

RobertRash_MATH3316_Project4

November 30, 2017

0.1 Project 4 - Numerical Integration

Robert Rash MATH3316 7 December 2017

0.2 Introduction

0.2.1 Project Structure

```
In [1]: %ls ..
```

```
MATH3316-Project4.xcodeproj/ lib/  
Makefile                      res/  
bin/                          src/  
doc/
```

Excluding the .xcodeproj file, which was used for integration with the Xcode IDE, debugging, and profiling purposes, each item in the project directory serves the following purpose:

- Makefile: GNU Make project build automation definitions.
- bin/: compiled binaries. Make will put binaries here by default.
- doc/: directory containing all documentation, including this report.
- lib/: reused libraries that are not part of this project specifically. Contains a rewrite of the Matrix library ([phrz/matrix](#)).
- res/: where calculated data is stored after program execution. Files are .txt files containing real numbers, space delimited to denote row items, and newline delimited to denote new rows. For this project, the .txt files are also organized into separate res/part{1..3}/ directories.
- src/: contains the C++ implementations of the calculations described in this report.

0.2.2 Using this Project

Prerequisites

- A Unix or Unix-like OS (e.g. macOS or Linux)
- A compiler with support for C++14 (LLVM or GNU toolchain)
- Python 3.5
- The latest Jupyter distribution
 - matplotlib

- LaTeX with pdf_latex
- GNU Make 3.81

Building this project `make all` (default) - will compile binaries, execute them to generate data files, execute Jupyter notebooks with new data files, and convert them to PDFs in `res/reports/`.

`make all_bin` - will compile binaries for part 1 and 2 of this project.

`make all_data` - will compile binaries and execute them to generate data files.

`make clean` - will delete all compiled binaries, generated data, executed notebook copies (but not the original notebooks), and report PDFs.

0.3 Part 1 - Trapezoid Rule and Simpson's Rule

0.3.1 Background

0.3.2 Implementation

0.4 Part 2 - Application

In this section, we focus on interpolation using the Newton form in addition to the resulting error analysis relative to the function as calculated using the built-in function.

0.4.1 Background

0.4.2 Implementation

0.4.3 Analysis

```
In [2]: %pylab inline
        pylab.rcParams['figure.figsize'] = (10,6)
        matplotlib.rcParams.update({'font.size': 16})
        matplotlib.rcParams.update({'axes.labelsize': 20})
        matplotlib.rcParams.update({'xtick.labelsize': 12})
        matplotlib.rcParams.update({'ytick.labelsize': 12})
        matplotlib.rcParams.update({
            'font.family': 'Helvetica, Arial, sans-serif'
        })
```

Populating the interactive namespace from numpy and matplotlib

```
In [3]: names = [ 'carbon_1', 'carbon_2', 'carbon_10', 'carbon_40' ]
        data = {name: loadtxt('../res/part2/'+name+'.txt') for name in names}
        data['x'] = linspace(0,3,200)
```

```
In [4]: # plot  $C(x, t)$  versus  $x$  for each specified value of  $t$ 
        # and overlay the four curves (corresponding to four
        # values of  $t$ ) in one figure

        pylab.plot(data['x'], data['carbon_1'])
        pylab.plot(data['x'], data['carbon_2'])
        pylab.plot(data['x'], data['carbon_10'])
```

```

pylab.plot(data['x'], data['carbon_40'])

pylab.title('Concentration of carbon  $C(x,t)$  in a piece of steel,  $x \in [0, 3]$ ,  $t \in \{1, 2, 10, 40\}$ ')
pylab.xlabel('$x$')
pylab.ylabel('$C(x,t)$')
pylab.grid()

pylab.legend(('C(x, 1)',
              'C(x, 2)',
              'C(x, 10)',
              'C(x, 40)'))

```

Out[4]: <matplotlib.legend.Legend at 0x10bd5d390>

Concentration of carbon $C(x, t)$ in a piece of steel, $x \in [0, 3]$, $t \in \{1, 2, 10, 40\}$

