# Team Project Proposal Assignment

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## Project title

Duel of the Data Structures

### Team information

Team member's name	Discipline	STAT 312 or STAT 542 student?
Project Contact: Andrew Gilbert	Comp. Sci.	312
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## Progress

Completion	Activity	Completion Date	Comments
100%	Design test framework	???	No official design phase
100%	Build test framework	2 Nov 2013	Written in Java, shown to Dr Smith.
100%	Pilot study	7 Nov 2013	Date is that of data generation, according to Git repository.
100%	Analyse pilot study	7 Nov 2013	
	Write team project update	7 Nov 2013	This document.
100%	Find implementations of all data structures	8 Nov 2013	Done ahead of time.
0%	Run tests	15 Nov 2013	
0%	Analyse full study	22 Nov 2013	
0%	Create presentation	6 Dec 2013	

Reproduced above is our team's table of activities, with updated completion dates, comments, and a percent completion list. In general, the code has been working well. Our testing framework has already produced

data spanning all our desired factors, and is capable of producing an arbitrary number of replicates with full randomization. Writing the code took slightly longer than expected, with completion being approximately the 2<sup>nd</sup> of November, rather than the 1<sup>st</sup>. The data for the pilot study has been gathered and analyzed: the results will be reported later in this paper.

### Pilot study and power analysis

We have completed a pilot study, consisting of two of our experimental factors—the data structure type and the operation on the structure—varied over two levels each in a full-factorial experiment. The resulting data was gathered by our program and put into a CSV with minimal human interaction.

All the factor levels involved in our experiment can be controlled exactly, as the computer is running all the tests. In the case of our pilot study in particular, the only factors tested were categorical and were fully under the control of our software (assuming the software wasn't doing anything really strange we don't know about!) Each of the results in our raw data is the time at nanosecond precision to execute the operation on a group of random items with a clean instance of the data structure. Each test run uses a fresh instance of the data structure, and a fresh block of random data which is generated on the spot before timing begins.

From the pilot study data, we calculated a standard deviation of 8073696, which was used in our power analysis below. The dotplot (figure 1) showed fairly tight clustering of data points with a few outliers. The ANOVA results (see page 5) indicate that there is a definite interaction between operation and data structure type. That's something worth exploring: is that expected according to computational complexity? If not, what's causing it?

Our pilot study basically sustained our current expectations, with our system working perfectly. We see no reason not to simply run the next step of our project and begin analysis.

Our power analysis (see figure 2 and the Minitab output in figure ) indicates that we should need 224 repetitions to achieve a resolution of 1ms with a target power of 0.95. A run of our program to achieve that many repetitions with all the factors and levels required 67.19994490468333 minutes, and produced a mere 229 kB of data. Given the automated nature of the testing, this is not unreasonable, although it may be expedient to run the 140 repetitions required for 80% power instead if we decide there is no reason for the higher power level.

The effect sizes were chosen based on a quick summary of mean deltas from the Tukey output (page 5). We looked at each of the deltas in millions of nanoseconds (milliseconds), and noticed that the lowest delta was roughly 5 million. Realizing that that represents a delta of 5 milliseconds, and that Java may or may not be measuring to nanoseconds anyway (in fact, it probably isn't), we decided to generate power analyses for effect sizes of 1 ms, 5 ms, and 10 ms. 1 ms is 1/5th of the smallest observed delta, so it should be more than good enough to find most changes. 5 ms is right near the smallest observed delta, which was between the less-meaningful means of BST overall and Trie overall. Since there's a known interaction, those means could probably be ignored.

 $<sup>^{1}</sup>$ Note: This statistic, like 68.738247% of other statistics, was carried to a meaningless degree of accuracy

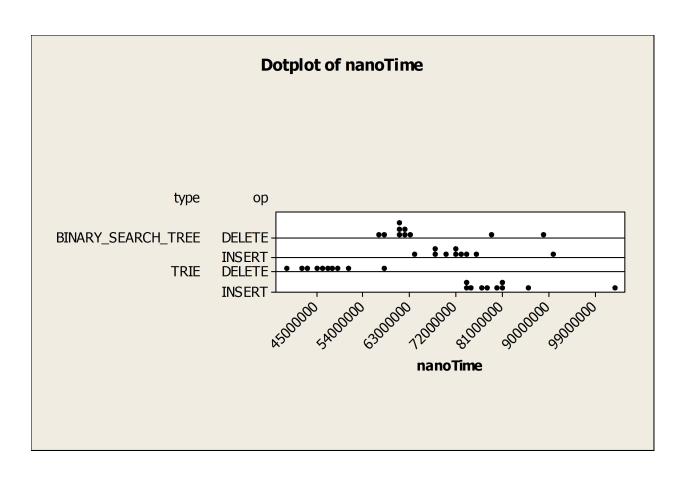


Figure 1: Dotplot of time taken (in nanoseconds) vs. data structure type and operation under test

