save_timesteps; i++){
    t = i*dt*N_between_steps; // time at step i
    fprintf(file_pointer, "%.4f", t);
```

```
    for (int j=0; j<N_save_atoms; j++){
        fprintf(file_pointer, "\t %.8f", displacements[i][j]);
     }
     fprintf(file_pointer, "\n");
  }
  fclose(file_pointer);

   /* Write MSD to file */
  sprintf(file_name,"../data/temp-%d_pres-%d_dynamicProperties.tsv",
      (int) T_eq_C, (int) P_eq_bar);
  file_pointer = fopen(file_name, "w");
  // write header
  fprintf(file_pointer, "%% t[ps] \t MSD[A^2] \t vel_corr [A/ps]^2 \n");
  for (int i=0; i<N_save_timesteps; i++){
     t = i*dt*N_between_steps; // time at step i
     fprintf(file_pointer, "%.4f \t %.8f \t %.8f \n", t, msd[i], vel_corr[i]);
  }
  fclose(file_pointer);

  sprintf(file_name,"../data/temp-%d_pres-%d_power-spectrum.tsv",
      (int) T_eq_C, (int) P_eq_bar);
  file_pointer = fopen(file_name, "w");
  // write header
  fprintf(file_pointer, "%% f[1/ps] \t P[A/ps]^2 \n");
  for (int i=0; i<N_save_timesteps/2; i++){ // only print from f=0 to f_crit
     fprintf(file_pointer, "%.4f \t %.8f \n", freq[i], pow_spec[i]);
  }
  fclose(file_pointer);

  free(pos);           pos = NULL;
  free(pos_0);         pos_0 = NULL;
  free(momentum);      momentum = NULL;
  free(forces);        forces = NULL;
  free(temperature);   temperature = NULL;
  free(pressure);      pressure = NULL;
  free(displacements); displacements = NULL;
  free(pos_all); pos_all = NULL;
  free(vel_all); vel_all = NULL;
  free(msd); msd = NULL;
  free(vel_corr); vel_corr = NULL;
  free(pow_spec); pow_spec = NULL;
  free(freq); freq = NULL;
  return 0;
}
```

A.5 Production runs for tasks 3-7 : `main_Prod.c`

```
/*
 MD_main.c

 Created by Anders Lindman on 2013-10-31.
 */

#include <stdio.h>
#include <math.h>
#include <stdlib.h>
#include <time.h>

#include "initfcc.h"
#include "alpotential.h"
#include "funcs.h"

#define N_cells 4
/* define constants in atomic units: eV,   , ps, K */
#define AMU 1.0364e-4
#define degC_to_K 273.15
#define bar 6.2415e-07
#define kB 8.61733e-5

/* Main program */
int main()
{
  char file_name[100];

  int N_atoms = 4*N_cells*N_cells*N_cells;
  double m_Al = 27*AMU;
  /*
    Values of Young's and shear modulus, Y and G resp., taken from
    Physics Handbook, table T 1.1. Bulk mudulus then calculated as
    B = Y*G / (9*G - 3*Y)   [F 1.15, Physics Handbook]
    kappa = 1/B
  */
//  double kappa_Al = 100/(6.6444e+05 * bar); // STRANGE FACTOR 100 OFF !!!
  double cell_length = 0;
  double inv_volume;

```

