

## Scientific programming in mathematics

### Exercise sheet 7

#### Introduction to C++, classes, functions

Starting with this exercise sheet, all exercises should be programmed in the C++ programming language. For more information about the class `string`, please refer to the webpage

<http://www.cplusplus.com/reference/string/string/>

**Exercise 7.1.** Extend the class `Triangle` from the lecture notes (slide 202) with two further methods:

- `double getPerimeter()`, which computes and returns the perimeter of a triangle;
- `bool isEquilateral()`, which checks whether a triangle is equilateral.

Test your implementation in a suitable way! Save your source code as `triangle.{hpp,cpp}` into the directory `series07`.

**Exercise 7.2.** An ellipse is a curve in the plane surrounding two focal points such that the sum of the distances to the two focal points is constant for every point on the curve. If Cartesian coordinates are introduced such that the axes of the ellipse are parallel to the coordinate axes, the points of an ellipse with center  $(x_0, y_0) \in \mathbb{R}^2$  and semi-axis lengths  $a, b > 0$  satisfy the equation

$$\frac{(x - x_0)^2}{a^2} + \frac{(y - y_0)^2}{b^2} = 1.$$

Recall that an ellipse is a generalization of a circle, in the sense that a circle of radius  $r$  is an ellipse with semi-axis lengths  $a = b = r$ . Write the class `Ellipse` to store ellipses of the aforementioned type. The class contains the variable members `center`, a two-dimensional array of type `double` containing the coordinates of the center, as well as the variables `a` and `b`, both of type `double`, containing the lengths of the semi-axes. Implement the standard mutator methods (`get` and `set` methods) to work with the class. Moreover, implement the methods:

- `bool isInside(double x, double y)`, which checks whether a given point lies in the part of the plane delimited by the ellipse. If the point lies exactly on the ellipse, the return value of the method is still `true` and a message informing the user about this fact is additionally printed to the screen.
- `bool isCircle()`, which checks whether an ellipse is actually a circle.
- `void printFocalPoints()`, which computes and prints to the screen the position of the focal points. Note that, if  $a > b$ , the focal points are located on the axis of the ellipse that is parallel to the  $x$ -axis and their coordinates are given by  $(x_0 \pm c, y_0)$ , where  $c = \sqrt{a^2 - b^2}$ . Adapt these formulae accordingly for the remaining cases  $a \leq b$ . What is the position of the focal points of a circle?
- `double getEccentricity()`, which computes and returns the eccentricity of an ellipse, which is given by the formula

$$e = \sqrt{1 - \left( \frac{\min(a, b)}{\max(a, b)} \right)^2}.$$

What is the eccentricity of a circle?

Test your implementation in a suitable way! Save your source code as `ellipse.{hpp,cpp}` into the directory `series07`.

**Exercise 7.3.** Write a function `bool isPalindrome(string word)` that checks whether a word is a palindrome. A palindrome is a word which reads the same backward or forward, e.g., radar, level, madam, racecar. The function returns the value `true` if the input string is a palindrome, otherwise it returns the value `false`. Write a main program which reads a word from the keyboard and checks whether it is a palindrome. Test your program appropriately! Save your source code as `palindrome.cpp` into the directory `series07`.

**Exercise 7.4.** Write a class `University` to store some information about a university. The class should contain the variable members `name` (`string`), `city` (`string`), and `num_students` (a non-negative `int`). All data members should be declared as `private`. Therefore, in order to work with the class, you have to implement suitable mutator methods (`get` and `set` methods). Moreover, implement the methods `void graduate()`, and `void newStudent()`. If the method `graduate` is called, the number of students gets decreased by one, whereas if `newStudent` is called, the number of students increases by one. Use `assert` to ensure that `graduate` does not make `num_students` negative. Test your implementation with suitable examples! Save your source code as `university.{hpp,cpp}` into the directory `series07`.

**Exercise 7.5.** Write a class `Name` which contains two members, `first_name` and `surname`, both of type `string`. Implement the standard mutator methods to work with the class. Moreover, implement the set method `setFullName`, which has one string variable as input parameter and splits the input in first name and surname automatically. Note that the input can contain multiple first names (but you can assume that the surname consists of only one word). Furthermore, write a method `void printName()` which prints to the screen the name. In case of multiple first names, only the first one should be printed entirely. For all others, only the initial should be printed. For example, for the name `Max Maxi Mustermann`, the method `printName` should print to the screen the output `Max M. Mustermann`. Save your source code as `name.{hpp,cpp}` into the directory `series07`.

**Exercise 7.6.** Write a class `Customer` for a bank customer. The class contains the name of the customer as `string`, the current balance in EUR as `double`, and a PIN code as `int`. Implement the mutator functions (`set` and `get` methods) for the member variables together with the following methods:

- `void printBalance()`, which prints the current balance to the screen.
- `bool checkPIN()`, which reads a PIN code from the keyboard and checks whether it is correct or not.
- `void drawMoney(double amount = 0)`, which reads a PIN code from the keyboard. If the code is correct, the method needs to know the amount of money the customer wants to draw. This is either passed to the method as optional input parameter or read from the keyboard. If the desired amount is positive and not larger than the current balance, the operation is performed and the new balance is printed to the screen. If the new balance becomes less than EUR 10.00, the method prints a warning to the screen. If the desired amount is larger than the current balance, the operation is interrupted.

Use `assert` to intentionally terminate the program and return error messages whenever needed (e.g., when the PIN is wrong or when the desired amount is not admissible). Test your implementation in a suitable way! Save your source code as `customer.{hpp,cpp}` into the directory `series07`.

**Exercise 7.7.** The numeral system of Roman numerals is an additive system such that any symbol has a fixed value:  $I = 1$ ,  $V = 5$ ,  $X = 10$ ,  $L = 50$ ,  $C = 100$ ,  $D = 500$ ,  $M = 1000$ . In order to avoid four characters being repeated in succession, the following subtractive notation is used:  $IV = 4$ ,  $IX = 9$ ,  $XL = 40$ ,  $XC = 90$ ,  $CD = 400$ ,  $CM = 900$ . Apart from this, the value of a symbol is independent of its position. Implement the functions:

- `string int2roman(int n)`, which computes and returns the representation as Roman numeral of an integer  $1 \leq n \leq 3999$ ;
- `int roman2int(string s)`, which computes and returns the decimal representation of a Roman number between  $I$  and  $MMMCMXCIX$ .

Test your implementation appropriately! Save your source code as `roman.cpp` into the directory `series07`.

**Exercise 7.8.** Any integer  $0 \leq n \leq 65535 = 2^{16} - 1$  has a binary representation of the form

$$n = \sum_{i=0}^{15} a_i 2^i,$$

where  $a_i \in \{0, 1\}$  for  $i = 0, \dots, 15$ . Implement two functions:

- `string dec2bin(int n)`, which, given an integer  $0 \leq n \leq 65535$ , computes and returns a string with its representation in the binary numeral system;
- `int bin2dec(string s)`, which, given a string consisting of at most 16 characters containing a binary representation of a number between 0 and 1111111111111111, returns the representation of the integer in the decimal system.

The functions work with binary representation without leading zeros. For instance, for  $n = 77$ , the function `dec2bin` returns the string 1001101. Test your implementation appropriately! Save your source code as `decVsbinary.cpp` into the directory `series07`.