

while-based loops

- ▶ Condition-controlled loops
- ▶ Pre-test vs. post-test loops
- ▶ Operators `++` and `--`

- ▶ `while`
- ▶ `do - while`

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The while loop

- ▶ Structure: `while(condition) statement`
 - `condition` is evaluated
 - If `condition` is true, `statement` is executed
 - This repeats until `condition` becomes false
- ▶ `condition` is checked *before* the block is executed
 - So-called `pre-test` loop
 - No execution of `statement` is possible
- ▶ `statement` can be a block of code
- ▶ Compare with `for(; condition ;)` in `binSearch`

```
1 #include <stdio.h>
2
3 main() {
4     int counter = 5;
5
6     while (counter > 0) {
7         printf("%d ",counter);
8         counter = counter-1;
9     }
10    printf("\n");
11 }
```

- ▶ Output:
5 4 3 2 1

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Operators ++

- ▶ `++a` and `a++` are arithmetically equivalent to `a=a+1`
- ▶ Additional `evaluation` of the variable `a`
- ▶ Pre-increment `++a`
 - First increase, then evaluate
- ▶ Post-increment `a++`
 - First evaluate, then increase

```
1 #include <stdio.h>
2
3 main() {
4     int a = 0;
5     int b = 43;
6
7     printf("1) a=%d, b=%d\n",a,b);
8
9     b = a++;
10    printf("2) a=%d, b=%d\n",a,b);
11
12    b = ++a;
13    printf("3) a=%d, b=%d\n",a,b);
14 }
```

- ▶ Output:
 - 1) a=0, b=43
 - 2) a=1, b=0
 - 3) a=2, b=2

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Operators ++ and --

- ▶ Operators similar to `a++` and `++a`
 - Pre-decrement `--`
 - * First decrease, then evaluate
 - Post-decrement `--`
 - * First evaluate, then decrease
- ▶ Note the difference in condition-controlled loops!

```
1 #include <stdio.h>
2
3 main() {
4     int counter = 5;
5
6     while (--counter>0) {
7         printf("%d ",counter);
8     }
9     printf("\n");
10 }
```

- ▶ Output: 4 3 2 1 (for `--counter` in line 6)
- ▶ Output: 4 3 2 1 0 (for `counter--` in line 6)

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Bisection method (revisited)

► Input

- Continuous function $f : [a, b] \rightarrow \mathbb{R}$ satisfying $f(a)f(b) \leq 0$
- Tolerance $\tau > 0$

► Intermediate value theorem

- There exists $x \in [a, b]$ with $f(x) = 0$

► Task

- Find approximation of a zero of f
- i.e., find $x_0 \in [a, b]$ with the following property:
 $\exists x \in [a, b]$ such that $f(x) = 0$ and $|x - x_0| \leq \tau$

► Bisection method = Interval halving method

- As long as $|b - a| > 2\tau$
 - * Compute midpoint m of $[a, b]$ and $f(m)$
 - * If $f(a)f(m) \leq 0$, consider $[a, m]$
 - * Otherwise consider $[m, b]$
- $x_0 := m$ is the desired approximation

► The method terminates after a finite number of steps

► Convergence towards $x \in [a, b]$ with $f(x) = 0$ as $\tau \rightarrow 0$

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Bisection method (revisited)

```
1 #include <stdio.h>
2 #include <math.h>
3
4 double f(double x) {
5     return x*x + exp(x) -2;
6 }
7
8 double bisection(double a, double b, double tol){
9     double fa = f(a);
10    double m = 0.5*(a+b);
11    double fm = 0;
12
13    while ( b - a > 2*tol ) {
14        m = 0.5*(a+b);
15        fm = f(m);
16        if ( fa*fm <= 0 ) {
17            b = m;
18        }
19        else {
20            a = m;
21            fa = fm;
22        }
23    }
24    return m;
25 }
26
27 main() {
28     double a = 0;
29     double b = 10;
30     double tol = 1e-12;
31     double x = bisection(a,b,tol);
32
33     printf("Approximate zero x=%g\n",x);
34     printf("Function value f(x)=%g\n",f(x));
35 }
```

- Using the variables **fa** and **fm** avoids a double evaluation of **f**

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Euclidean algorithm

► Input: Two integers $a, b \in \mathbb{N}$

► Task: Compute greatest common divisor $\gcd(a, b) \in \mathbb{N}$

► Euclidean algorithm:

- If $a = b$, then $\gcd(a, b) = a$
- If $a < b$, swap a and b
- It holds that $\gcd(a, b) = \gcd(a - b, b)$, because:
 - * Let g a divisor of a, b
 - * i.e., $ga_0 = a$ and $gb_0 = b$ with $a_0, b_0 \in \mathbb{N}$, $g \in \mathbb{N}$
 - * Hence, $g(a_0 - b_0) = a - b$ and $a_0 - b_0 \in \mathbb{N}$
 - * i.e., g divides both b and $a - b$
 - * Hence, $\gcd(a, b) \leq \gcd(a - b, b)$
 - * Similarly, $\gcd(a - b, b) \leq \gcd(a, b)$
- Replace a with $a - b$ and repeat the above steps

► Algorithm yields $\gcd(a, b)$ in finitely many steps:

- If $a \neq b$, $n := \max\{a, b\} \in \mathbb{N}$ becomes smaller at each step
- After finitely many steps, $a \neq b$ does not hold

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Euclidean algorithm

```
1 #include <stdio.h>
2
3 main() {
4     int a = 200;
5     int b = 110;
6     int tmp = 0;
7
8     printf("gcd(%d,%d)=", a, b);
9
10    while (a != b) {
11        if ( a < b ) {
12            tmp = a;
13            a = b;
14            b = tmp;
15        }
16        a = a-b;
17    }
18
19    printf("%d\n", a);
20 }
```

- Computation of gcd of $a, b \in \mathbb{N}$
- Basic idea: $\gcd(a, b) = \gcd(a - b, b)$ for $a > b$
- For $a = b$, it holds that $\gcd(a, b) = a = b$
- Output:
 $\gcd(200, 110) = 10$

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Euclidean algorithm (improved)

- Key part of the previous implementation

```
10 while (a != b) {
11     if (a < b) {
12         tmp = a;
13         a = b;
14         b = tmp;
15     }
16     a = a-b;
17 }
```

- Recall: $a \% b$ is the rest of the integer division a/b
- Euclidean algorithm iterates $a := a - b$ until $a \leq b$
 - i.e., until $a = a \% b$
 - Finally, it holds that $a = 0$ and $b = \text{gcd}(a, b)$

```
10 while (a != 0) {
11     if (a < b) {
12         tmp = a;
13         a = b;
14         b = tmp;
15     }
16     a = a % b;
17 }
```

- The rest always satisfies $a \% b < b$
 - i.e., always variable swap after the computation
 - Finally, it holds that $b = 0$ and $a = \text{gcd}(a, b)$

```
10 while (b != 0) {
11     tmp = a % b;
12     a = b;
13     b = tmp;
14 }
```

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The do-while loop

- Structure: **do statement while(condition)**
 - **statement** is executed and **condition** is evaluated
 - If **condition** is false, break
 - This repeats until **condition** becomes false
- **condition** is checked *after* the block is executed
 - So-called **post-test** loop
 - At least *one* execution of **statement**
- **statement** can be a block of code

```
1 #include <stdio.h>
2
3 main() {
4     int counter = 5;
5
6     do {
7         printf("%d ", counter);
8     }
9     while (--counter > 0);
10    printf("\n");
11 }
```

- Output:

5 4 3 2 1

- **counter--** in line 9 yields the output: 5 4 3 2 1 0

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Another example

```
1 #include <stdio.h>
2
3 main() {
4     int x[2] = {0,1};
5     int tmp = 0;
6     int c = 0;
7
8     printf("c=");
9     scanf("%d",&c);
10
11    printf("%d %d ", x[0], x[1]);
12
13    do {
14        tmp = x[0] + x[1];
15        x[0] = x[1];
16        x[1] = tmp;
17        printf("%d ", tmp);
18    }
19    while(tmp < c);
20
21    printf("\n");
22 }
```

- The **Fibonacci sequence** diverges towards infinity
 - $x_0 := 0$, $x_1 := 1$ and $x_{n+1} := x_{n-1} + x_n$ for $n \in \mathbb{N}$
- Task: Given a threshold $c \in \mathbb{N}$, compute the first sequence member satisfying $x_n > c$
- Input $c = 1000$ yields output:
c=1000
0 1 1 2 3 5 8 13 21 34 55 89 144 233 377 610 987 1597