```
40
41    double T_eq_C   = 500;
42    double P_eq_bar = 1;
43  //  double T_eq     = T_eq_C + degC_to_K;
44  //  double P_eq     = P_eq_bar*bar;
45    double dt       = 5e-4; // higher res for spectral function
46    double t_end    = 5;
47  //  double tau_T = 100*dt;
48  //  double tau_P = 100*dt;
49
50    int N_timesteps = t_end/dt;
51
52    int N_between_steps = 1;
53    int N_save_timesteps = N_timesteps / N_between_steps; //for the displacements
54    int N_save_atoms = 5;
55
56  //  double alpha_T, alpha_P,alpha_P_cube_root;
57    double t, E_kin, virial;
58
59    double (*pos)[3]      = malloc(sizeof(double[N_atoms][3]));
60    double (*pos_0)[3]    = malloc(sizeof(double[N_atoms][3]));
61    double (*momentum)[3] = malloc(sizeof(double[N_atoms][3]));
62    double (*forces)[3]   = malloc(sizeof(double[N_atoms][3]));
63    double (*displacements)[N_save_atoms] =
64              malloc(sizeof(double[N_save_timesteps][N_save_atoms]));
65    double (*pos_all)[N_atoms][3] =
66              malloc(sizeof(double[N_save_timesteps][N_atoms][3]));
67    double (*vel_all)[N_atoms][3] =
68              malloc(sizeof(double[N_save_timesteps][N_atoms][3]));
69    double *temperature   = malloc(sizeof(double[N_timesteps]));
70    double *pressure      = malloc(sizeof(double[N_timesteps]));
71    double *msd           = malloc(sizeof(double[N_save_timesteps]));
72    double *vel_corr      = malloc(sizeof(double[N_save_timesteps]));
73    double *pow_spec      = malloc(sizeof(double[N_save_timesteps]));
74    double *freq            = malloc(sizeof(double[N_save_timesteps]));
75
76    for (int i = 0; i<N_save_timesteps; i++){
77      msd[i] = 0;
78      pow_spec[i] = 0;
79      vel_corr[i] = 0;
80    }
81    FILE *file_pointer;
82
83    /* ----------------------------- TASK 3 ----------------------------------*/
84
85    // read positions, momenta and cell_length
86    sprintf(file_name,"../data/INIDATA_temp-%d_pres-%d.bin",
87        (int) T_eq_C, (int) P_eq_bar);
88    file_pointer = fopen(file_name, "rb");
89    fread(pos, sizeof(double), 3*N_atoms, file_pointer);
90    fread(momentum, sizeof(double), 3*N_atoms, file_pointer);
91    fread(&cell_length, sizeof(double), 1, file_pointer);
92    fclose(file_pointer);
93
94    for (int i=0; i<N_atoms; i++){
95      for (int j=0; j<3; j++){
96        pos_0[i][j]=pos[i][j];
97      }
98    }
99    inv_volume = pow(N_cells*cell_length, -3);
100   get_forces_AL( forces, pos, cell_length, N_atoms); //initial cond forces
101
102   printf("Initialized. Starting with Verlet timestepping.\n");
103   for (int i=0; i<N_timesteps; i++){
104     /*
105        The loop over the timesteps first takes a timestep according to the
106        Verlet algorithm, then calculates the energies and temeperature.
107     */
108     timestep_Verlet(N_atoms, pos,  momentum, forces, m_Al, dt, cell_length);
109
110     E_kin  = get_kin_energy(N_atoms, momentum, m_Al );
111     virial = get_virial_AL(pos, cell_length, N_atoms);
112
113     /* PV = NkT + virial */
114     pressure[i] = inv_volume * (1.5*E_kin + virial);
115     /* 3N*kB*T/2 = 1/(2m) * \sum_{i=1}^{N} p_i^2  = p_sq/(2m) */
116     temperature[i] =  E_kin * 1/(1.5*N_atoms*kB);
117
118     if (i % N_between_steps == 0){
119          int k = i/N_between_steps; // number of saved timesteps so far
120           get_displacements (N_save_atoms,  pos, pos_0, displacements[k]);
121          copy_mat(N_atoms, 3, pos, pos_all[k]);
122
123          copy_mat(N_atoms, 3, momentum, vel_all[k]);
124          scale_mat(N_atoms, 3, vel_all[k], 1/m_Al);
125      }
126     if ((i*10) % N_timesteps == 0){
127        printf("done %d0 %% of Verlet timestepping\n", (i*10)/N_timesteps);
128     }
129   }
130   printf("calculating MSD\n");
```

```
  get_MSD(N_atoms, N_save_timesteps, pos_all, msd);

  printf("calculating velocity correlation\n");
  get_vel_corr(N_atoms, N_save_timesteps, vel_all, vel_corr);

  printf("calculating power spectrum\n");
  get_powerspectrum(N_atoms, N_save_timesteps, vel_all, pow_spec);
  fft_freq(freq, dt, N_save_timesteps);



  printf("writing to file\n");
  /* Write tempertaure to file */

  sprintf(file_name,"../data/temp-%d_pres-%d_Prod-test.tsv",
      (int) T_eq_C, (int) P_eq_bar);
  file_pointer = fopen(file_name, "w");
  for (int i=0; i<N_timesteps; i++){
    t = i*dt; // time at step i
    fprintf(file_pointer, "%.4f \t %.8f \t %.8f \n",
        t, temperature[i],pressure[i]);
  }
  fclose(file_pointer);

