Python for High Performance Computing

Exercises

About

There are 4 exercises:

- Exercise 1: calculate the median from a list;
- · Exercise 2: basic NumPy array indexing;
- Exercise 3: Monte--Carlo integration;
- Exercise 4: function integration using the trapezium rule;

Working environment

Using the ARC cluster "arcus-b"

Use the teaching account credentials you have been given to log in. For example, if you have been given account details for account teaching01

```
ssh -XC teaching01@arcus-b.arc.ox.ac.uk
```

We have automatically set up your working environment to use the following system environment modules:

```
module load python/anaconda2/2019.03
module load gcc/5.3.0
module load git
```

For the last exercise you may wish to submit and test MPI jobs

To submit jobs, use the template submission file named "arcus-slurm-submit.sh" which is provided in the integral directory.

Submit with the command

```
sbatch arcus-slurm-submit.sh
```

Working in your local Linux environment

Alternatively if you have an Anaconda environment set up on your local machine you may download the material from GitHub:

```
git clone https://github.com/andygittings/python-dec-2019
```

Connecting to ARCUS-B from Windows

If you have problems with connecting via SSH (including X display issues) Try connecting via Windows using the MobaXTerm application. This may be downloaded from:

```
https://mobaxterm.mobatek.net/download-home-edition.html
```

Find the downloaded file named "MobaXterm_Portable_v12.4.zip" and extract this and run MobaXterm Personal 12.4.exe

Once MobaXterm is open click "Session" then select the "SSH" tab and enter : arcus-b.arc.ox.ac.uk in the "Remote Host" field - then click OK.

When prompted to "login as:" type the username on the training account sheet you have been given, and when prompted for "teachingNN password:" enter the password from the sheet.

You should now be connected to the ARCUS-B system.

Material

Once logged into the ARC server you will find a directory named:

```
python-dec-2019/
```

If you change into this directory...

```
cd python-dec-2019
```

as well as this PDF file, you will find the following directories:

```
darts\     Question 3.
integral\     Question 4.
examples\     Some useful demonstration scripts
slides\     Course slides in PDF format
```

Editing files

To edit files, use the nano editor, for example to edit the file mypython.py:

```
nano mypython.py
```

Use CTRL-X to quit, you will need to answer Y to save, and then confirm the filename.

You can then run the resulting file in python e.g.

```
python mypython.py
```

Solutions

At some point during the practical we will make solutions to the exercises available for download. These will be available from the following Git repository: https://github.com/andygittings/python-worked-dec-2019

To download, use the following command:

```
git clone https://github.com/andygittings/python-worked-dec-2019
```

Exercise 1: calculate the median from a list

Define a function called my_median() that

- takes a list of years (assumed to have an odd number of elements $N \ge 3$),
- computes the median based on the elapsed number of years since 1900 for each entry in the list and
- return the median and the value either side of the median as a list.

For instance, if the input is years = [1989, 1955, 2011, 1943, 1975], then the returned result should be [55, 75, 89].

Either using a python script file, or by using the interactive python shell:

- 1. Define the function and use the above example list as input to check you get the right answer.
- 2. The list needs to be sorted -- how?
- 3. List indexing may help you to get the final result, e.g. list[3:5].
- 4. Try generating a random array for input using module random.
- 5. Put a test in the function to check the input list has an odd number of elements.

Hint: the list.append() method is very useful for this exercise.

Exercise 2: basic NumPy array indexing

- 1. Define a 1D NumPy array x, containing random numbers (real, double precision).
- 2. Using index slicing and negative indices, assign the "interior" of the array x (the entire array except the first and the last entry) to a new array variable y.
- 3. Using slicing, create yet another array z that contains every other element of x, starting with the first.
- 4. Using fancy indexing, create an array z2 that contains all the negative elements of z.
- 5. Reshape the array x into a 2D array and assign the result to x2. Verify whether the two arrays share the same data or not.

Exercise 3: Monte--Carlo integration

Computing π using Monte-Carlo integration

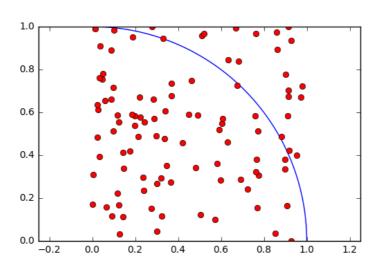
Computing high-dimensional definite integrals with complicated boundaries was the first use of the Monte-Carlo method. Using this approach, π can be computed as the surface integral over the unit circle of a constant unit integrand.

