An Example Article*

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Abstract

This is an example LaTeX article. This can be used as a template for new articles. Abstracts must be able to stand alone and so cannot contain citations to the paper's references, equations, etc. An abstract must consist of a single paragraph and be concise. Because of online formatting, abstracts must appear as plain as possible. Any equations should be inline.

Keywords: Example, LaTeX, numerical methods

2000 Mathematics Subject Classification: 65L60, 65L05, 65L70.

1 Introduction

The introduction introduces the context and summarizes the manuscript. It is importantly to clearly state the contributions of this piece of work.

In this paper we present a new method for solving the model equation

$$\begin{cases} \partial_t u - \varepsilon^2 \Delta u + u^3 - u = 0, & \text{in } \Omega \times \mathcal{T}, \\ u(x,y,t) = g(t), & \text{on } \partial\Omega, \\ u(x,y,0) = \varphi(x,y), & \text{on } \Omega. \end{cases} \tag{1.1}$$

where ε is a small parameter.

This is an example of quoting an equation (1.1).

The merits of our method are as follows:

- item one

- item two

1. item one

2. item two

The outline is not required, but we show an example here.

The paper is organized as follows. Our main results are in 2, our new algorithm is in 3, experimental results are in 4, discussion is in 5 and the conclusions follow in 6.

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2 Main results

We interleave text filler with some example theorems and theorem-like items.

Definition 2.1. This is a definition environment.

Lemma 2.1. *This is a lemma environment.*

Theorem 2.1. *This is a theorem environment.*

Proof. This is a proof environment. □

Lemma 2.2. *This is a lemma environment*

   (i) *item A*

   (ii) *item B*

$$\lim_{n\to\infty} \left(1 + \frac{1}{n}\right)^n = e. \tag{2.1}$$

This is a citation example [2].

Here we state our main result as 2.2.

Theorem 2.2 (LDL^T Factorization [1])**.** *If $A \in \mathbb{R}^{n \times n}$ is symmetric and the principal submatrix $A(1:k, 1:k)$ is nonsingular for $k = 1 : n-1$, then there exists a unit lower triangular matrix L and a diagonal matrix*

$$D = \mathrm{diag}(d_1, \ldots, d_n),$$

such that $A = LDL^T$. The factorization is unique.

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Theorem 2.3 (Mean Value Theorem)**.** *Suppose f is a function that is continuous on the closed interval $[a, b]$. and differentiable on the open interval (a, b). Then there exists a number c such that $a < c < b$ and*

$$f'(c) = \frac{f(b) - f(a)}{b - a}.$$

In other words,

$$f(b) - f(a) = f'(c)(b - a).$$

Remark 2.1. Observe that 2.2, 2.3 correctly mix references to multiple labels.

Corollary 2.1. *Let $f(x)$ be continuous and differentiable everywhere. If $f(x)$ has at least two roots, then $f'(x)$ must have at least one root.*

Proof. Let a and b be two distinct roots of f. By 2.3, there exists a number c such that

$$f'(c) = \frac{f(b) - f(a)}{b - a} = \frac{0 - 0}{b - a} = 0.$$

□

Note that it may require two LaTeX compilations for the proof marks to show.

Display matrices can be rendered using environments from `amsmath`:

$$S = \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix} \quad \text{and} \quad C = \begin{pmatrix} 1 & 1 & 0 \\ 1 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}. \tag{2.2}$$

Equation 2.2 shows some example matrices.

We calculate the Fréchet derivative of F as follows:

$$\begin{align} F'(U,V)(H,K) &= \langle R(U,V), H\Sigma V^T + U\Sigma K^T - P(H\Sigma V^T + U\Sigma K^T)\rangle \tag{2.3a} \\ &= \langle R(U,V), H\Sigma V^T + U\Sigma K^T\rangle \\ &= \langle R(U,V)V\Sigma^T, H\rangle + \langle \Sigma^T U^T R(U,V), K^T\rangle. \tag{2.3b} \end{align}$$

2.3a is the first line, and 2.3b is the last line.