  /* Write displacements to file */
  sprintf(file_name,"../data/temp-%d_pres-%d_displacements.tsv",
      (int) T_eq_C, (int) P_eq_bar);
  file_pointer = fopen(file_name, "w");
  for (int i=0; i<N_save_timesteps; i++){
    t = i*dt*N_between_steps; // time at step i
    fprintf(file_pointer, "%.4f", t);
    for (int j=0; j<N_save_atoms; j++){
        fprintf(file_pointer, "\t %.8f", displacements[i][j]);
     }
     fprintf(file_pointer, "\n");
  }
  fclose(file_pointer);

   /* Write MSD to file */
  sprintf(file_name,"../data/temp-%d_pres-%d_dynamicProperties.tsv",
      (int) T_eq_C, (int) P_eq_bar);
  file_pointer = fopen(file_name, "w");
  // write header
  fprintf(file_pointer, "%% t[ps] \t MSD[A^2] \t vel_corr [A/ps]^2 \n");
  for (int i=0; i<N_save_timesteps; i++){
     t = i*dt*N_between_steps; // time at step i
     fprintf(file_pointer, "%.4f \t %.8f \t %.8f \n", t, msd[i], vel_corr[i]);
  }
  fclose(file_pointer);

  sprintf(file_name,"../data/temp-%d_pres-%d_power-spectrum.tsv",
      (int) T_eq_C, (int) P_eq_bar);
  file_pointer = fopen(file_name, "w");
  // write header
  fprintf(file_pointer, "%% f[1/ps] \t P[A/ps]^2 \n");
  for (int i=0; i<N_save_timesteps/2; i++){ // only print from f=0 to f_crit
     fprintf(file_pointer, "%.4f \t %.8f \n", freq[i], pow_spec[i]);
  }
  fclose(file_pointer);

  free(pos);           pos = NULL;
  free(pos_0);         pos_0 = NULL;
  free(momentum);      momentum = NULL;
  free(forces);        forces = NULL;
  free(temperature);   temperature = NULL;
  free(pressure);      pressure = NULL;
  free(displacements); displacements = NULL;
  free(pos_all); pos_all = NULL;
  free(vel_all); vel_all = NULL;
  free(msd); msd = NULL;
  free(vel_corr); vel_corr = NULL;
  free(pow_spec); pow_spec = NULL;
  free(freq); freq = NULL;
  return 0;
}
```

A.6 Misc functions : `funcs.c`

```
#include "funcs.h"

void add_noise(int M, int N, double mat[M][N], double noise_amplitude )
{
  const  gsl_rng_type *T; /*  static  info  about  rngs */
  gsl_rng *q; /* rng  instance  */
  gsl_rng_env_setup (); /*  setup  the  rngs */
  T = gsl_rng_default; /*  specify  default  rng */
```

```
  q = gsl_rng_alloc(T); /*  allocate  default  rng */
  gsl_rng_set(q,time(NULL)); /*  Initialize  rng */

  for (int i=0; i<N; i++){
    for (int j=0; j<M; j++){
      // adds uniformly distributed random noise in range +-`noise_amplitude`
      mat[i][j] += noise_amplitude * (2*gsl_rng_uniform(q)-1);
    }
  }
  gsl_rng_free(q); /*  deallocate  rng */
}

void timestep_Verlet ( int N_atoms, double (*pos)[3],  double (*momentum)[3],
                double (*forces)[3], double m, double dt,
                double cell_length){
  for (int i = 0; i < N_atoms; i++) {
    for (int j = 0; j < 3; j++) {
      /* p(t+dt/2) */
      momentum[i][j] += dt * 0.5 * forces[i][j];
      /* q(t+dt) */
      pos[i][j] += dt * momentum[i][j] / m;
    }
  }
  /* F(t+dt) */
  get_forces_AL( forces, pos, cell_length, N_atoms);
  for (int i = 0; i < N_atoms; i++) {
    for (int j = 0; j < 3; j++) {
      /* p(t+dt/2) */
      momentum[i][j] += dt * 0.5 * forces[i][j];
    }
  }
}

double get_kin_energy ( int N_atoms,  double (*momentum)[3], double m ) {
  double p_sq=0; // momentum squared
  for (int i = 0; i < N_atoms; i++) {
    for (int j = 0; j < 3; j++) {
      p_sq += momentum[i][j] * momentum[i][j];
    }
  }
  return p_sq / (2*m);
}

void get_displacements ( int N_atoms,  double (*positions)[3],
             double (*initial_positions)[3], double disp[]) {
  for (int i = 0; i < N_atoms; i++) {
    for (int j = 0; j < 3; j++) {
      disp[i] += (positions[i][j] - initial_positions[i][j])
            *(positions[i][j] - initial_positions[i][j]);
    }
    disp[i] = sqrt(disp[i]);
  }
}