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break and continue

```
1 #include <stdio.h>
2
3 main() {
4     int j = 0;
5     int k = 0;
6
7     for (j=0; j<4; ++j) {
8         if (j%2 == 0) {
9             continue;
10        }
11        for (k=0; k < 10; ++k) {
12            printf("j=%d, k=%d\n", j, k);
13            if (k > 1) {
14                break;
15            }
16        }
17    }
18    printf("End: j=%d, k=%d\n", j, k);
19
20 }
```

- **continue** and **break** in **statement** of the loop
 - **continue** terminates the current iteration of the loop and continues with the next iteration
 - **break** terminates the loop and continues executing the code after the loop (if any)

- Output:

j=1, k=0
j=1, k=1
j=1, k=2
j=3, k=0
j=3, k=1
j=3, k=2
End: j=4, k=2

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'as long as' vs. 'until'

```
1 #include <stdio.h>
2
3 main() {
4     int a = 200;
5     int b = 110;
6     int tmp = 0;
7
8     printf("gcd(%d,%d)=",a,b);
9
10    while (1) {
11        if (a == b) {
12            break;
13        }
14        else if ( a < b) {
15            tmp = a;
16            a = b;
17            b = tmp;
18        }
19        a = a-b;
20    }
21
22    printf("%d\n",b);
23 }
```

- ▶ **for** and **while** loops runs depending on **condition**
 - i.e., the loop runs as long as **condition** is true
- ▶ Algorithm implementation can be only based on a termination condition **done**
 - i.e., it is interrupted if **done** is true
 - i.e., **condition** = logical complement of **done**
- ▶ Easy realization via infinite loop and **break**
 - Condition in line 10 is always true
 - Termination only via **break** in line 12

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Simple error control

- ▶ Avoid runtime error
- ▶ Intentional error-caused termination

- ▶ gcc -c
- ▶ gcc -c -Wall
- ▶ assert
- ▶ #include <assert.h>

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Motivation

- ▶ Fact: All programmers make mistakes
 - A program is usually not correct the first time
- ▶ Most of the programming time is usually spent in finding and correcting own mistakes
- ▶ Efficiency in error search is a big distinction between *professionals* and *beginners*
- ▶ **Syntax errors** are **easy** to identify
 - The compiler reports even the line number
 - Check regularly the syntax while programming
 - * gcc -c **name.c** generates only object code
 - * gcc -Wall **name.c** enables compiler warnings
- ▶ **Runtime error** are **more difficult** to identify
 - The program works, but does not what it should
 - Sometimes the error is noticed after a long time
 - ⇒ This can have undesired effects (see later)

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Good habits that help programmers to avoid mistakes

- ▶ **Follow programming convention**
 - Use meaningful and consistent names
 - * e.g., for variables, functions, etc.
 - Use a consistent layout of code
 - * Indentation
- ▶ **Add explanations with comments in all relevant part of the code**
 - e.g., non-obvious conditional statements
 - e.g., functions (specify aim, input, output)
- ▶ **Break code into small functions**
 - Each function expresses a logical action
 - * Make testing and debugging easier
 - Check input for admissibility
 - * Abortion if non-admissible
 - Ensure that the output is admissible
- ▶ **Do not program all code at the same time**
 - This is a usual mistake of beginners

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Library assert.h

```
1 #include <stdio.h>
2 #include <assert.h>
3
4 void test(int x, int y) {
5     assert(x<y);
6     printf("It holds x < y\n");
7 }
8
9 main() {
10     int x = 0;
11     int y = 0;
12
13     printf("x = ");
14     scanf("%d",&x);
15
16     printf("y = ");
17     scanf("%d",&y);
18
19     test(x,y);
20 }
```

- ▶ **Aim:** Termination with error message, whenever the function notices that input/output is not admissible
- ▶ **#include <assert.h>**
 - **assert(condition);** yields erroneous termination if **condition** does not hold
- ▶ **Input:**
 - x = 2
 - y = 1
- ▶ **Output:**
 - Assertion failed: (x<y), function test, file assert.c, line 5.

