

$$x \uparrow^n y = \begin{cases} x^y & \text{if } n = 1 \\ x & \text{if } n > 1 \text{ and } y = 1 \\ x \uparrow^{n-1} (x \uparrow^n (y - 1)) & \text{otherwise} \end{cases}$$