void get_MSD ( int N_atoms,  int N_times, double all_pos[N_times][N_atoms][3],
                double MSD[N_times]) {
   /* all_pos = positions of all particles at all (saved) times */
   /* outer time index it starts at outer it = 1, since MSD[0] = 0*/
   for (int it = 1; it < N_times; it++) { //
      for (int jt = 0; jt < N_times-it; jt++) { // summed time index
         for (int kn = 0; kn < N_atoms; kn++) { // particle index
            for (int kd = 0; kd < 3; kd++) { // three dimensions
               MSD[it] += (all_pos[it+jt][kn][kd] - all_pos[jt][kn][kd])
                          *(all_pos[it+jt][kn][kd] - all_pos[jt][kn][kd]);
            }
         }
      }
      MSD[it] *= 1/( (double)N_atoms * (N_times-it));
   }
}

void get_vel_corr ( int N_atoms,  int N_times, double all_vel[N_times][N_atoms↩
    ][3],
                double vel_corr[N_times]) {
   /* all_vel = velocity of all particles at all (saved) times */
   for (int it = 0; it < N_times; it++) { //
      for (int jt = 0; jt < N_times-it; jt++) { // summed time index
         for (int kn = 0; kn < N_atoms; kn++) { // particle index
            for (int kd = 0; kd < 3; kd++) { // three dimensions
               vel_corr[it] += (all_vel[it+jt][kn][kd] * all_vel[jt][kn][kd]);
            }
         }
      }
      vel_corr[it] *= 1/( (double)N_atoms * (N_times-it));
   }
}

void get_powerspectrum ( int N_atoms,  int N_times, double all_vel[N_times][↩
    N_atoms][3],
                double pow_spec[N_times]) {
```

```c
   /* all_vel = velocity of all particles at all (saved) times */
   double vel_component[N_times]; // "all_vel[:][i][j]"
   double pow_spec_component[N_times];
   double normalization_factor = 1/( (double)N_atoms * (N_times));
   for (int kn = 0; kn < N_atoms; kn++) { // particle index
    for (int kd = 0; kd < 3; kd++) { // three dimensions
         for (int it = 0; it < N_times; it++) { //
            vel_component[it] = all_vel[it][kn][kd];
          }
          powerspectrum(vel_component, pow_spec_component, N_times);
          for (int iw = 0; iw < N_times; iw++) { // for all frequencies
            pow_spec[iw] += pow_spec_component[iw];
          }
       }
   }
   for (int iw = 0; iw < N_times; iw++) { // for all frequencies
       pow_spec[iw] *= normalization_factor;
    }
}



void copy_mat (int M, int N, double mat_from[M][N], double mat_to[M][N]){
   /* Copies matrix `mat_from` to `mat_to` */
   for (int i = 0; i < M; i++) {
      for (int j = 0; j < N; j++) {
      mat_to[i][j] = mat_from[i][j];
      }
   }
}

void set_zero (int M, int N, double mat[M][N]){
  /* Sets the matrix `mat` to zero */
  for (int i = 0; i < M; i++) {
    for (int j = 0; j < N; j++) {
      mat[i][j] = 0;
    }
  }
}

void scale_mat (int M, int N, double mat[M][N], double alpha){
  /* Scales the matrix `mat` by factor `alpha` */
  for (int i = 0; i < M; i++) {
    for (int j = 0; j < N; j++) {
      mat[i][j] *= alpha;
    }
  }
}
```

B Auxiliary

B.1 Makefile

```
CC = gcc
CFLAGS = -O3 -Wall -Wno-unused-result

LIBS = -lm -lgsl -lgslcblas

HEADERS = initfcc.h alpotential.h funcs.h fft_func.h
OBJECTS = initfcc.o alpotential.o funcs.o fft_func.o


%.o: %.c $(HEADERS)
    $(CC) -c -o $@ $< $(CFLAGS)

all: Task1 Task2 Task3 main_Prod.c

Task1: $(OBJECTS) main_T1.c
    $(CC) -o $@ $^ $(CFLAGS) $(LIBS)

Task2: $(OBJECTS) main_T2.c
    $(CC) -o $@ $^ $(CFLAGS) $(LIBS)

Task3: $(OBJECTS) main_T3.c
    $(CC) -o $@ $^ $(CFLAGS) $(LIBS)

Prod: $(OBJECTS) main_Prod.c
    $(CC) -o $@ $^ $(CFLAGS) $(LIBS)