3 Algorithm

Our analysis leads to the algorithm in 1.

Algorithm 1 Build tree
___

Define $P := T := \{\{1\}, \ldots, \{d\}\}$
while $\#P > 1$ **do**
    Choose $C' \in \mathcal{C}_p(P)$ with $C' := \text{argmin}_{C \in \mathcal{C}_p(P)}\, \varrho(C)$
    Find an optimal partition tree $T_{C'}$
    Update $P := (P \backslash C') \cup \{\bigcup_{t \in C'} t\}$
    Update $T := T \cup \{\bigcup_{t \in \tau} t : \tau \in T_{C'} \backslash \mathcal{L}(T_{C'})\}$
end whilereturn T

Reduce the width of the algorithm environment

Algorithm 2 Euclid's algorithm
___

procedure Euclid(a,b) ▷ The g.c.d. of a and b
    $r \leftarrow a \bmod b$
    while $r \neq 0$ **do**   ▷ We have the answer if r is 0
        $a \leftarrow b$
        $b \leftarrow r$
        $r \leftarrow a \bmod b$
    end while
    return b ▷ The gcd is b
end procedure

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4 Experimental results

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Example 1. This is example environment.

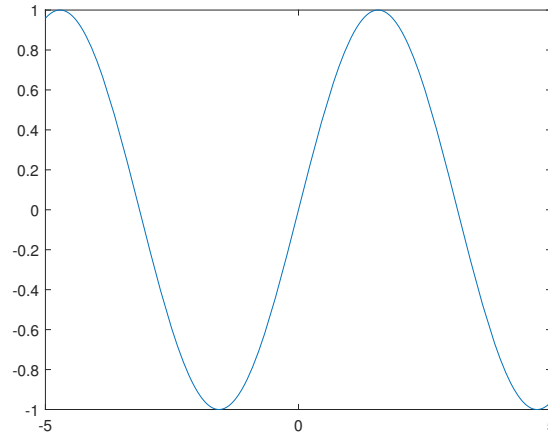Figure 4.1 shows some example results.

Figure 4.1: Example figure using external image files.

The two figures are placed side by side, sharing the same title.
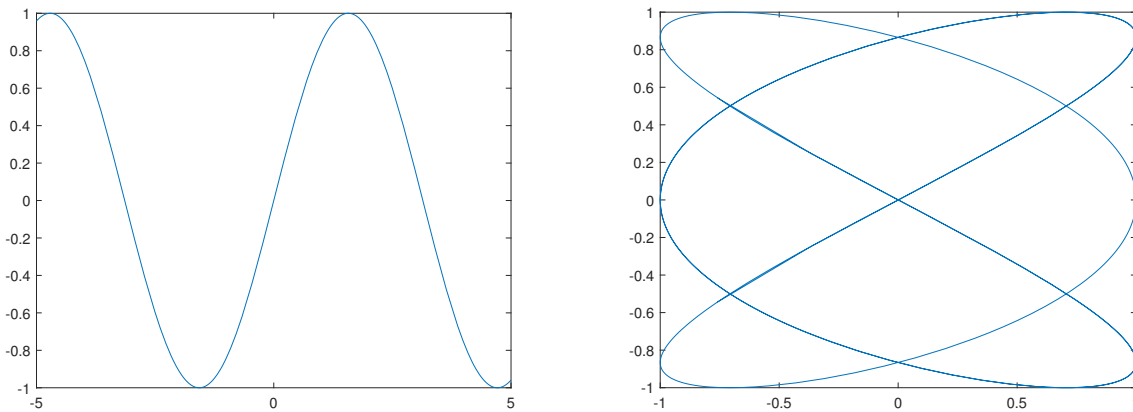

Figure 4.2: Left: Caption 1, Right: Caption 2.

