

```
function prob4(N)
```

```
%NODES
```

```
nodes = zeros((N+1)^2 , 3);
```

```
%nodes(k,1), nodes(k,2) are the x, y coordinates of the kth node  
%nodes(k,3) is 1 if the kth node is free, or else -1 if the node is  
constrained
```

```
[X, Y] = meshgrid(1:(N-1),1:(N-1));
```

```
X=(X')/N; Y=(Y')/N; %for renormalizing into the unit square
```

```
nodes(1:((N-1)^2),1) = reshape(X, (N-1)^2, 1);
```

```
nodes(1:((N-1)^2),2) = reshape(Y, (N-1)^2, 1);
```

```
nodes(1:((N-1)^2),3) = ones((N-1)^2,1);
```

```
%bottom boundary points
```

```
nodes(((N-1)^2+1):((N-1)^2+N),1) = ([0:(N-1)]') ./ N; %x coords
```

```
nodes(((N-1)^2+1):((N-1)^2+N),2) = zeros(N,1); %y coords
```

```
nodes(((N-1)^2+1):((N-1)^2+N),3) = -ones(N,1);
```

```
%right boundary nodes
```

```
nodes(((N-1)^2+N+1):((N-1)^2+2*N),1) = ones(N,1); %x coords
```

```
nodes(((N-1)^2+N+1):((N-1)^2+2*N),2) = ([0:(N-1)]') ./ N; %y coords
```

```
nodes(((N-1)^2+N+1):((N-1)^2+2*N),3) = -ones(N,1);
```

```
%top boundary nodes
```

```
nodes(((N-1)^2+2*N+1):((N-1)^2+3*N),1) = flipud([1:N] ./ N)'; %x  
coords
```

```
nodes(((N-1)^2+2*N+1):((N-1)^2+3*N),2) = ones(N,1); %y coords
```

```
nodes(((N-1)^2+2*N+1):((N-1)^2+3*N),3) = -ones(N,1); %y coords
```

```
%left boundary nodes
```

```
nodes(((N-1)^2+3*N+1):((N-1)^2+4*N),1) = zeros(N,1); %x coords
```

```
nodes(((N-1)^2+3*N+1):((N-1)^2+4*N),2) = flipud([1:N] ./ N)'; %y  
coords
```

```
nodes(((N-1)^2+3*N+1):((N-1)^2+4*N),3) = -ones(N,1); %x coords
```

```
% TRIANGLES
```

```
triangles = zeros(2*N^2,3);
```

```
% triangle(k,i) records the global node number of the ith local node of  
triangle k
```

```
%auxilliary definitions
```

```
triangle_coords = zeros(2*N^2,6);
```

```
oddtriangle = [0,1/N, 0, 0, 1/N, 1/N]; %equal to triangle_coords(1,:)
```

```
eventriangle = [1/N, 0, 1/N, 1/N, 0, 0]; %equal to triangle_coords(2,:)
```

```
% provides coordinates for triangles
```

```
% e.g., triangle_coords(k,:) = [(x1,y1), (x2,y2), (x3,y3)], where (xi,yi)  
are the coordinates for the ith local node of triangle k
```

```
% every odd/even triangle given the same info as triangle 1/2, resp.
```

```
triangle_coords = (mod(1:2*N^2,2))' * oddtriangle + ((1-mod(1:2*N^2,2))' *  
eventriangle;
```

```
% each odd triangle info shifted by appropriate amount - x and then y  
coordinates
```

```
triangle_coords = triangle_coords + ((mod(1:2*N^2,2) .* (mod((1:2*N^2)-1,2*N)  
/2))' * [1/N, 0, 1/N, 0, 1/N, 0];
```

```
triangle_coords = triangle_coords + ((mod(1:2*N^2,2) .* (floor(((1:2*N^2)-1)/  
(2*N)))') * [0, 1/N, 0, 1/N, 0, 1/N];
```

```
% each even triangle info shifted by appropriate amount - x and then y
```

coordinates

```
triangle_coords = triangle_coords + (((1-mod(1:2*N^2,2)).*(mod((1:2*N^2)-2,2)*N)/2))'*[1/N, 0, 1/N, 0, 1/N, 0];
triangle_coords = triangle_coords + (((1-mod(1:2*N^2,2)).*(floor(((1:2*N^2)-1)/(2*N))))'*[0, 1/N, 0, 1/N, 0, 1/N];
```

% adjust for special top left and bottom right corners

```
BRL = [triangle_coords(2*N-1,3:4), triangle_coords(2*N,1:2), triangle_coords(2*N-1,1:2)];
BRR = [triangle_coords(2*N,3:4), triangle_coords(2*N-1,1:2), triangle_coords(2*N,1:2)];
triangle_coords(2*N-1,:) = BRL;
triangle_coords(2*N,:) = BRR;
TLL = [triangle_coords(2*(N-1)*N+1,3:4), triangle_coords(2*(N-1)*N+2,1:2), triangle_coords(2*(N-1)*N+1,1:2)];
TLR = [triangle_coords(2*(N-1)*N+2,3:4), triangle_coords(2*(N-1)*N+1,1:2), triangle_coords(2*(N-1)*N+2,1:2)];
triangle_coords(2*(N-1)*N+1,:) = TLL;
triangle_coords(2*(N-1)*N+2,:) = TLR;
```

```
for k=1:(2*N^2)
    for l=1:3
        test=(abs(nodes(:,1)-triangle_coords(k,2*l-1))<eps).*(abs(nodes(:,2)-triangle_coords(k,2*l))<eps);
        triangles(k,l)=(1:((N+1)^2))*test;
    end
end
```

%VISUALIZE MESH

```
for k=1:(2*N^2)
    plot(triangle_coords(k,[1, 3]), triangle_coords(k,[2, 4])); hold on;
    plot(triangle_coords(k,[3, 5]), triangle_coords(k,[4, 6])); hold on;
    plot(triangle_coords(k,[5, 1]), triangle_coords(k,[6, 2])); hold on;
end
```

nodes
triangles