# $(PROGRAMS): $(OBJECTS) main_T1.c
#    $(CC) -o $@ $^ $(CFLAGS) $(LIBS)

clean:
```

```
    rm -f *.o
    touch *.c
```

C Matlab scripts

C.1 Analysis scripts for tasks 3-7: `Al_energies.m`

```
tmp = matlab.desktop.editor.getActive; %% cd to current path
cd(fileparts(tmp.Filename));
set(0,'DefaultFigureWindowStyle','docked');
GRAY = 0.7*[0.9 0.9 1];
warning('off','MATLAB:handle_graphics:exceptions:SceneNode'); % interpreter warning
%% task 1: lattice energies
clc

energy_data = load('../data/lattice_energies.tsv');
a0 = energy_data(:,1);
v0 = a0.^3;

energy = energy_data(:,2);
figure(1);clf;
plot(v0,energy, 'xk');

start_v = 64;
end_v = 68;
indToInclude = (v0 > start_v) & (v0 < end_v);
p = polyfit(v0(indToInclude),energy(indToInclude),2);
hold on;

vvec = linspace(start_v, end_v);
plot(vvec, p(1)*vvec.^2 + p(2)*vvec + p(3), '-r');
xlim([64 68]);

v_min = -p(2)/(2*p(1));
a_min = v_min^(1/3);

ax = gca;
ax.YLim = [-13.45 -13.42];
h1 = plot( v_min*[1 1], ax.YLim, '--k'); % plot vertical line at v_min


ax.YTick = (-13.45:0.01:-13.42);
ylabel('$E_{\rm pot}$ [eV/unit cell]');
xlabel('$a_0^3$ [\AA$^3$]');
legend('data', 'quadratic fit', ['$V_{\rm eq} \approx \, $' num2str(round(v_min,2)) '\, \AA$^3$'], ...
    'location', 'southeast')
ax = gca; ax.Children = ax.Children(3:-1:1);
ImproveFigureCompPhys(gcf); h1.LineWidth = 2; setFigureSize(gcf, 300, 600);

%axis([63 68 ylim(1) 0]);
saveas(gcf, '../figures/potential_energy.eps', 'epsc')

%% task 2: find a suitable timestep
clc;clf;

dt=[1e-2,5e-3,2e-3,1e-3];
figure(1);clf;figure(2);clf;
for i=1:4
    T_data = load(sprintf('../data/temperature_dt-%0.0e_Task2.tsv',dt(i)));
    E_data = load(sprintf('../data/total_energy_dt-%0.0e_Task2.tsv',dt(i)));
    t = T_data(:,1);
    T = T_data(:,2);
    E = E_data(:,2);

    t_eq=0.5;

    fprintf('dt = %0.0e\n',dt(i));

    T_avg=mean(T(t>t_eq));
    T_std=std(T(t>t_eq));
    fprintf('\tT = %0.2f +- %0.1f %%\n', T_avg, abs(T_std/T_avg)*100);

    E_avg=mean(E(t>t_eq));
    E_std=std(E(t>t_eq));
    fprintf('\tE = %0.2f +- %0.1e %%\n', E_avg, abs(E_std/E_avg)*100);

    figure(1)
    plot(t, T); hold on;

    %yyaxis right
    figure(2)
    plot(t, E);hold on;
```

```
    %ylim(E_avg*(1+0.001*[1,-1]));
end
for ifig = 1:2
    figure(ifig);
    h = legend(strcat({'$dt = $ '}, num2str(round(dt',4)) , ' ps'));
    xlabel('$t$ [ps]');
    if ifig ==1
        ylabel('$T$ [K]')
    else
        ylabel('$E_{\rm tot}$ [eV/unit cell]');
        ax = gca; ax.YTick = (-13:0.1:-10);
        ax.YLim = [-12.6 -12.2];
        %h.Location = 'best';
    end
    ImproveFigureCompPhys(gcf,'Linewidth', 2);setFigureSize(gcf, 400, 400);
end
saveas(1, '../figures/dt-scan-temperature.eps', 'epsc')
saveas(2, '../figures/dt-scan-energy.eps', 'epsc')

