Lab 2: INS and Kalman Filter

TTK5: Kalman Filtering and Navigation

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Task 1

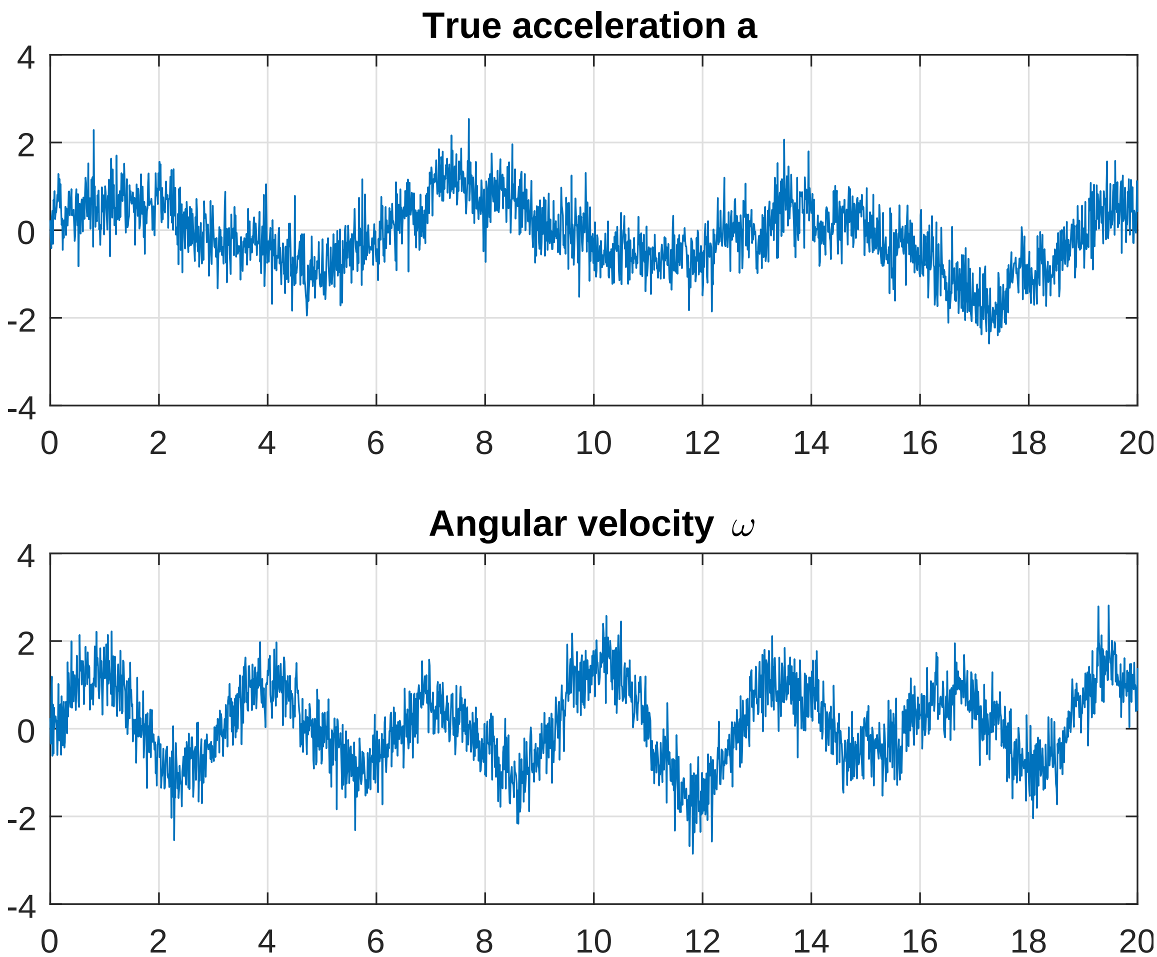

Figure 1: True acceleration and angular velocity.

