

5. Let the i^{th} Affine matrix be

$$\begin{bmatrix} A_{11} & A_{12} & A_{13} & t_x \\ A_{21} & A_{22} & A_{23} & t_y \\ A_{31} & A_{32} & A_{33} & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$iA_1 = [A_{11} \ A_{12} \ A_{13}]$
 $iA_2 = [A_{21} \ A_{22} \ A_{23}]$

$$\tilde{x}_{ij} = iA_i p_j$$

Now, the matrix ~~Per~~ form will be

$$\tilde{W} = AS$$

$$\begin{matrix} \leftarrow \\ 2N \times n \end{matrix} = \begin{pmatrix} iA_1 \\ \vdots \\ iA_2 \end{pmatrix} \begin{pmatrix} | p_1 | p_2 | p_3 \dots | p_n \rangle \end{pmatrix} \begin{matrix} \leftarrow \\ 3 \times n \end{matrix}$$

$\rightarrow 2N \times 3$

$$\tilde{W} = U_{2N \times 2N} D_{2N \times n} (V_{n \times n})^T$$

$$= U_{2N \times 3} D_{3 \times 3} (V_{n \times 3})^T$$

taking rank-3 approximation

(\because the matrix in RHS (AS) has rank=3)

$$= \underbrace{U_{2N \times 3} D_{3 \times 3}^{1/2}}_{A'} \underbrace{D_{3 \times 3}^{1/2} (V_{n \times 3})^T}_{S'}$$

$$A = A'Q \quad S = Q'^T S'$$

Here, we do not have any constraints on iA_1 or iA_2 to find out Q (not ~~the~~ similar to the case ~~when~~ of 3D rigid motion as solve in the class). Because here, matrix A has 6-degree of freedom.

~~Here, we have 6-degree of freedom just to find A and for the whole affine matrix~~

So, we can't find S and A

and since, we can't find $A \therefore$ we also can't find the whole Affine matrix.

\therefore We can't find the point coordinates and the affine object motion.