<u>Announ Cements</u>

Final exam! Thursday 12/19 1:30-4:30pm 4025 Campus Instructional Facility

Wed. class will be review Policies/practice problems to come later

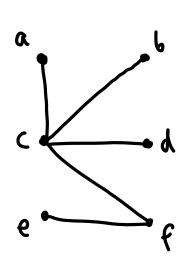
& 11.1: Trees

Def: A tree is a conn. (undir.) graph w/ no rimple circuits

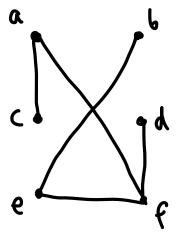
A forest is a graph consisting of one or more trees

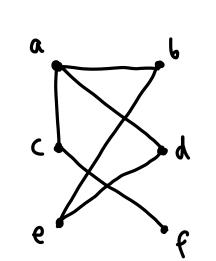
Class activity: Tree or no tree?

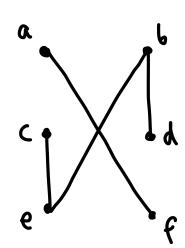
(D



b)







Properties: Suppose T is a tree.

- a) T has no loops of mult. edges
- b) There is exactly one simple path blun, any two vents.
- c) |E| = |V| 1
- d) Every edge is a cut edge
- e) Adding any edge creates a simple circuit

Def: A rooted tree is a tree in which one vertex has been designated the root

Note: We sometimes think of a rooted tree as a digraph where every edge is directed away from the root

Ex:

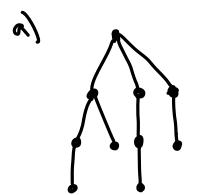
rooted tree w/root a

rooted tree w/ root c

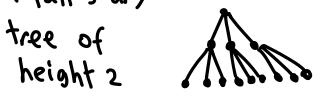
leaves

Def: A rooted tree is called an m-ary tree if every internal vertex has <m children. If every internal vertex has = m children, it is called full An m-ary tree w/ m=2 is a binary tree An m-ary tree of height h has < mh leaves

Class activity: Count the number of leaves, internal vertices, (total) vertices in



b) A full 3-ary



- b) A fall binary tree of height 3
- d) A full binary tree of height 7

Facts:

- a) A full binary tree of height h has 2 1 vertices, 2h of which are leaves, and 2h-1 of which are internal vertices.
- b) A full m-ary tree of height h has I + m + m2 + ... + mh herts. mh of which are leaves, and 1+m+--+mh-1 of which are internal vertices.
- c) A full m-ary tree w/ i int. verts. has mit1 verts. and (m-1) it I leaves
 - d) A full m-ary tree ω / n verts. has $\frac{n-1}{m}$ int. verts. and $\frac{(m-1)n+1}{m}$ leaves