Announcements

Quiz today!

Midterm 1 Wed 9/2s in-class (50 minutes)

Covers through this Friday (Ch 2,3,5,6)

Policy email later today

§ 6.1: Counting

Counting problem: determine the cardinality of a set "combinatorics"

Product rule: Suppose that a procedure can be broken down as a sequence of two tasks. If there are m ways to do the first task n ways to do the second task*,

then there are mn ways to do the procedure

* For any of the m choices for the first task

Ex 2: How many ways are there to write a letter followed by a digit? (e.g. AO, C8, Y2)

Ans: 26 letters. 10 digits = 260 ways

Ex 1: 2 employees, 12 offices. How many ways are thore to assign each employee an office?

Ans: 12 choices for Employee 1, then 11 (remaining!) choices for Employee 2.

Ex 7: How many one-to-one functions are there from a set with metts to one with n elts.

Ans:
$$N(n-1)(n-2) \cdots (n-m+1)$$

(If m) n, this is 0)

Sum rule: If a task can be done either in one of m ways or one of n ways, with no overlap, then there are men ways to do the task.

Ex: How many length-2 "words" are there, where the first letter is capital or lower-case, and the second is lower-case?

First letter: 26 + 26 = 52 (hoices (sum rule)
Second letter: 26 choices

Total: 52.26= 1352 "words" (product rule)

Ex 16: How many passwords are there satisfying:

- a) Length 6,7, or 8
- 6) Made up of digits and uppercase letters
- c) At least one digit

Length 6:

26+10=36 Choices for each digit

Total passwords satisfying b):

36.36.36.36.36.36=36.

ist 2nd digit digit

Passworks containing only letters (i.e. violating c)): 26.26.26.26.26.26.26

Length-6 valid passwords: 36°-26°=1,867,866,560 Length-7 valid passwords: 367-267 Length-8 valid passwords: 368-268

Total: 36°-26°+367-267+36°-268=2,684,483,063,360

Subtraction rule: If a task can be done either in one of m ways or one of n ways, with overlap of k, then there are mente ways to do the task.

|AUB|= |A|+|B|-|AAB| m n k Ex 18: How many 01-strings of length 8 either start w/ 1 or end w/ 00?

Start w/ 1:

1 * * * * * * *

1.2.2.2.2.2.2 = 128 choices

End w/ 00

*****00

2.2.2.2.2.2.1.1=64 chaices

Start w/ 1 AND end w/ 00:

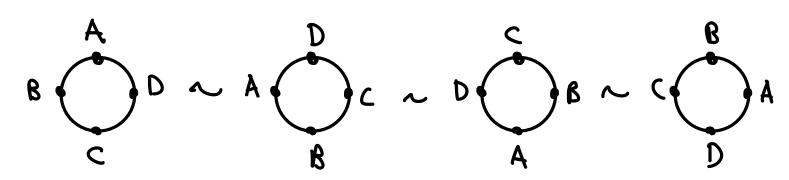
1*** ** 00

1.2.2.2.2.2.1.1 = 32 choices

Ans: 128+64-32 = 160 strings

Division rule: If there are n ways to do a task, and groups of d of these ways are equivalent, then there are not ways up to equivalence.

Ex 20: How many different ways are there to seat 4 people around a circular table, where two seatings are considered equivalent if they are rotations of each other?



4 rotations of each reating arrangement
4.3.2.1=24 seating arrangements