The algorithm of computing π is the area of the unit circle in the 2D plane is to "throw darts" and to count those that fall in the circle. More specifically,

- generate a number of N (uniformly distributed) points in the 2D plane;
- count the number $N_{\rm in}$ of points in the unit circle;
- compute the approximation as $\pi \approx N/N_{\rm in}$.

Exploiting the symmetry of the unit circle, only the area of a single quadrant of the circle can be computer. Thus, the random points are generated with coordinates in the [0, 1) interval and the estimated value of pi is

$$\pi_{approx} = 4 \frac{N}{N_{\text{in}}} \longrightarrow \pi \quad \text{as} \quad N \longrightarrow \infty$$



Setup

The initial Python scripts for this exercise is found in the directory darts/, which you are asked to modify using a text editor of your choice. All Python scripts are to be run directly at the command line.

Aim

Building on the provided scripts which use only Python, you are also asked to provide alternative implementations of the method scripted using

- NumPy
- Numba
- multiprocessing

Instructions

Go into the directory darts/ and follow the following steps:

Step 1: Edit the files darts.py,run_darts.py and plot_results.py and understand their structure and functionality. Run the test file run_darts.py and observe the output. Notice how the number of tries needed for the function numQuadrantHitsPython are generated using the NumPy function logspace. Verify the code computes π with increasing accuracy as the number of tries (controlled by numPoints) increases.

Step 2: Add a new function numQuadrantHitsNumPy to darts.py that performs the same operations as numQuadrantHitsPython but using NumPy vectorised operations:

- generate x and y as random NumPy arrays using the numPy function random.ranf;
- use fancy indexing and array functions to compute the number of "hits".

Modify the file run_darts.py to time the execution of the function numQuadrantHitsNumPy and verify the accuracy of its result.

Step 3: Similarly, add a function numQuadrantHitsNumba to darts.py that performs the same operations as numQuadrantHitsPython using the Numba JIT compiler:

- start with the same code as for numQuadrantHitsPython;
- import the numba module and add the appropriate decorator;
- remember to run the new function once (on a small number of tries numPoints) to trigger the JIT compilation and cache the results.

Again, modify the file run_darts.py to time the execution of the function numQuadrantHitsNumba and verify the accuracy of its result.

Step 4: Edit the file darts.py again and implement a solution that uses the multiprocessing module. For this, create a funtion called numQuadrantHitsMP that

- · opens a pool of processes
- use map async to call the function numQuadrantHitsNumpy independently from each process
- each call to numQuadrantHitsNumpy computes a partial result of the hits calculation

map_async is mapped to a Python iterable (array or list) that contains the partial number of tries per process repeated a number of times; this partial number is numPoints / numProcs. While each process carries out only a part of the calculation, together, the processes carry out all the calculations cooncurrently. The raw results from map_async is a Python object; use the get() method to retrieve the partial hit counts into a list and the function sum() to sum up all the partial hit counts into the total.

After retrieving the partial hit counts using get(), print the values. What do you notice? What happens?

Modify the function numQuadrantHitsNumpy (preferably creating a new one) by adding a random number generator seed using the function numpy.random.seed() and the process rank. In order to map the new function to data using map_async, you will need to

- allow numQuadrantHitsNumpy to take a tuple as argument, to contain the original numPoints as well as the value seed;
- create an appropriate list of tuples to map the function onto.

Check the accuracy of the results using darts_test.py and make sure the multiprocessing implementation scales in performance with the number of processes (*i.e.* the processing time roughly halves when the number pf processes doubles).

Step 5: Finally, run both run_darts.py and use plot_results.py in order to cross-compare all solutions. Thus, for the same number of tries, make sure that

• the same level of accuracy in estimating π is achieved with all solutions;

Exercise 4: Function integration using the trapezium rule

Integration by the trapezium rule

You are asked to evaluate a definite integral using the trapezium rule.

The function is defined as $f(x) = 2.0 * sqrt(1.0 - x^2)$ which is integrated over -1.0 to +1.0 to obtain π

Setup

The initial Python scripts for this exercise is found in the directory integral/, which you are asked to modify using a text editor of your choice. All Python scripts are to be run directly at the command line.

