# Announcements

Midtern 3: Wed. in class

Covers through Section 10.5

Reference sheet allowed (one Ay sheet w/ writing on both sides) See policy email (practice problems etc.)

Problem session this week will be Tuesday & review

# Midterm 3 Review

(Partial) list of topics:

Everything from first two midterms (sets, functions, algorithms, induction, Counting, probability, etc.)

#### Relations

Def'n & examples

Properties: reflexive, irref., symmetric, antisym., asymm., transitive

Operations: RUS, RNS, R-S, SOR, R, R-

Matrices / digraphs for relations

Go botton ordered mirs, matrices, digraphs

Connections to properties

Operations

Connections to (h. 10

Equivalence relins

Definition

Equiv. classes and set partitions

Graphs/digraphs

Defins: simple/multi./nbhd./deg./bipartite/(induced) subgraph
Handshake thm.

Special classes of graphs

Constructions: deletion/contraction/union

Adiacency Lincidence matrices

Isomorphism

Show that graphs are isomorphic: explicit isom., adj. matrices

Thow that graphs are <u>not</u> isomorphic! different "label-indep proporties"

Connectivity (for digraphs, weak vs. strong), cut-edges/cut-vertices

Paths/circuits

Eulerian/Hamiltonian

t criteria

### Other tips:

Look at HW, quizzes, lecture notes, textlook, other problems We have lots of defins and constructions—learn them and/or write them on your ref. sheet

## Examples:

1) Find the equiv-relin corresp. to the following set partition:

$$A = \mathcal{X} = A_1 \cup A_2 \cup A_3 \cup A_4 \cup A_5$$

Solin: 
$$\alpha \sim b$$
 if and only if  $\alpha - b = 5$   
A; = [i] for  $i = 1,2,3,4,5$ 

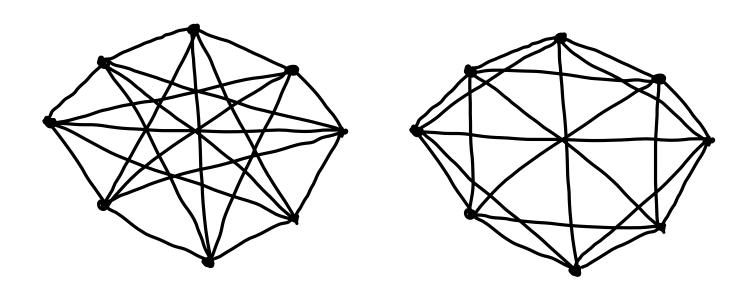
2)a) Find a reln that is reflexive and transitive, but not symmetric or antisym.

$$R = \{(1,1),(1,2),(3,3),(1,1),(1,1),(1,3)\}$$

- b) Show that any relation which is sym. and antisym. is also transitive.
- Pf: Let A be a set and  $R \subseteq A \times A$  be a relin that is both sym. and antisym. If  $x \neq y$  and  $(x,y) \in R$ , then since R is sym,  $(y,x) \notin R$ , but since R is antisym.,  $(y,x) \notin R$ . Both statements can't be true at the same time, so if  $x \neq y$ ,  $(x,y) \notin R$ , and every elt. of R is of the

form (x,x). Now let a,b,ceA such that (a,b)eR and (b,c)eR. By the previous statements, b=c, so (a,c)=(a,b)eR, and therefore R is transitive.

3) (10.3.44) Determine whether or not these graphs are isomorphic.



6) Do they have Eulerian/Hamiltonian paths/circuits?