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Example: Euclidean algorithm

```
1 // author: Dirk Praetorius
2 // last modified: 30.03.2017
3
4 // Euclidean algorithm to compute the gcd
5 // based on gcd(a,b) = gcd(a-b,b) for a>b
6 // and gcd(a,b) = gcd(b,a)
7
8 int euklid(int a, int b) {
9     assert(a>0);
10    assert(b>0);
11    int tmp = 0;
12
13    // reduction gcd(a,b) = gcd(a-b,b)
14    // realized via integer division, until
15    // b = 0. Then a==b, thus gcd = a
16
17    while (b != 0) {
18        tmp = a%b;
19        a = b;
20        b = tmp;
21    }
22
23    return a;
24 }
```

- ▶ **assert** ensures admissibility of input
 - i.e., it must be $a, b \in \mathbb{N}$

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Testing

- ▶ Motivation
- ▶ Quality assurance
- ▶ Types of test

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Mistakes can be costly



- ▶ Patriot Missile failure (February 1991)
 - Wrong treatment of rounding error
 - 28 deads, 100 injured
- ▶ Sinking of *Sleipner A platform* (August 1991)
 - Wrong finite element analysis
 - Damage 700 million Dollar
- ▶ Explosion of Ariane 5 rocket (June 1996)
 - Conversion `double` → `int`
 - Damage 500 million Dollar

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Quality assurance

- ▶ Simple, but true:
 - Fact 1: Software is made by humans
 - Fact 2: Making mistakes is human
 - Consequence: Software can include mistakes
- ▶ **Desirable:** Find errors before it is too late
- ▶ **The later an error is identified, the more difficult becomes its correction**
- ▶ Ideal work organization:
 - 1/3 of time for programming
 - 1/3 of time for testing
 - 1/3 of time for documenting
- ▶ In practice:
 - Most of the time for programming
 - Much less time for testing
 - Even less time for documenting ;-)

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Testing

- ▶ **Testing** is the process of executing a program with the intent of finding errors
 - G. Myers: *The art of software testing* (1979)
- ▶ A test is the comparison of the behavior of a program (**what it does**) with its desired behavior (**what it should do**)
- ▶ In practice, it is impossible to test all functions in a program with all possible combinations of input data
 - i.e., testing is by definition incomplete
- ▶ **Problems with incomplete testing**
 - Tests allow only to find mistakes
 - Tests do not provide a rigorous proof that the code has no errors
 - Test cases can themselves be incorrect
- ▶ **Important aspects in testing**
 - Tests should consider 'realistic input'
 - Tests must be reproducible

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Types of test

- ▶ **Structural tests** (for each function)
 - Are all instructions executed or are there 'dead' parts of the code?
 - Analyze conditional statements!
 - * e.g., check both occurrences (true/false) in **if ... else**
- ▶ **Functional tests** (for each function & program)
 - Does the function behave correctly for admissible input parameters? (i.e., is the result correct?)
 - Does the program (or a part of it) behave correctly? (i.e., is the result correct?)
 - Are non-admissible input parameters recognized?
 - Are limit cases and exceptions recognized and treated correctly?
 - What happens in the case of wrong input? (e.g., if the user makes a mistake)

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How to test?

- ▶ **Aim:** Is the function / program correct?
- ▶ Functional tests need **test cases**
 - (where the result is known)
- ▶ Tests should address conditional statements
 - Use parameters which lead to different outcomes in conditional statements
 - Try to test all outcome combinations
- ▶ Which cases are critical?
 - Inspect delicate parts of code
 - Be careful with type casting!
- ▶ **Start early with testing**
 - Test a function right after its implementation
 - Do not wait that the entire code is finished...
- ▶ Repeat all (!) tests after a change
 - i.e., test documenting is also important
- ▶ From now on, in the exercises you might find the following question:
 - **How did you test your program?**
 - Provide concrete examples to convince your tutor that you accurately tested your code

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Pointers

- ▶ Variables vs. Pointers
- ▶ Dereferencing
- ▶ Address-of operator **&**
- ▶ Dereference operator *****
- ▶ Call by reference

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Variables vs. Pointers

- ▶ **Variable** = Symbolic name (**identifier**) of a storage location (**memory address**) containing some quantity of information (**value**) of a specific type (**data type**)
- ▶ **Pointer** = Variable containing the address of a storage location
- ▶ **Dereferencing** = Accessing the content of a storage location using the corresponding pointer

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Pointers in C

- ▶ Pointers and variables are closely related in C:
 - Variable **var** \Rightarrow **&var** corresponding pointer
 - Pointer **ptr** \Rightarrow ***ptr** corresponding variable
 - In particular, ***&var = var** and **&*ptr = ptr**
- ▶ Like any other variable, a pointer must be declared before use
- ▶ The declaration must include the **type** of the pointer, since ***ptr** must be a variable
 - **int* ptr;** declares **ptr** as **pointer to an int**
- ▶ As usual, simultaneous declaration and initialization are possible
 - **int var;** declares the variable **var** of type **int**
 - **int* ptr = &var;** declares **ptr** and assigns the address location of the variable **var** to it
 - * In such assignments the type of the pointer and the variable must coincide
 - Usually the compiler gives a warning, e.g., **incompatible pointer type**
- ▶ The same holds for all other data types
- ▶ Some tasks are done more easily with pointers
- ▶ Other tasks cannot be done without pointers
 - e.g., dynamic memory allocation (see later)