%% task 3: temperature and pressure equilibration,
% and task4: test production pressure and temperature

clc; clf;
temps = [500 700 500 700];
temperatures_str = num2str([500;700]);
FILENAMES = [strcat({'../data/temp-'}, temperatures_str, '_pres-1_Task3.tsv');
    strcat({'../data/temp-'}, temperatures_str, '_pres-1_Prod-test.tsv')];
bar = 6.2415e-07;
Kelvin_to_degC = -273.15;
t_eqs = [1 1 0.5 0.5]; % approximate equilibration time
N_average_points = 50;
dt = 5e-3;
tau_equilibration = 100*dt;

for iFile = 1:numel(FILENAMES)
    figure(iFile);clf;
    data = load(FILENAMES{iFile});

    t = data(:,1);
    T = data(:,2)+Kelvin_to_degC;
    P = data(:,3)/bar;

    t_eq=t_eqs(iFile);

    %fprintf('dt = %0.0e\n',dt(i));
    T_avg=mean(T(t>t_eq));
    T_std=std(T(t>t_eq));
    fprintf('\tT = %0.2f +- %0.1f K\n', T_avg, abs(T_std));

    P_avg=mean(P(t>t_eq));
    P_std=std(P(t>t_eq));
    fprintf('\tP = %0.2f +- %0.1f bar\n', P_avg, abs(P_std));

    yyaxis left

    if iFile <=2 % equlibration run, otherwise production
        plot(t./tau_equilibration,T, 'color', GRAY),hold on;
        plot(t./tau_equilibration, movmean(T,N_average_points),'-k')
    else
        plot(t,T, 'color', GRAY),hold on;
        plot(t, cumsum(T)./(1:length(t))','-k')
    end
    ylabel('$T \, [^\circ \rm C]$')


    if iFile <=2 % equlibration run, otherwise production
        ylim(temps(iFile)*(1+ 0.3*[-1,1.2]))
        yyaxis right
        plot(t./tau_equilibration,P),hold on;
        plot(t./tau_equilibration, movmean(P,N_average_points),'-k')
        legend('$\mathcal{T}$', 'mov avg','$\mathcal{P}$', 'mov avg');
        xlabel('$t/\tau_{\rm eq}$')
        xlim([0 5])
    else
        ylim(temps(iFile)+ 100*[-3,3])
        yyaxis right
        plot(t,P),hold on;
        plot(t, cumsum(P)./(1:length(t))','-k')
        legend('$\mathcal{T}$', 'cum avg','$\mathcal{P}$', 'cum avg');
        xlabel('$t$\, [ps]')
    end
    ylabel('$P \,[\rm bar]$')
    ylim([-100,400])
    ImproveFigureCompPhys(gcf, 'linewidth', 3, 'LineColor', {'MYORANGE', GRAY, '↩
        MYBLUE', GRAY}');
    setFigureSize(gcf, 400, 400);
end

saveas(1, '../figures/TP-eq-500.eps', 'epsc')
saveas(2, '../figures/TP-eq-700.eps', 'epsc')
saveas(3, '../figures/TP-prod-500.eps', 'epsc')
```

```
saveas(4, '../figures/TP-prod-700.eps', 'epsc')


%% determine displacements and MSD
temperatures_str = num2str([500;700]);
clc; clf;
figure(10); clf;
FILENAMES = strcat({'../data/temp-'}, temperatures_str, '_pres-1_displacements.tsv');
FILENAMES_Dyn = strcat({'../data/temp-'}, temperatures_str, '_pres-1_dynamicProperties.tsv');
FILENAMES_Pow = strcat({'../data/temp-'}, temperatures_str, '_pres-1_power-spectrum.tsv');
for iFile = 1:numel(FILENAMES)

    figure(iFile); clf;
    data = load(FILENAMES{iFile});
    t = data(:,1);
    dx = data(:,2:end);



    data = load(FILENAMES_Dyn{iFile});
    MSD = data(:,2);
    vel_corr = data(:,3);
    plot(t, MSD, 'k'); hold on;

    if iFile ==2 % liquid
        tStart = 1;
        D = MSD(t>tStart)./(6*t(t>tStart));
        selfDiffusionCoeff = mean(D); % in   ^2 /ps
        plot(t, 6*t*selfDiffusionCoeff, ':r');
    end

    plot(t, dx.^2, 'color', GRAY); hold on;

    xlabel('$t$ [ps]')
    ylabel('$\Delta x^2 \,[\rm \AA^2]$')
    if iFile ==1
        ylim([ 0 1.0]);
        leg = legend( '$\Delta_{\rm MSD}$', 'individual trajectories');
    else
        ylim([0 20]);
        leg = legend('$\Delta_{\rm MSD}$', '$6 t D_s$', 'individual trajectories');
    end



