109705040 戏暖晨

22.
$$P^{2} = \begin{bmatrix} \frac{1}{5} & \frac{1}{10} \\ \frac{1}{5} & \frac{1}{10} \end{bmatrix} = \begin{bmatrix} \frac{1}{5} & \frac{1}{10} \\ \frac{1}{5} & \frac{1}{5} \end{bmatrix} \Rightarrow \text{Regular}.$$

$$\begin{cases} \frac{1}{5} & \frac{1}{10} \\ \frac{1}{5} & \frac{1}{10} \end{bmatrix} = \begin{bmatrix} \chi \\ \chi \\ \chi \end{bmatrix} = \begin{bmatrix} \chi \\ \chi \\ \chi \end{bmatrix} = \begin{bmatrix} \chi \\ \chi \\ \chi \end{bmatrix}$$

$$\begin{cases} \frac{1}{5} & \frac{1}{10} \\ \frac{1}{5} & \frac{1}{10} \end{bmatrix} = \begin{bmatrix} \chi \\ \chi \\ \chi \end{bmatrix} = \begin{bmatrix} \chi \\ \chi \\ \chi$$

42.
$$P\overline{X} = \overline{X} \qquad \qquad \stackrel{?}{\searrow} \overline{X} = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$\begin{bmatrix} 0.1 & 0 & 0 \\ 0.3 & 1 & 0 \\ 0.7 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$\begin{cases}
0.1X = X \\
0.2X+y = y \\
0.1X+z=z
\end{cases} \Rightarrow y=t, 0 \le t \le 1$$

$$X+y+z=1$$

$$X+y+z=1$$

44.
$$PX = X$$
 $\hat{z}X = \begin{bmatrix} w \\ x \\ y \end{bmatrix}$

$$\begin{bmatrix} 0.7 & 0 & 0.2 & 0.1 \\ 0.1 & 1 & 0.5 & 0.6 \\ 0 & 0 & 0.2 & 0.2 \\ 0.2 & 0 & 0.1 & 0.1 \end{bmatrix} \begin{bmatrix} w \\ x \\ y \\ z \end{bmatrix} = \begin{bmatrix} w \\ x \\ y \\ z \end{bmatrix}$$

$$\begin{cases} 0.7 w \cdot +0.5y + 0.12 = w \\ 0.1 w + x +0.5y +0.62 = x \\ +0.2y +0.22 = y \\ 0.3w +0.1y +0.1z = z \\ w + x + y + z = 1 \end{cases} \Rightarrow \begin{cases} w = 0 \\ y = 0 \\ z = 0 \end{cases}$$

$$|X| = 0$$

$$\left[\begin{array}{cc} (8 & -16) \\ \left[\begin{array}{cc} 1 & -3 \\ 1 & -3 \end{array} \right] = \left[\begin{array}{cc} 0 & 16 \end{array} \right]$$

$$\begin{bmatrix} \xi & -\beta_0 \end{bmatrix} \begin{bmatrix} 1 & -2 \\ 1 & -2 \end{bmatrix} = \begin{bmatrix} 2 & -\beta \end{bmatrix}$$

$$\begin{bmatrix} 42 & -26 \end{bmatrix} \begin{bmatrix} 1 & -2 \\ 1 & -3 \end{bmatrix} = \begin{bmatrix} 14 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 2| & 0 \end{bmatrix} = \begin{bmatrix} 1 & -1 \\ 1 & -1 \end{bmatrix} = \begin{bmatrix} 27 & 27 \end{bmatrix}$$

$$\begin{bmatrix} \lambda & -\lambda \end{bmatrix} \begin{bmatrix} 1 & -\lambda \\ 1 & -\lambda \end{bmatrix} = \begin{bmatrix} 0 & \lambda \end{bmatrix}$$

$$\begin{bmatrix} 12 & -10 \end{bmatrix} \begin{bmatrix} 1 & -2 \\ 1 & -2 \end{bmatrix} = \begin{bmatrix} 5 & 0 \end{bmatrix}$$