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An elementary example

```
1 #include <stdio.h>
2
3 main() {
4     int var = 1;
5     int* ptr = &var;
6
7     printf("a) var = %d, *ptr = %d\n", var, *ptr);
8
9     var = 2;
10    printf("b) var = %d, *ptr = %d\n", var, *ptr);
11
12    *ptr = 3;
13    printf("c) var = %d, *ptr = %d\n", var, *ptr);
14
15    var = 47;
16    printf("d) *(&var) = %d, *(%d)", *(%d));
17    printf("e) *(&var) = %d\n", *(&var));
18
19    printf("e) &var = %p\n", &var);
20 }
```

- ▶ **%p** placeholder for **printf** for addresses
- ▶ Output:
 - a) var = 1, *ptr = 1
 - b) var = 2, *ptr = 2
 - c) var = 3, *ptr = 3
 - d) *(&var) = 47, *(%d) = 47
 - e) &var = 0x7fff518baba8

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Call by reference in C

- ▶ In C, basic data types are passed to functions via *call by value*
 - e.g., int, double, pointers
- ▶ *Call by reference* can be realized with pointers

```
1 #include <stdio.h>
2
3 void test(int* y) {
4     printf("a) *y=%d\n", *y);
5     *y = 43;
6     printf("b) *y=%d\n", *y);
7 }
8
9 main() {
10     int x = 12;
11     printf("c) x=%d\n", x);
12     test(&x);
13     printf("d) x=%d\n", x);
14 }
```

- ▶ Output:
 - c) x=12
 - a) *y=12
 - b) *y=43
 - d) x=43

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Summary

- ▶ **Call by value**
 - Functions receive **values** of variables as input parameters and copy them in local variables
 - Changes to the input parameters are **not** effective **outside** of the function
- ▶ **Call by reference**
 - Functions receive **addresses** of variables as input parameters
 - Changes to the input parameters are effective also **outside** of the function
- ▶ In C, for basic data types, the standard approach is call by value
- ▶ Call by reference can be realized with pointers
- ▶ Arrays are always passed to functions via call by reference

Why call by reference?

- ▶ Functions in C can have at most 1 return value
- ▶ If a functions should have more return values...

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Example

```
1 #include <stdio.h>
2 #include <assert.h>
3 #define DIM 5
4
5 void scanVector(double input[], int dim) {
6     assert(dim > 0);
7     int j = 0;
8     for (j=0; j<dim; ++j) {
9         input[j] = 0;
10        printf("%d: ", j);
11        scanf("%lf", &input[j]);
12    }
13 }
14
15 void determineMinMax(double vector[], int dim,
16                      double* min, double* max) {
17     int j = 0;
18     assert(dim > 0);
19
20     *max = vector[0];
21     *min = vector[0];
22     for (j=1; j<dim; ++j) {
23         if (vector[j] < *min) {
24             *min = vector[j];
25         }
26         else if (vector[j] > *max) {
27             *max = vector[j];
28         }
29     }
30 }
31
32 main() {
33     double x[DIM];
34     double max = 0;
35     double min = 0;
36     scanVector(x, DIM);
37     determineMinMax(x, DIM, &min, &max);
38     printf("min(x) = %f\n", min);
39     printf("max(x) = %f\n", max);
40 }
```

- ▶ **determineMinMax** returns maximum and minimum of a vector via call by reference

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Remarks about pointer declarations

- ▶ Spaces are ignored by the compilers
- ▶ ***** is applied only to the successive name
- ▶ In particular,
 - **int* pointer;**, **int *pointer;**, and **int*pointer;** are fully equivalent
 - **int* pointer, var;** declares a pointer to **int** and a variable of type **int**
 - **int *pointer1, *pointer2;** declares two pointers to **int**
- ▶ For ease of readability, try to avoid declarations of lists including variables and pointers

Pointer & Arrays

- ▶ Declaration **int array[N];** automatically creates a pointer **array** of type **int***
- ▶ **int array[];** and **int* array;** are equivalent declarations

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