    leg.Location='northwest';
    ImproveFigureCompPhys(gcf, 'Linewidth', 2);
    ax = gca; [ax.Children(6:end).LineWidth] = deal(5);
    ax.Children = ax.Children([6:end 1:5]);

    setFigureSize(gcf, 400, 400);

    figure(10)
    plot(t, vel_corr/vel_corr(1), 'color', GRAY); hold on;
    xlim([0 0.8])

end

% % velocity correlation
figure(10);clf; figure(11);clf;
n_average_points = 1;%30;
for iFile = 1:numel(FILENAMES)
    data = load(FILENAMES_Dyn{iFile});
    t = data(:,1);
    vel_corr = data(:,3);

    data = load(FILENAMES_Pow{iFile});
    freq = data(:,1);
    pow_spec = data(:,2);

    figure(10);
    plot(t, vel_corr/vel_corr(1)); hold on;

    dt = t(2)-t(1);
    N_times = round(length(t)/2); % we have too bad statistics at later times.
    deltaf = 1/(N_times * dt);
    freqvec = 0:deltaf:(1/(2*dt));
    PhiHat = 2 * trapz(t(1:N_times), (vel_corr(1:N_times) * ones(size(freqvec)))
          .*     cos(2*pi*t(1:N_times) * freqvec ), 1); %dimension 1
    %PhiHat =  1/2 * 1/N_times * 2 * sum( (vel_corr(1:N_times) * ones(size(freqvec))) .* cos(2*pi*t(1:N_times) * freqvec ), 1); %dimension 1

    figure(11);

    plot(freqvec, PhiHat); hold on;
    plot(freq, pow_spec*t(end), ':'); hold on;
    if iFile ==2 % liquid
```

```
        tStart = 1;
        selfDiffusionCoeff_spectral = PhiHat(1)/6; % in   ^2 /ps
    end

end

disp([selfDiffusionCoeff selfDiffusionCoeff_spectral]);

figure(10)
xlim([0 1])
leg = legend(strcat({'$T='}, num2str([500;700]), '\,^\circ $C'));
leg.Location='northeast';
xlabel('$t$ [ps]')
ylabel('$\Phi (t)/\Phi(0)$')
ImproveFigureCompPhys(gcf);
setFigureSize(gcf, 400, 400);

figure(11)
leg = legend('$T= 500 \, ^\circ $C, $ \hat \Phi$' , '$T= 500 \, ^\circ $C, $\hat P$',...
    '$T= 700 \, ^\circ $C, $ \hat \Phi$', '$T= 700 \, ^\circ $C, $\hat P$');
xlim([0 30])
ylim([0 Inf])
xlabel('$f$ [ps$^{-1}$]')
ylabel('$\hat P$ [\AA$^2$/ps] ')
setFigureSize(gcf, 400, 400);

ImproveFigureCompPhys(gcf,'LineColor', {'r', 'MYRED', 'GERIBLUE','MYLIGHTBLUE'});



saveas(1, '../figures/MSD-500.eps', 'epsc')
saveas(2, '../figures/MSD-700.eps', 'epsc')
saveas(10, '../figures/Phi-t.eps', 'epsc')
saveas(11, '../figures/P-freq.eps', 'epsc')
```

C.2 Improve figure appearance: `ImproveFigureCompPhys.m`

```
function ImproveFigureCompPhys(varargin)
%ImproveFigureCompPhys Improves the figures of supplied handles
%  Input:
% - none (improve all figures) or handles to figures to improve
% - optional:
%       LineWidth  int
%       LineStyle  column vector cell, e.g. {'-','--'}',
%       LineColor  column vector cell, e.g. {'k',[0 1 1], 'MYBLUE'}'
%                           colors: MYBLUE,MYORANGE,MYGREEN,MYPURPLE, MYYELLOW,
%                           MYLIGHTBLUE, MYRED
%       Marker column vector cell, e.g. {'.', 'o', 'x'}'

% ImproveFigure was originally written by Adam Stahl, but has been heavily
% modified by Linnea Hesslow


%%% Handle inputs
% If no inputs or if the first argument is a string (a property rather than
% a handle), use all open figures
if nargin == 0 || ischar(varargin{1})
    %Get all open figures
    figHs = findobj('Type','figure');
    nFigs = length(figHs);
else
    % Check the supplied figure handles
    figHs = varargin{1};
    figHs = figHs(ishandle(figHs) == 1); %Keep only those handles that are proper graphics handles
    nFigs = length(figHs);
end

