Announcements

H/W 10 will be posted soon Quiz this Wed. Midtern 3 Wed. 11/20 in class

Recall:

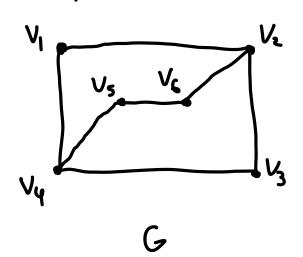
Def: Let $G = (V_1, E_1)$ and $H = (V_2, E_2)$ be simple grophs. A function $f: V_1 \rightarrow V_2$ is an <u>isomorphism</u> if a) f is a bijection G(G) and G(G) are adj. if and only if a and b are adj. If any isomorphism exists, G and G are isomorphic

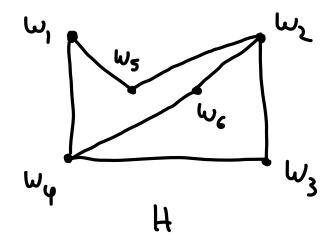
Two ways to show two graphs are irom.

- 1) Find an isomorphism (examples last time)
- 2) Show that the adjacency matrices are the same for some ordering of the vertices

(always same ordering on nows & cols!)

Ex 11:





$$Adi_{H} = \begin{cases} W_{1} & W_{2} & W_{3} & W_{4} & W_{5} & W_{6} \\ W_{1} & 0 & 0 & 1 & 1 & 0 \\ W_{2} & 0 & 0 & 1 & 0 & 1 \\ W_{3} & 0 & 1 & 0 & 1 & 0 \\ W_{4} & 1 & 0 & 1 & 0 & 0 & 0 \\ W_{5} & 1 & 1 & 0 & 0 & 0 & 0 \\ W_{6} & 0 & 1 & 0 & 1 & 0 & 0 \end{cases}$$

Not the same

But... put the vertices in a different order, and

So G and H are isomorphic.

§10.4: Connectivity

Def: A path is an alternating sequence

Vo, e,, V,, ez, --, en, Vn

Vi EV, eif E ei has endpoints Vi-1 & Vi

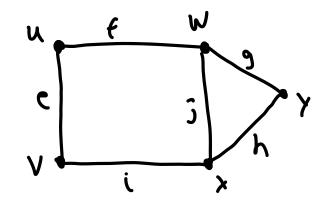
If no repeated edges, the path is simple

If vo = vn, it is a circuit

If G is a simple graph, don't need to write the edges, since they're implies

* Note: terminology matches Rosen, different from other sources

Class activity:



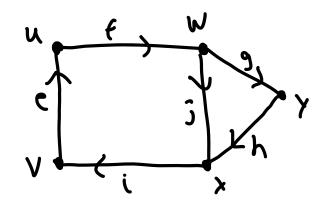
Which of the following are paths? Circuits? Simple paths/circuits?

α) ω, ξ, ω, ;, x, i, ν, e, α δ) ω, ω, x, ν, α c) ω, e, ω, i, x, i, ν, ξ, α

d) ω, ω, χ, γ, ω, χ, γ e) ω, ε, ω, ε, ω

Def: Paths/circuits are the same in digraphs except they must follow the arrow

Class activity:



Which of the following are paths? Circuits? Simple paths/circuits?

σ) u, ξ, ω, ; , x, i, v, e, u δ) u, ω, x, v, u

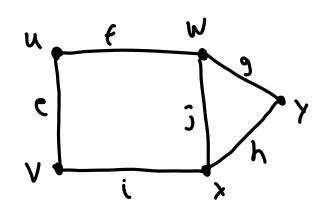
c) u, e, w, i, x, i, v, f, u

d) u, w, x, y, w, x, y

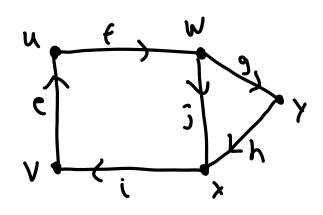
e) u, f, w, f, w, f, w

Def: a) A graph is connected if there is a Path from every vertex to every other vertex b) A digraph is strongly connected if there is a Path from every vertex to every other vertex c) A digraph is weakly connected if there is a Path from every vertex to every other vertex in the underlying graph (erase the arrows) d) A cut edge/cut vertex in a graph is an edge/ vertex which, when deleted, disconnects the graph

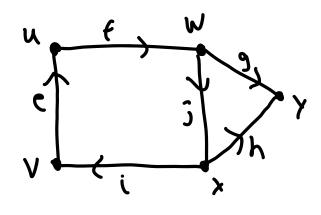
Examples:



Connected, no cat-edges/vertices



strongly conn.

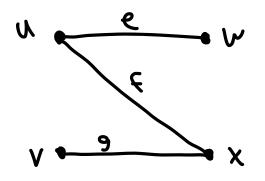


weakly conn.
since no path from
y to e.g. v

U • W

dis connected





connected cut-vertices: u,x cut-edge: f