Task 2

In order to discretize the system, it must first be written as a state space model. The system

$$\dot{x} = v \tag{1a}$$

$$\dot{v} = a \tag{1b}$$

$$\dot{\theta} = \omega \tag{1c}$$

can be written as

$$\dot{\boldsymbol{x}} = \boldsymbol{A}\boldsymbol{x} + \boldsymbol{B}\boldsymbol{u} \tag{2a}$$

$$\begin{bmatrix} \dot{x} \\ \dot{v} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} x \\ v \\ \theta \end{bmatrix} + \begin{bmatrix} 0 & 0 \\ 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} a \\ \omega \end{bmatrix}. \tag{2b}$$

By using forward Euler to discretize the system, it can be written on the form

$$\boldsymbol{x}(t_{k+1}) = (\boldsymbol{I} + h\boldsymbol{A}(t_k)\boldsymbol{x}(t_k)) + h\boldsymbol{B}(t_k)\boldsymbol{u}(t_k) \tag{3}$$

where h is the step size. The discretized system then becomes

$$\boldsymbol{x}(t_{k+1}) = \begin{bmatrix} 1 & h & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \boldsymbol{x}(t_k) + \begin{bmatrix} 0 & 0 \\ h & 0 \\ 0 & h \end{bmatrix} \boldsymbol{u}(t_k). \tag{4}$$

Figure 2 shows plots of the states in the discretized system.

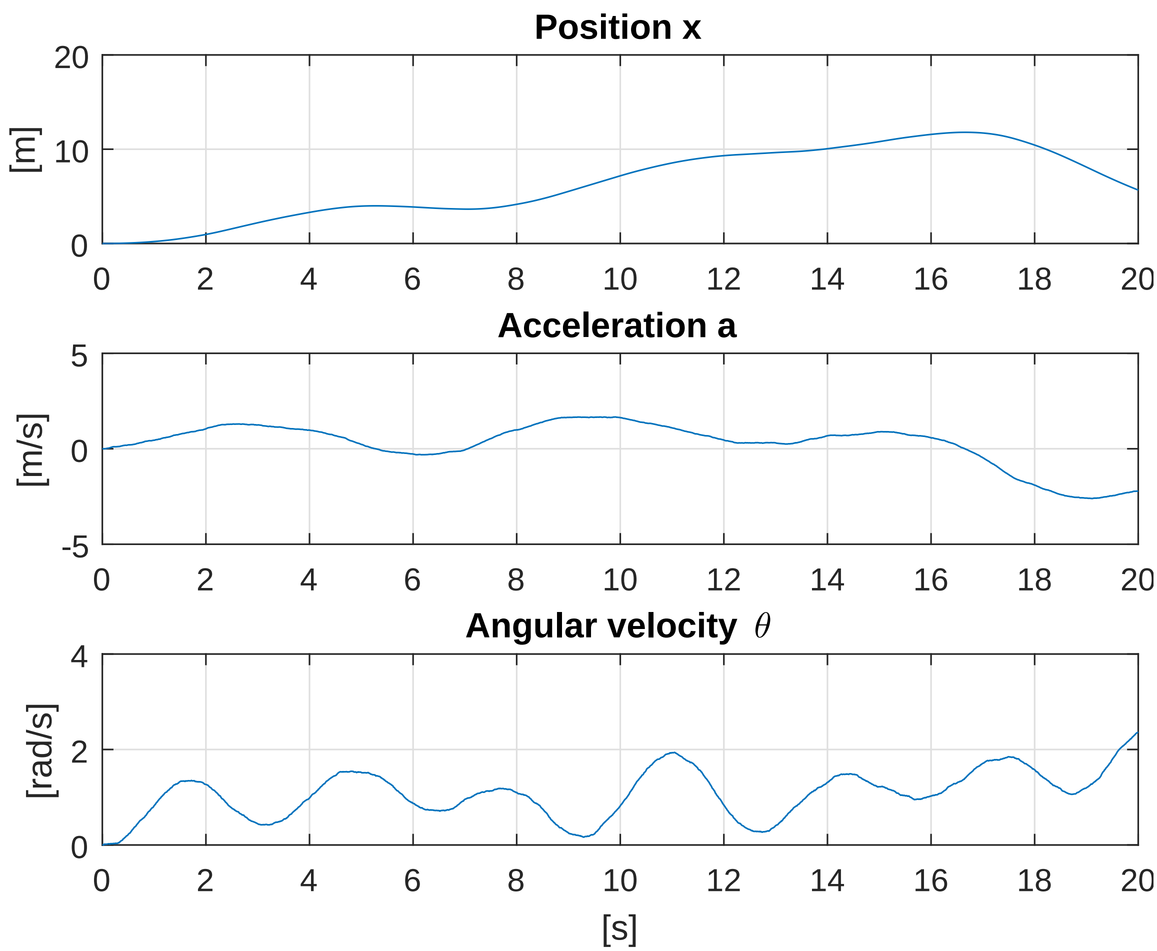

Figure 2: States of the discretized system.