% Define desired properties
titleSize = 24;
interpreter = 'latex';
lineWidth = 4;
axesWidth = 1.5;
labelSize = 22;
textSize = 20;
legTextSize = 18;
tickLabelSize = 18;
LineColor = {};
LineStyle = {};
Marker = {};

% define colors
co =  [ 0    0.4470    0.7410
```

```
    0.8500    0.3250    0.0980
    0.9290    0.6940    0.1250
    0.4940    0.1840    0.5560
    0.4660    0.6740    0.1880
    0.3010    0.7450    0.9330
    0.6350    0.0780    0.1840 ];
colors = struct('MYBLUE', co(1,:),...
    'MYORANGE', co(2,:),...
    'MYYELLOW', co(3,:),...
    'MYPURPLE', co(4,:),...
    'MYGREEN', co(5,:),...
    'MYLIGHTBLUE', co(6,:),...
    'MYRED',co(7,:),...
    'GERIBLUE', [0.3000    0.1500    0.7500],...
    'GERIRED', [1.0000    0.2500    0.1500],...
    'GERIYELLOW', [0.9000    0.7500    0.1000],...
    'LIGHTGREEN', [0.4    0.85    0.4],...
    'LINNEAGREEN', [7 184 4]/255);

% Loop through the supplied arguments and check for properties to set.
for i = 1:nargin
    if ischar(varargin{i})
        switch lower(varargin{i})   %Compare lower case strings
            case 'linewidth'
                lineWidth = varargin{i+1};
            case 'linestyle'
                LineStyle = varargin{i+1};
            case 'linecolor'
                LineColor = varargin{i+1};
                for iLineColor = 1:numel(LineColor)
                    if isfield(colors, LineColor{iLineColor})
                        LineColor{iLineColor} = colors.(LineColor{iLineColor});
                    end
                end
            case 'marker'
                Marker = varargin{i+1};
        end
    end
end
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

%%% Improve the figure(s)

for iFig = 1:nFigs

    fig = figHs(iFig);

    lineObjects = findall(fig, 'Type', 'line');
    textObjects = findall(fig, 'Type', 'text');
    axesObjects = findall(fig, 'Type', 'axes');
    legObjects =  findall(fig, 'Type', 'legend');
    contourObjects = findall(fig,'Type','contour'); % not counted as lines

    %%% TEXT APPEARANCE: first set all to textSize and then change the ones
    %%% that need to be changed again

    %Change size of any text objects in the plot
    set(textObjects,'FontSize',textSize);
    set(legObjects,'FontSize',legTextSize);

    %%% FIX LINESTYLE, COLOR ETC. FOR EACH PLOT SEPARATELY
    for iAx =  1:numel(axesObjects)
        lineObjInAx = findall(axesObjects(iAx), 'Type', 'line');

        %set line style and color style (only works if all figs have some
        %number of line plots..)
        if ~isempty(LineStyle)
            set(lineObjInAx, {'LineStyle'}, LineStyle)
            set(contourObjects, {'LineStyle'}, LineStyle); %%%%%%
        end
        if ~isempty(LineColor)
            set(lineObjInAx, {'Color'}, LineColor)
            set(contourObjects, {'LineColor'}, LineColor); %%%%%%
        end
        if ~isempty(Marker)
            set(lineObjInAx, {'Marker'}, Marker)
            set(lineObjInAx, {'Markersize'}, num2cell(10+22*strcmp(Marker, '.'))↩
                )
        end

        %%% change font sizes.
        % Tick label size
        xLim = axesObjects(iAx).XLim;
        axesObjects(iAx).FontSize = tickLabelSize;
        axesObjects(iAx).XLim = xLim;
        %Change label size
        axesObjects(iAx).XLabel.FontSize = labelSize;
        axesObjects(iAx).YLabel.FontSize = labelSize;

        %Change title size
        axesObjects(iAx).Title.FontSize = titleSize;
```

```
    end

    %%% LINE APPEARANCE
    %Change line thicknesses
    set(lineObjects,'LineWidth',lineWidth);
    set(contourObjects, 'LineWidth', lineWidth);
    set(axesObjects, 'LineWidth',axesWidth)

    % set interpreter: latex or tex
    set(textObjects, 'interpreter', interpreter)
    set(legObjects, 'Interpreter', interpreter)
    set(axesObjects,'TickLabelInterpreter', interpreter);
end
end
```

C.3 Change size of figures: `setFigureSize.m`

```
function [ fig ] = setFigureSize( fig, H, W )
fig.Units = 'points';
fig.WindowStyle = 'normal'; % undock
fig.Position(3:4) = [W H];
end
```