> JOHN RETURN TO BASE

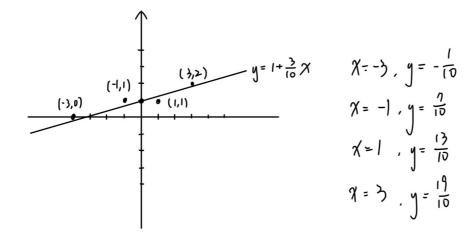
$$\chi = \begin{bmatrix}
1 & -3 \\
1 & -1 \\
1 & 1 \\
1 & 3
\end{bmatrix} \qquad
 y = \begin{bmatrix}
0 \\
1 \\
1 \\
2
\end{bmatrix}$$

$$\chi^{T}\chi = \begin{bmatrix} 1 & 1 & 1 & 1 \\ -3 & -1 & 1 & 3 \end{bmatrix} \begin{bmatrix} 1 & -3 \\ 1 & -1 \\ 1 & 1 \end{bmatrix} = \begin{bmatrix} 4 & 0 \\ 0 & 20 \end{bmatrix}$$

$$\chi^{T}Y = \begin{bmatrix} 1 & 1 & 1 & 1 \\ -3 & -1 & 1 & 3 \end{bmatrix} \begin{bmatrix} 0 \\ 1 \\ 1 \\ 2 \end{bmatrix} = \begin{bmatrix} 4 \\ 6 \end{bmatrix}$$

$$A = (\chi^{T} \chi)^{-1} \chi^{T} \chi = \frac{1}{80} \begin{bmatrix} 20 & 0 \\ 0 & 4 \end{bmatrix} \begin{bmatrix} 4 \\ 6 \end{bmatrix} = \frac{1}{80} \begin{bmatrix} 20 \\ 24 \end{bmatrix} = \begin{bmatrix} 1 \\ \frac{2}{10} \end{bmatrix}$$

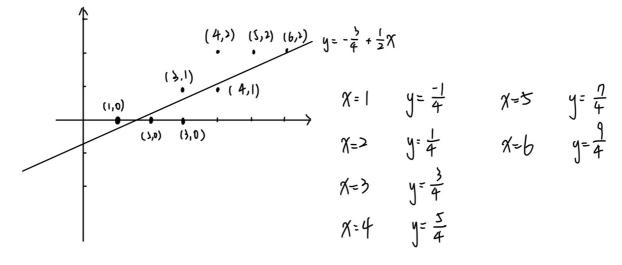
... the least squares regression line is $y = 1 + \frac{3}{10}x$.



$$(0-(-\frac{1}{5}))^{\frac{1}{5}}+(1-\frac{1}{10})^{\frac{1}{5}}+(\frac{13}{10}-1)^{\frac{1}{5}}+(2-\frac{19}{10})^{\frac{1}{5}}=\frac{1}{5}$$

$$A = \left(\chi^{T}\chi\right)^{T}\chi^{T}\gamma = \frac{1}{1+4}\begin{bmatrix}11b & -38\\ -38 & 8\end{bmatrix}\begin{bmatrix}8\\ 37\end{bmatrix} = \frac{1}{1+4}\begin{bmatrix}-108\\ 72\end{bmatrix} = \begin{bmatrix}\frac{-2}{4}\\ \frac{1}{2}\end{bmatrix}$$

... the least squares regression line is $y = \frac{-3}{4} + \frac{1}{5} x$.



$$\left[\left(0 - \left(-\frac{1}{4} \right) \right)^{2} + \left(\frac{1}{4} - 0 \right)^{2} + \left(\frac{3}{4} - 0 \right)^{2} + \left(\frac{3}{4} - 1 \right)^{2} + \left(\frac{5}{4} - 1 \right)^{2} + \left(\frac{5}{4} - 2 \right)^{2} + \left(\frac{7}{4} - 2 \right)^{2} + \left(\frac{9}{4} - 2 \right)$$