Aim

Building on the provided scripts which use only Python, you are also asked to provide alternative implementations of the method scripted using

- NumPy
- Numba
- Cython
- mpi4py

Instructions

Go into the directory integral/ and follow the following steps:

Step 1: Edit the files integral.py, run_integral.py and plot_results.py and understand their structure and functionality. Run the test file run_integral.py followed by plot_results.py and observe the output. Notice how the number of integration intervals N needed for the function trapintPython are generated using the NumPy function logspace. Verify the code computes the value of π with increasing accuracy as the number of intervals (controlled by N) increases.

Step 2: The function trapintPython computes the integral of a mathematical function defined by funcPython, which, in turn, uses the sqrt function from math. Add a new function trapintNumPy to integral.py that performs the same operations as trapintPython but using NumPy vectorised operations. For this purpose, create a NumPy version of funcPython called funcNumpy that uses the sqrt function from numpy to operate on an entire array rather than a single scalar.

Modify the file run_integral.py to time the execution of the function trapintNumPy and verify the accuracy of its result. Satisfy yourself the execution of the NumPy solution is faster than the pure Python implementation.

Step 3: Similarly, add a function trapintNumba to integral.py that performs the same operations as trapintPython using the Numba JIT compiler:

- start with the same code as for trapintPython;
- import the numba module and add the appropriate decorator;
- remember to run the new function once (on a small number of interval N) to trigger the JIT compilation and cache the results.

Again, modify the file run_integral.py to time the execution of the function trapintNumba and verify the accuracy of its result.

Step 4: Now, copy the source of the trapintNumpy function into a file integral.pyx and modify this source to create a Cython function trapint that performs the optimised function of the original trapintNumpy.

Start by generating a Cython implementation from the original pure Python source:

- create a distutil setup file and install the Cython module with python setup build_ext --inplace;
- modify the file run_integral.py to time the execution of the Cython function trapint and verify the accuracy of its result.

Next, work on improving the performance of the Cython function trapint. In particular

- · type all variables as well as the function itself;
- replace the use of the Python math sqrt function with the C equivalent (see hint below);
- verify the results of these steps by running the test run_integral.py.

Hint: Import the standard C math sqrt funtion with

from libc.math cimport sqrt

Further, improve the performance of of the Cython solution via multithreading. This involves two important aspects:

- releasing the GIL for the main loop in trapint and
- using the parallel variant prange of the iterator.

Pass the number of threads to use as an argument to the function trapint and use openmp.omp_set_num_threads() to set the number of OpenMP threads. Using different number of threads

- test that the Cython function produces accurate results and
- ensure the performance of the threaded function scales with the number of threads (*i.e.* execution time is nearly halved by doubling the number of threads).

Step 5: Write a file integral_mpi.py to implement a mpi4py version of the test in run_integral.py. Just as the original, the mpi4py implementation loops over a range of values for N and computes an approximation for the definite integral using the trapezium rule. Unlike run_integral.py, the mpi4py version computes the intergal value in a distributed fashion, with each process resposible for calculating the integral for only a part of the original interval of integration.

Here are the steps to follow in writing integral_mpi.py:

• Loop over the same range of values for N as in integral_test.py. For each value of N, each process computes the integral of the function for a part of the interval from a to b. Namely, the integration for process rank of size number of processes is between aProc and bProc, where

```
N1 = (float(N)* rank) / size
N2 = float(N)*(rank+1) / size
aProc = a + N1 * h
bProc = a + N2 * h
```

- Each process uses the NumPy function trapintNumPy for the calculation of a partial integral value valProc, computed between the limits aProc and bProc and using a number of intervals equal to N2-N1.
- The total value of the integral (between a and b) is obtained from sum-reducing all the partial results valProc. This is achieved by placing the partial result on each process in a vector of size 1 and by reducing all these partial vectors across all processes to a final result vector on a single process, typically the rank 0.
- Use the function MPI.Wtime() to measure execution time for each value of N.
- The approximated value for the integral (or the absolute error) is printed by the process of rank 0 only, along with the execution time.

Demonstrate to yourself that the performance of integrate_mpi.py scales with the number of processes used (*i.e.* execution time is nearly halved by doubling the number of processes).

Step 6: Finally, run both run_integral.py and integral_mpi.py once more in order to cross-compare all the 4 solutions. Thus, for the same number N of intervals, make sure that

- the same level of accuracy in estimating the integral is achieved with all solutions;
- execution time for the Cython implementation (with 1 thread) and the Numba one should be comparable;
- execution time for the Cython implementation (with 2 and 4 threads) and the mi4py one (with 2 and 4 processes, respectively) should also be comparable.