Theorem: The Hessian of a composition of maps $\psi \circ \phi : M \to N \to P$ is $\nabla d(\psi \circ \phi) = (\nabla d\psi)\,(d\phi, d\phi) + d\psi \circ (\nabla d\phi)$.

Proof:

$\square$