

Egyptian Fractions

In mathematics, a fraction is the rational number $\frac{p}{q}$, where p and q are integers. An Egyptian fraction is a sum of fractions, each with numerator 1 where all denominators are different, e.g. $\frac{1}{2} + \frac{1}{3} + \frac{1}{16}$ is an Egyptian fraction, but $\frac{1}{3} + \frac{1}{3} + \frac{1}{5}$ is not (repeated denominator 3). Every positive fraction ($q \neq 0, p \leq q$) can be represented by an Egyptian fraction, for instance, $\frac{43}{48} = \frac{1}{2} + \frac{1}{3} + \frac{1}{16}$. Given p and q , write a program to represent the fraction $\frac{p}{q}$ as an Egyptian fraction.

Examples

| Input | Output |
|-----------|--|
| 43/48 | 43/48 = 1/2 + 1/3 + 1/16 |
| 3/7 | 3/7 = 1/3 + 1/11 + 1/231 |
| 23/46 | 23/46 = 1/2 |
| 22/7 | Error (fraction is equal to or greater than 1) |
| 134/3151 | 134/3151 = 1/24 + 1/1164 + 1/2445176 |
| 2019/2019 | 2019/2019 = 1/2 + 1/3 + 1/6 |

Note: There may be more than one correct solution, e.g. $3/7 = 1/4 + 1/8 + 1/19 + 1/1064$. If you follow the greedy algorithm logic, you should get the solutions given in the input/output examples.

Hints

You can complete the expression by starting with the biggest fraction with numerator 1 which added to the expression keeps it smaller than or equal to the target fraction. The biggest fraction is the one with smallest denominator – 1/2. Increase the denominator until you've found a solution.