



Search and Sort

Luke Wu



Search



在一個任意排序的 Array 內找尋特定數字

ex: 下列 Array 內是否有 38

[55, 10, 35, 1, 2, 25, 37]



在一個 Sorted Array 內找尋特定數字

ex: 下列 Array 內是否有 38

[1, 2, 10, 25, 35, 37, 55]



Which one is better?



Time Complexity 時間複雜度

- Machine Independent - 運算次數
- 評估**運算次數**與**輸入**之間的關係



Asymptotic Notation - Big “Oh”

- $f(n) = O(g(n))$ iff

- \exists positive const. c and n_0 , $\exists f(n) \leq cg(n) \forall n, n \geq n_0$

- e.g.

- $3n+2 = O(n)$

- $3n+2 \leq 4n$ for all $n \geq 2$

- $10n^2+4n+2 = O(n^2)$

- $10n^2+4n+2 \leq 11n^2$, for all $n \geq 10$

- $3n+2 = O(n^2)$

- $3n+2 \leq n^2$ for all $n \geq 4$

* $g(n)$ should be a least upper bound



Time Complexity

- Linear Search - $O(n)$
- Binary Search(Under sorted array) - $O(\log n)$

* In Complexity, **log** usually stand for **log to the base 2**


```
if (n > 10) {  
    print("n is bigger than 10")  
}
```

$O(n)$

```
for (i = 0; i < n; i++) {  
    print("Hello world")  
}
```

```
for (i = 0; i < 1000; i++) {  
    print("Hello world")  
}
```

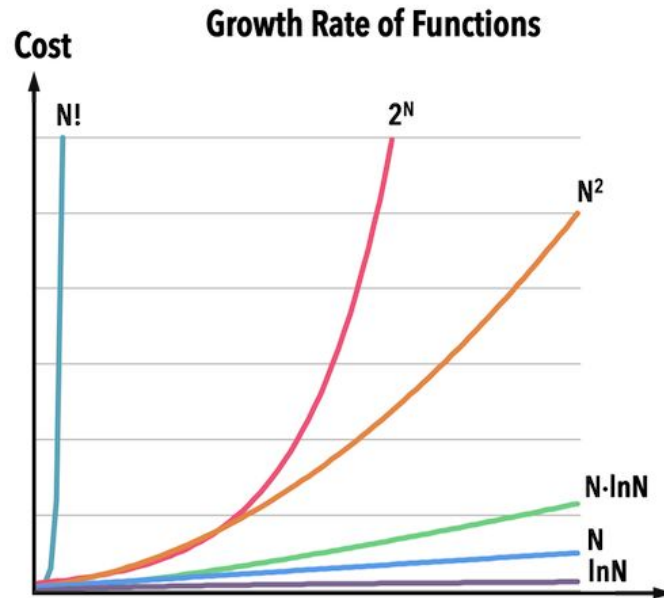
$O(n)$

```
for (i = 0; i < n; i++) {  
    print("AppWorks School")  
}
```

```
for (i = 0; i < n; i++) {  
    for (j = 0; j < i; i++) {  
        print("AppWorks School")  
    }  
}
```

$O(n^2)$

Complexity Compare





Sort



Selection Sort



Pseudo Code

提供足夠詳細的程式執行流程以描述程式的每一個執行步驟，藉以提供程式設計師在接下來把程式以特定的程式語言完成



Insertion Sort



Merge Sort



Time Complexity

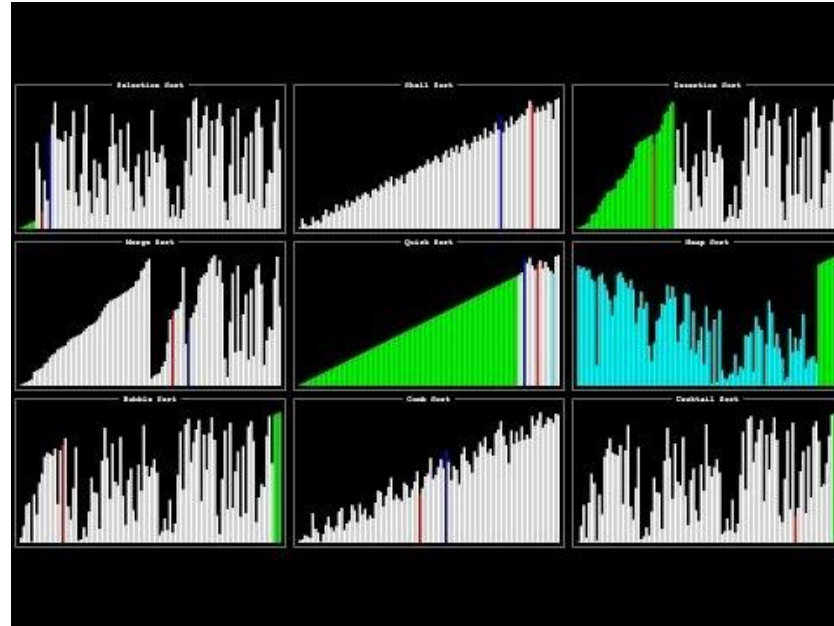
- Selection Sort - $O(n^2)$
- Insertion Sort - $O(n^2)$
- Merge Sort - $O(n \cdot \log n)$



Time Complexity

- Best Case
- Worst Case
- Average Case

Time Complexity





Question - Why Do We Take The First Scenario?

- Merge Sort + Binary Search = $O(n * \log n) + O(\log n)$
- Linear Search = $O(n)$



Reference

- <http://alrightchiu.github.io/SecondRound/mu-lu-yan-suan-fa-yu-zi-liao-jie-gou.html>
- [NCTU Data Structure](#) - 彭文志 教授
- [NTHU Data Structure](#) - 韓永楷 教授