k-th Smallest Element in a BST

difficulty: Medium

https://leetcode.com/problems/kth-smallest-element-in-a-bst/

Given a binary search tree, write a function k-thSmallest to find the k-th smallest element in it.

Note:

You may assume k is always valid, $1 \le k \le BST$'s total elements.

Example 1:

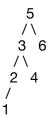
Input: root =
$$[3, 1, 4, \text{null}, 2], k = 1$$



Output: 1

Example 2:

Input: root =
$$[5, 3, 6, 2, 4, \text{null}, \text{null}, 1], k = 3$$



Output: 3

Follow up:

What if the BST is modified (insert/delete operations) often and you need to find the k-th smallest frequently? How would you optimize the k-thSmallest routine?

Constraints:

- The number of elements of the BST is between $1 \text{ to } 10^4$
- You may assume k is always valid, $1 \le k \le BST$'s total elements.