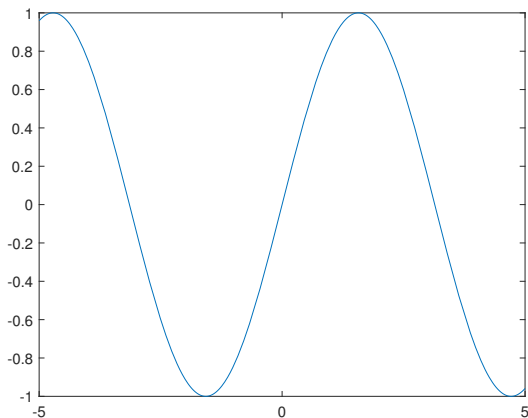Use `minipage` package to set up images side-by-side, each with its own title.
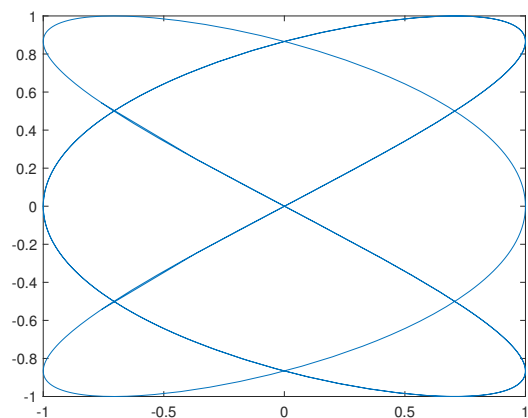

Figure 4.3: Caption A

Figure 4.4: Caption B

Additional results are available in the supplement in Table 4.1.

Table 4.1: Numerical error

degree	step-size h	L^2-errors	order	H^1-errors	order	L^∞-errors	order
	1/128	9.18E-06	2.02	7.70E-03	1.01	6.46E-07	2.02
1	1/256	2.29E-06	2.01	1.92E-03	1.00	1.61E-07	2.01
	1/512	5.70E-07	2.00	9.56E-04	1.00	4.01E-08	2.00
	1/128	1.39E-08	3.01	1.15E-05	2.01	3.48E-12	4.02
2	1/256	1.73E-09	3.01	2.88E-06	2.01	3.27E-13	3.94
	1/512	2.17E-10	3.00	7.24E-06	2.00	6.66E-13	1.55
	1/32	2.28E-09	4.05	6.92E-07	3.04	1.45E-15	8.21
3	1/64	1.42E-10	4.03	8.65E-08	3.02	2.06E-14	3.85
	1/128	8.91E-12	4.01	1.08E-08	3.01	3.86E-14	0.91

Use the `tabularx` environment to generate tables.

Table 4.2: Table description

N	A	B	C	D	E
2	9.20E-05	9.90E-05	1.00E-06	8.00E-06	1.50E-05
4	9.80E-05	8.00E-05	7.00E-06	1.40E-05	1.60E-05
6	4.00E-06	8.10E-05	8.80E-05	2.00E-05	2.20E-05
8	8.50E-05	8.70E-05	1.90E-05	2.10E-05	3.00E-06
10	8.60E-05	9.30E-05	2.50E-05	2.00E-06	9.00E-06
12	1.70E-05	2.40E-05	7.60E-05	8.30E-05	9.00E-05

5 Discussion of $Z = X \cup Y$

Some discussions here. Some discussions here. Some discussions here. Some discussions here. Some discussions here. Some discussions here. Some discussions here. Some discussions here. Some discussions here. Some discussions here. Some discussions here. Some discussions here. Some discussions here. Some discussions here.

6 Conclusions

Some conclusions here.

A An example appendix

The contents of the appendix are here.

Lemma A.1. *Test Lemma.*

This is a equation in appendix.
$$a^2 + b^2 = c^2. \tag{A.1}$$

Acknowledgments

References

[1] Gene H. Golub and Charles F. Van Loan. *Matrix Computations*. The Johns Hopkins University Press, Baltimore, 4th edition, 2013.

[2] Donald E. Woessner, Shanrong Zhang, Matthew E. Merritt, and A. Dean Sherry. Numerical solution of the Bloch equations provides insights into the optimum design of PARACEST agents for MRI. *Magnetic Resonance in Medicine*, 53(4):790–799, April 2005.