

2. Let p_{2c} is the coordinate of points in camera coordinate system and p_{1c}

$$\therefore p_{2c} = R p_{1c}$$

$$\left. \begin{array}{l} \text{Now, } p_2 = K p_{2c} \rightarrow p_2 = K R p_{1c} \\ p_1 = K p_{1c} \rightarrow p_{1c} = K^{-1} p_1 \end{array} \right\} \Rightarrow \boxed{p_2 = \underbrace{K R K^{-1}}_M p_1}$$

($\because K$ is full rank matrix)

$$p_1 = \begin{bmatrix} u_1 \\ v_1 \\ w_1 \end{bmatrix} \Rightarrow x_1 = \frac{u_1}{w_1} \text{ and } y_1 = \frac{v_1}{w_1}$$

$$p_2 = \begin{bmatrix} u_2 \\ v_2 \\ w_2 \end{bmatrix} \Rightarrow x_2 = \frac{u_2}{w_2} \text{ and } y_2 = \frac{v_2}{w_2}$$

$$\text{Now, } x_2 = \frac{M_{11} x_1 + M_{12} y_1 + M_{13}}{M_{31} x_1 + M_{32} y_1 + M_{33}}$$

$$y_2 = \frac{M_{21} x_1 + M_{22} y_1 + M_{23}}{M_{31} x_1 + M_{32} y_1 + M_{33}}$$

$$\text{Now, } \begin{bmatrix} x_{1i} & y_{1i} & 1 & 0 & 0 & 0 & -x_{1i}x_{2i} & -y_{1i}x_{2i} & -x_{2i} \\ 0 & 0 & 0 & x_{1i}y_{1i} & 1 & 0 & -x_{1i}y_{2i} & -y_{1i}y_{2i} & -y_{2i} \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \end{bmatrix} \begin{bmatrix} M_{11} \\ M_{12} \\ M_{13} \\ M_{21} \\ M_{22} \\ M_{23} \\ M_{31} \\ M_{32} \\ M_{33} \end{bmatrix} = 0$$

$$A M = 0$$

$\downarrow \quad \quad \downarrow$
 $2N \times 9 \quad \quad 9 \times 1$

this eqⁿ $A M = 0$ will be solved by computing the SVD of A i.e. $A = U S V^T$
the vector m will be given by the singular vector in V , corresponding to the least singular value in S .

Now, we got M matrix. $= K R K^{-1}$

$$\boxed{\therefore R = K^{-1} M K}$$