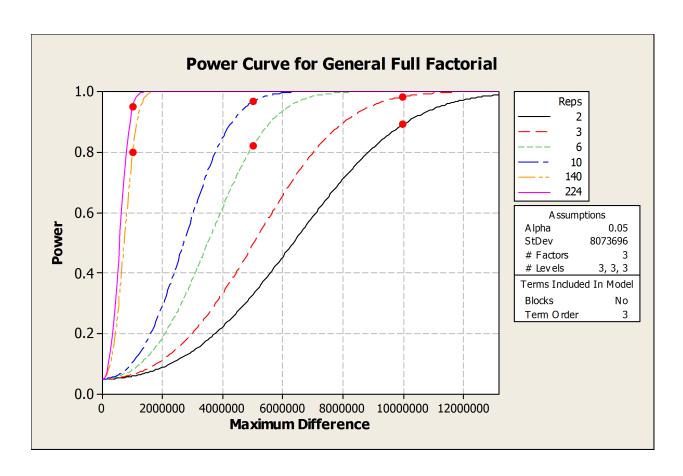


Figure 2: Power Analysis Results

### Minitab output

#### **GLM** results

General Linear Model: nanoTime versus type, op

Factor Type Levels Values

type fixed 2 BINARY\_SEARCH\_TREE, TRIE

op fixed 2 DELETE, INSERT

Analysis of Variance for nanoTime, using Adjusted SS for Tests

```
Source
        DF
                 Seq SS
                             Adj SS
                                         Adj MS
         1 2.70225E+14 2.70225E+14 2.70225E+14
                                                  4.15 0.049
type
         1 4.38992E+15 4.38992E+15 4.38992E+15
                                                 67.35 0.000
type*op
        1 1.80058E+15 1.80058E+15 1.80058E+15
                                                 27.62 0.000
Error
        36 2.34664E+15 2.34664E+15 6.51846E+13
Total
        39 8.80737E+15
```

S = 8073696 R-Sq = 73.36% R-Sq(adj) = 71.14%

Unusual Observations for nanoTime

```
        Obs
        nanoTime
        Fit
        SE Fit
        Residual
        St Resid

        2
        90524526
        72853504
        2553127
        17671022
        2.31 R

        3
        89375764
        65319945
        2553127
        24055820
        3.14 R

        9
        103446934
        81073760
        2553127
        22373174
        2.92 R
```

R denotes an observation with a large standardized residual.

#### Tukey test

Grouping Information Using Tukey Method and 95.0% Confidence

```
        type
        N
        Mean
        Grouping

        BINARY_SEARCH_TREE
        20
        69086724
        A

        TRIE
        20
        63888404
        B
```

Means that do not share a letter are significantly different.

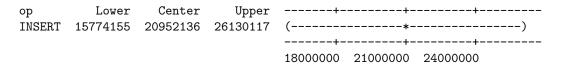
Tukey 95.0% Simultaneous Confidence Intervals Response Variable nanoTime All Pairwise Comparisons among Levels of type type = BINARY\_SEARCH\_TREE subtracted from:

Grouping Information Using Tukey Method and 95.0% Confidence

op N Mean Grouping INSERT 20 76963632 A DELETE 20 56011496 B

Means that do not share a letter are significantly different.

Tukey 95.0% Simultaneous Confidence Intervals Response Variable nanoTime All Pairwise Comparisons among Levels of op op = DELETE subtracted from:



Grouping Information Using Tukey Method and 95.0% Confidence

 type
 op
 N
 Mean
 Grouping

 TRIE
 INSERT
 10
 81073760
 A

 BINARY\_SEARCH\_TREE
 INSERT
 10
 72853504
 A
 B

 BINARY\_SEARCH\_TREE
 DELETE
 10
 65319945
 B
 B

 TRIE
 DELETE
 10
 46703047
 C

Means that do not share a letter are significantly different.

Tukey 95.0% Simultaneous Confidence Intervals
Response Variable nanoTime
All Pairwise Comparisons among Levels of type\*op
type = BINARY\_SEARCH\_TREE
op = DELETE subtracted from:

op

J 1	-				
BINARY_SEARCH_TREE	INSERT	-2193854	7533559	17260973	3
TRIE	DELETE	-28344311	-18616897	-8889484	1
TRIE	INSERT	6026402	15753816	25481229	9
type	op	+	+	+	
BINARY_SEARCH_TREE	INSERT		(*	:)	
TRIE	DELETE	(	*)		
TRIE	INSERT		(-	*)	
		+			
		-2.5E+07	0 2	5000000	50000000

Lower

type = BINARY\_SEARCH\_TREE
op = INSERT subtracted from:

type

Center

Upper

type op Lower Center Upper TRIE DELETE -35877870 -26150457 -16423043 TRIE INSERT -1507157 8220257 17947670 type op TRIE DELETE (---\*--) TRIE INSERT (---\*--) -2.5E+07 0 25000000 50000000 type = TRIE op = DELETE subtracted from:

type op Lower Center Upper TRIE INSERT 24643300 34370713 44098126

---+----+----+--type op TRIE INSERT (---\*---) -2.5E+07 0 25000000 50000000

#### Power analysis

Power and Sample Size

General Full Factorial Design

Alpha = 0.05 Assumed standard deviation = 8073696

Factors: 3 Number of levels: 3, 3, 3

Include terms in the model up through order: 3 Not including blocks in model.

Maximum		Total	Target	
Difference	Reps	Runs	Power	Actual Power
1000000	140	3780	0.80	0.800978
1000000	224	6048	0.95	0.950165
5000000	6	162	0.80	0.820545
5000000	10	270	0.95	0.967069
10000000	2	54	0.80	0.891741
10000000	3	81	0.95	0.983354