

# EECS 368

## Programming Language Paradigms

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# Conditional Expressions

As in most programming languages, functions can be defined using conditional expressions.

```
abs :: Int -> Int  
abs n = if n >= 0 then n else -n
```

abs takes an integer  $n$  and returns  $n$  if it is non-negative and  $-n$  otherwise.

Conditional expressions can be nested:

```
signum  :: Int -> Int
signum n = if n < 0 then -1 else
            if n == 0 then 0  else 1
```

In Haskell, conditional expressions must always have an else branch, which avoids any possible ambiguity problems with nested conditionals.

As an alternative to conditionals, functions can also be defined using guarded equations.

```
abs n | n >= 0      = n  
      | otherwise  = -n
```

As previously, but using guarded equations.

Guarded equations can be used to make definitions involving multiple conditions easier to read:

```
signum n | n < 0      = -1  
         | n == 0     = 0  
         | otherwise = 1
```

The catch all condition otherwise is defined as

```
otherwise = True
```

Many functions have a particularly clear definition using pattern matching on their arguments.

```
not      :: Bool -> Bool
not False = True
not True  = False
```

not maps False to True, and True to False.

Functions can often be defined in many different ways using pattern matching. For example

```
(&&)           :: Bool -> Bool -> Bool
True  && True   = True
True  && False  = False
False && True   = False
False && False  = False
```

can be defined more compactly by

```
(&&)           :: Bool -> Bool -> Bool
True  && True   = True
_      && _     = False
```

Internally, every non-empty list is constructed by repeated use of an operator (`:`) called `cons` that adds an element to the start of a list.

```
[1, 2, 3, 4]
```

Means `1:(2:(3:(4:[])))`.



Functions on lists can be defined using  $x:xs$  patterns.

```
head      :: [a] -> a
```

```
head (x:_) = x
```

```
tail      :: [a] -> [a]
```

```
tail (_:xs) = xs
```

`head` and `tail` map any non-empty list to its first and remaining elements.

- $x:xs$  patterns only match non-empty lists:

```
> head []
```

Error

- $x:xs$  patterns must be parenthesized, because application has priority over  $(:)$ . For example, the following definition gives an error:

```
head x:_ = x
```

Functions can be constructed without naming the functions by using lambda expressions.

```
\ x -> x + x
```

This is the nameless function that takes a number  $x$  and returns the result  $x+x$ .

- The symbol  $\lambda$  is the Greek letter lambda, and is typed at the keyboard as a backslash `\`.
- In Haskell, the use of the  $\lambda$  symbol for nameless functions comes from the lambda calculus, the theory of functions on which Haskell is based.

## Why Are Lambda's Useful?

Lambda expressions can be used to give a formal meaning to functions defined using currying. For example:

```
add x y = x+y
```

means

```
add = \ x -> (\ y -> x+y)
```

Lambda expressions can be used to avoid naming functions that are only referenced once. For example:

```
odds n = map f [0..n-1]
      where
          f x = x*2 + 1
```

can be simplified to

```
odds n = map (\ x -> x*2 + 1) [0..n-1]
```

An operator written between its two arguments can be converted into a curried function written before its two arguments by using parentheses.

For example:

```
> 1+2
```

```
3
```

```
> (+) 1 2
```

```
3
```

This convention also allows one of the arguments of the operator to be included in the parentheses.

For example:

```
> (1+) 2
```

```
3
```

```
> (+2) 1
```

```
3
```

In general, if  $\oplus$  is an operator then functions of the form  $(\oplus)$ ,  $(x\oplus)$  and  $(\oplus y)$  are called sections.